

The Kuiper Belt:

*Shedding light on Planet Formation & Collisional
Evolution in Debris Disks*



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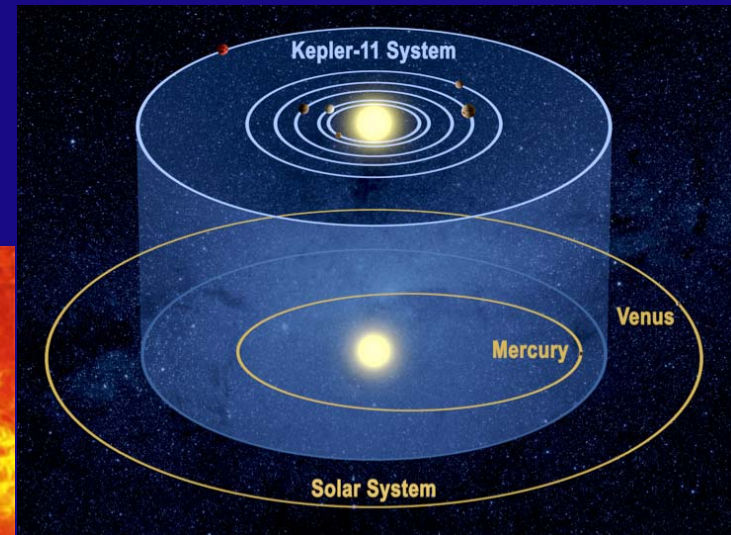
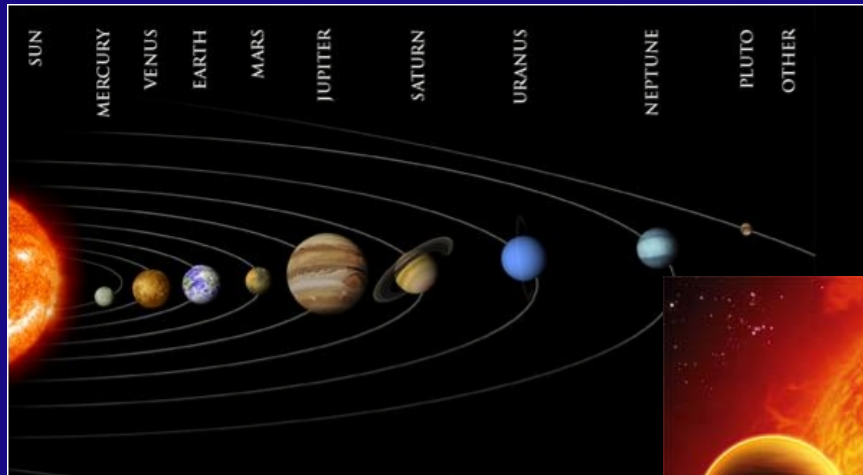
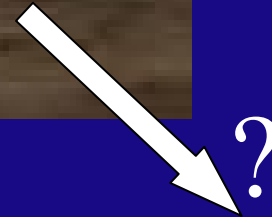
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The Future of Astronomy

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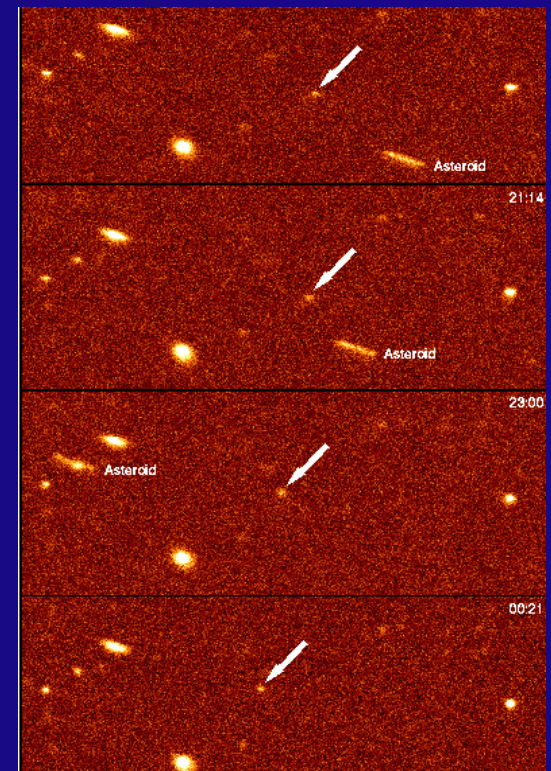
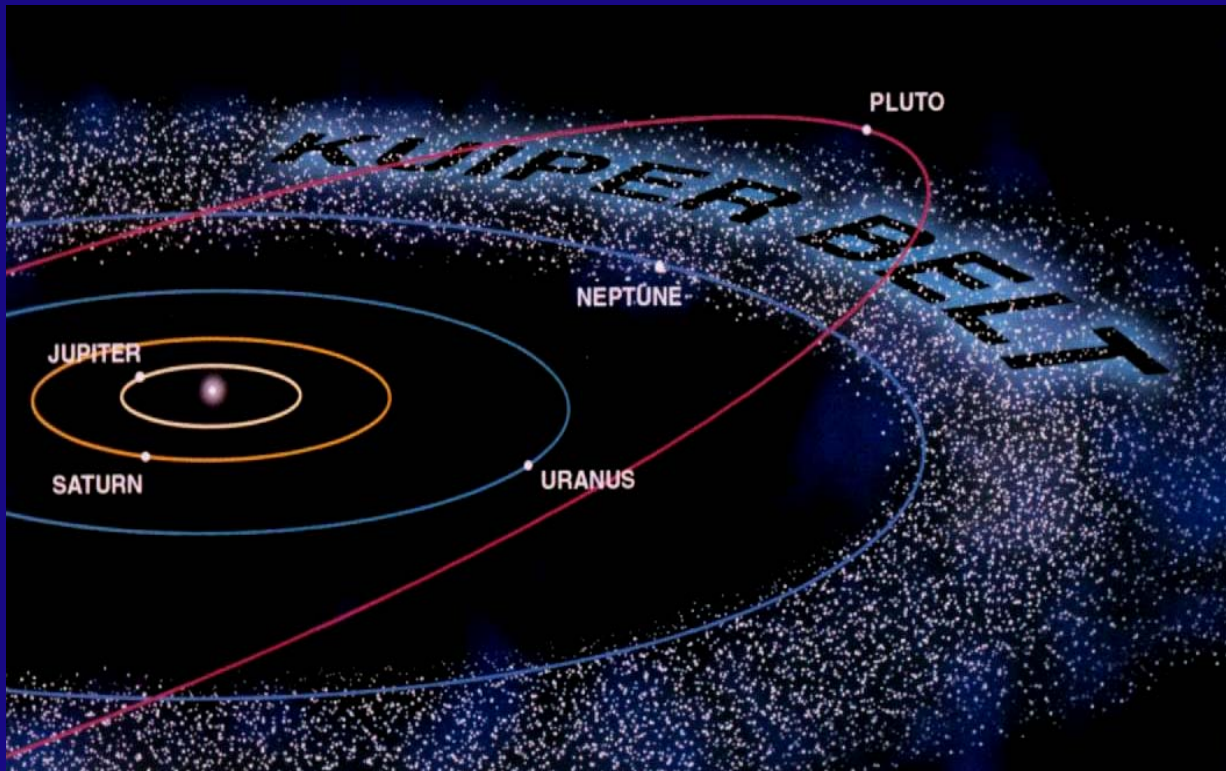
September 2nd 2011

From Gas & Dust to Planets

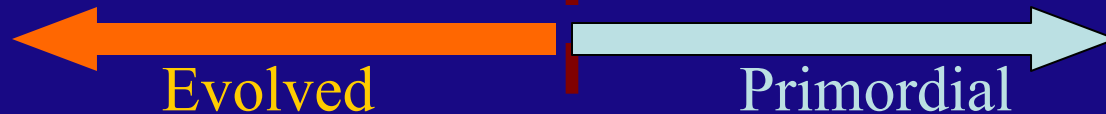
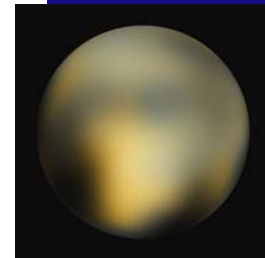
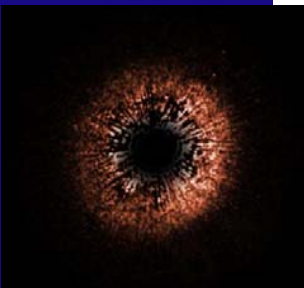
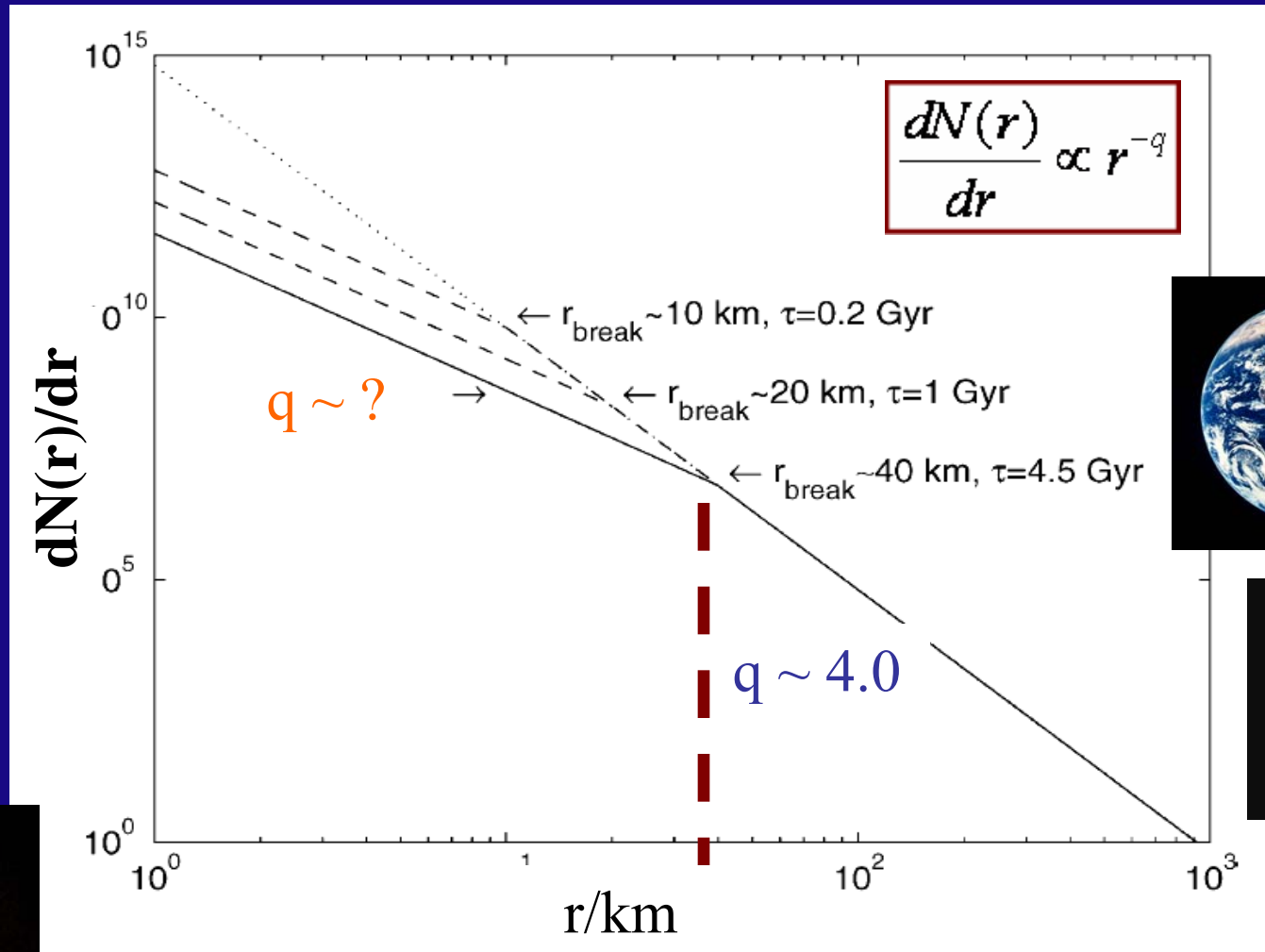


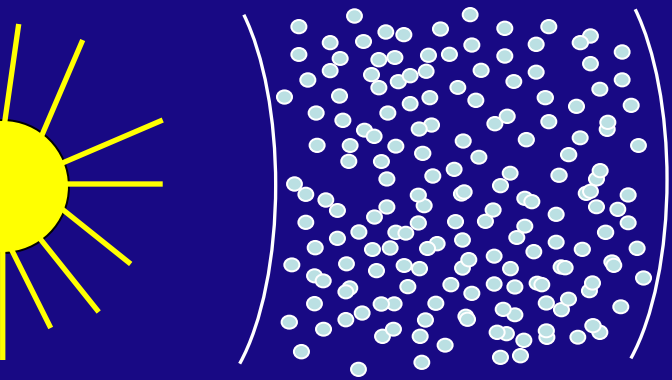
Kuiper Belt

- ~40 AU from the Sun
- Source of the short period comets
- ~1000 detected objects
- Solar System Debris Disk
- Size estimates based on brightness
 - Typical radius $R=100\text{km}$

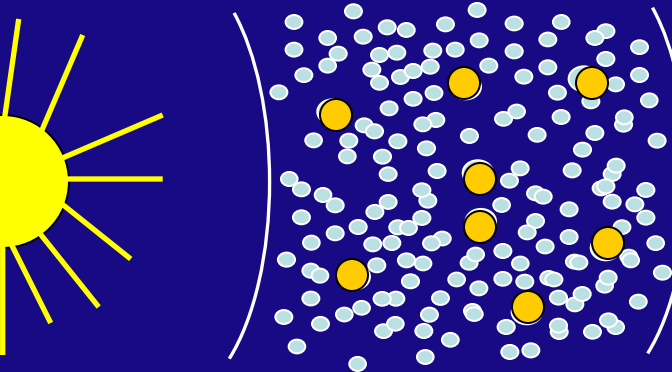


The Kuiper Belt Size Distribution





1. Planetesimal formation:

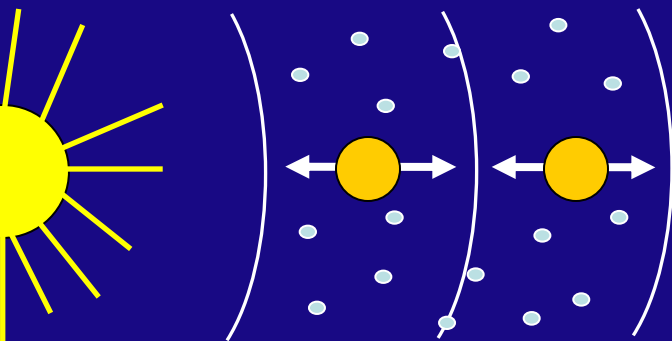


2. Runaway growth:

$$\frac{1}{R_1} \frac{dR_1}{dt} \propto R_1$$

For $v_{\text{esc}} > u$ gravitational focusing enhances the accretion rate

$$\frac{1}{R} \frac{dR}{dt} \sim \frac{\sigma \Omega}{\rho R} \left(\frac{v_{\text{esc}}}{u} \right)^2 \longrightarrow t_{\text{grow}} \sim 10^7 \text{ years}$$



3. Oligarchic growth & Isolation:

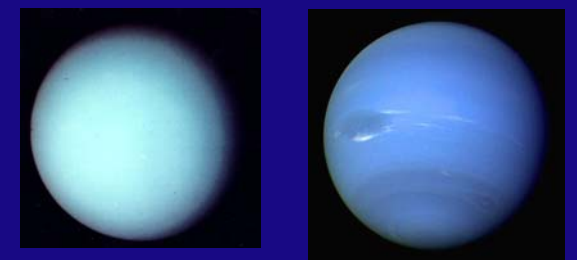
$$M_{\text{iso}} \approx 2\pi a (\Delta a_{\text{zone}}) \Sigma \sim M_{\text{Neptune}}$$

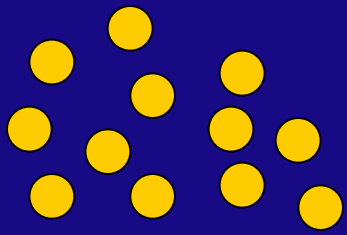
planetesimals

protoplanets

$$u, \sigma$$

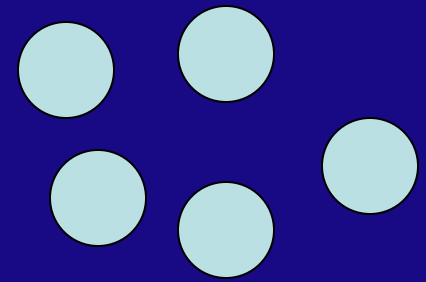
$$v, \Sigma$$





Small bodies

Runaway Growth



Big Bodies

$$\frac{1}{R} \frac{dR}{dt} \sim \frac{\sigma \Omega}{\rho R} \left(\frac{u}{v_{esc}} \right)^{-2} + \frac{\Sigma \Omega}{\rho R} \alpha^{-3/2}$$

Accretion of small
bodies

Accretion of big
bodies

$$\alpha \sim R_{Sun} / a$$

$$\sim 10^{-4} \text{ at } 40 \text{ AU}$$

When accretion of small and big bodies contribute equally to the growth:

$$\Sigma \sim \alpha^{3/4} \sigma \sim 10^{-3} \sigma \sim 3 \times 10^{-4} \text{ g/cm}^2$$

$$\sigma \sim \sigma_{MMSN}$$

$$\sim 0.3 \text{ g/cm}^2$$

$$\Sigma \propto N(> R) R^3 \sim \text{const}$$



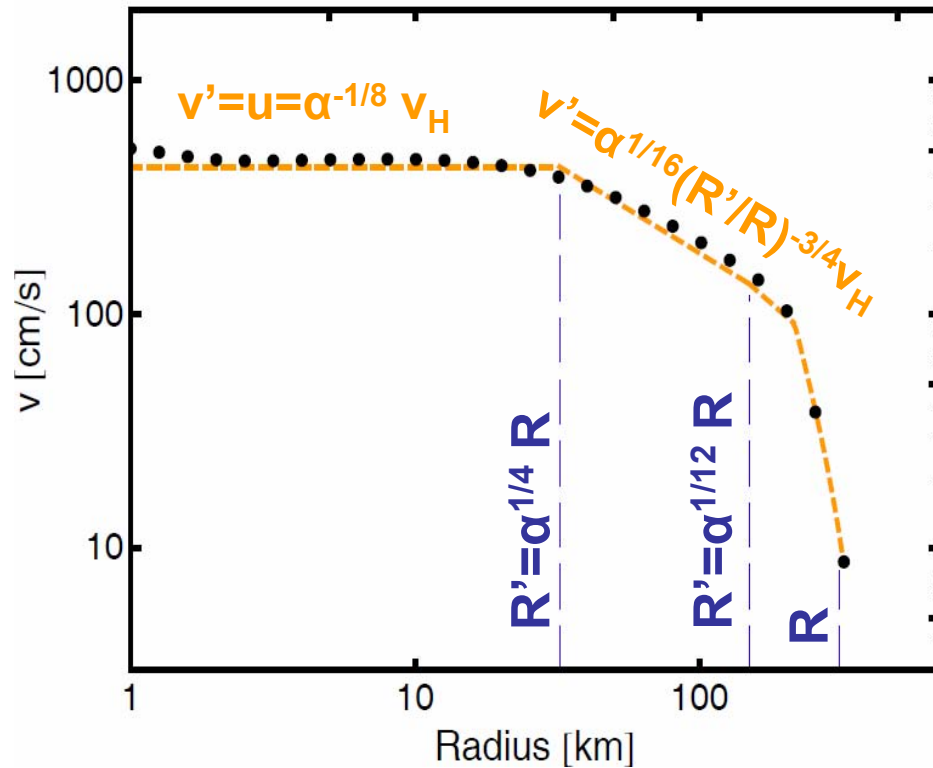
$$N(> R) \propto R^{-3}$$



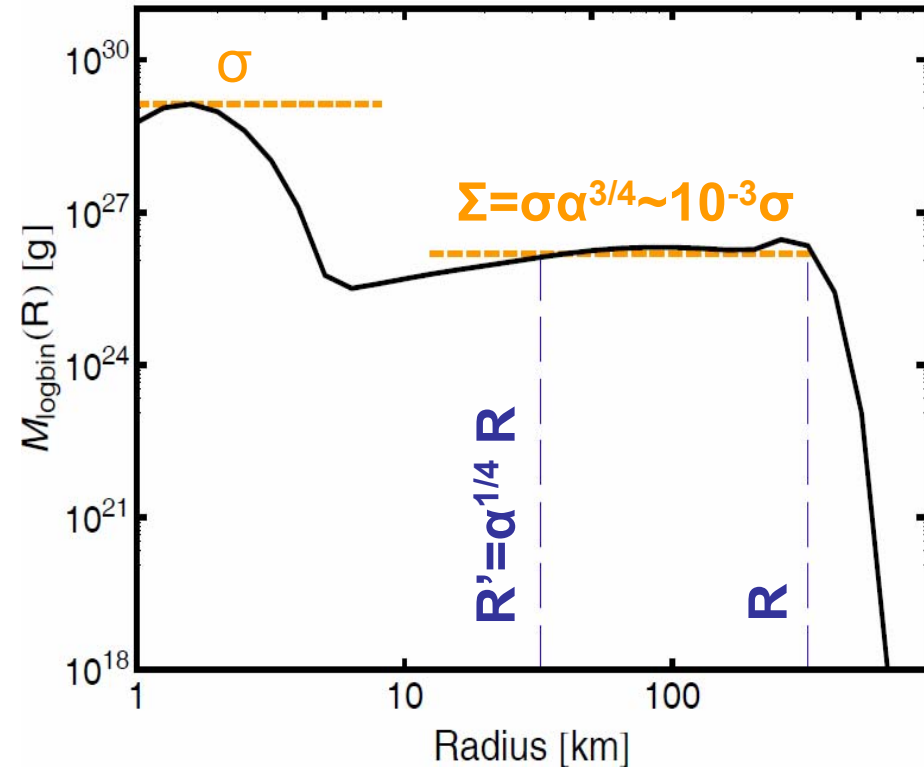
$$q = 4$$

i.e. Equal mass per logarithmic mass bin

Velocity

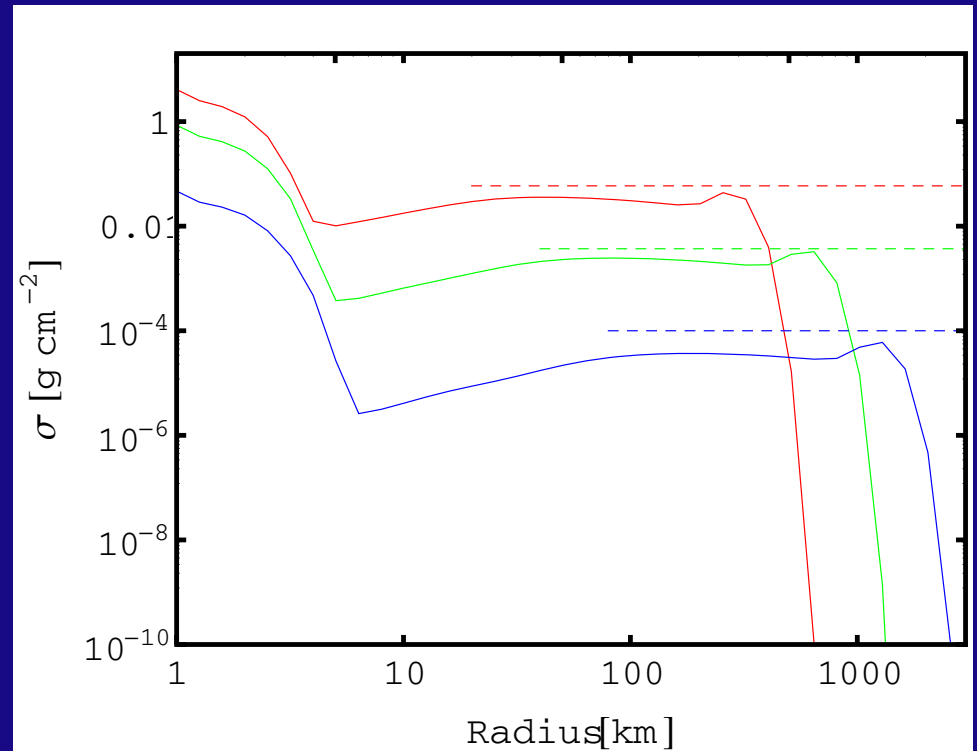
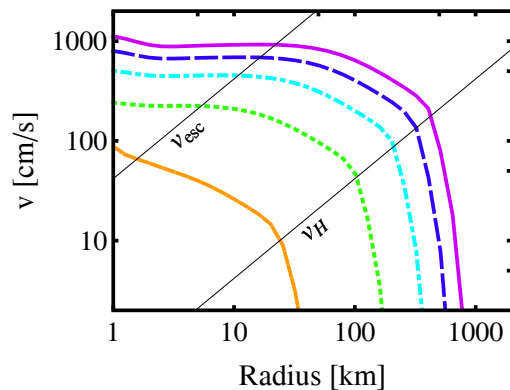
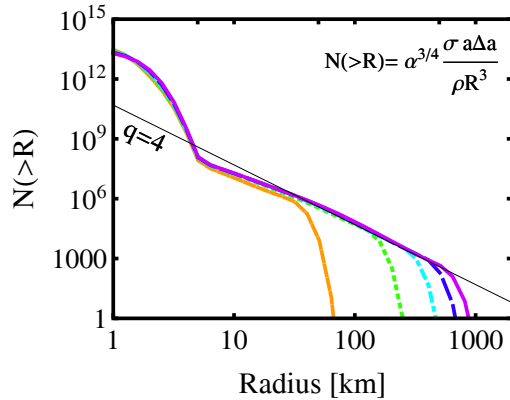
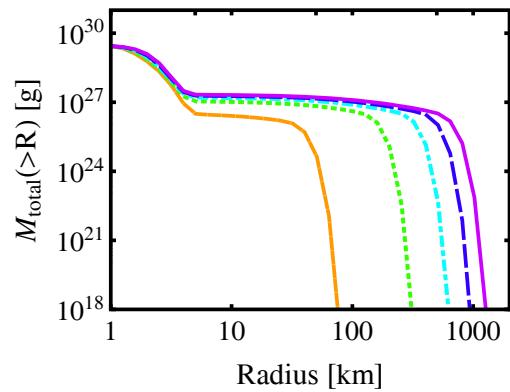


Mass



(Schlichting & Sari, 2011)

Time = 10^7 years



$$\frac{dN(R)}{dR} \propto R^{-q}$$

(Schlichting & Sari, 2011)

$t = 10^6$ years, $t = 10^7$ years, $t = 2 \times 10^7$ years, $t = 3 \times 10^7$ years, $t = 5 \times 10^7$ years

Results

Runaway growth:

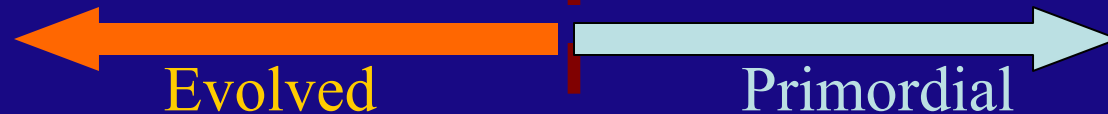
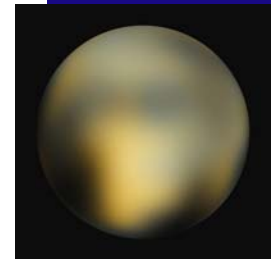
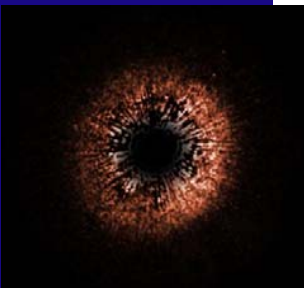
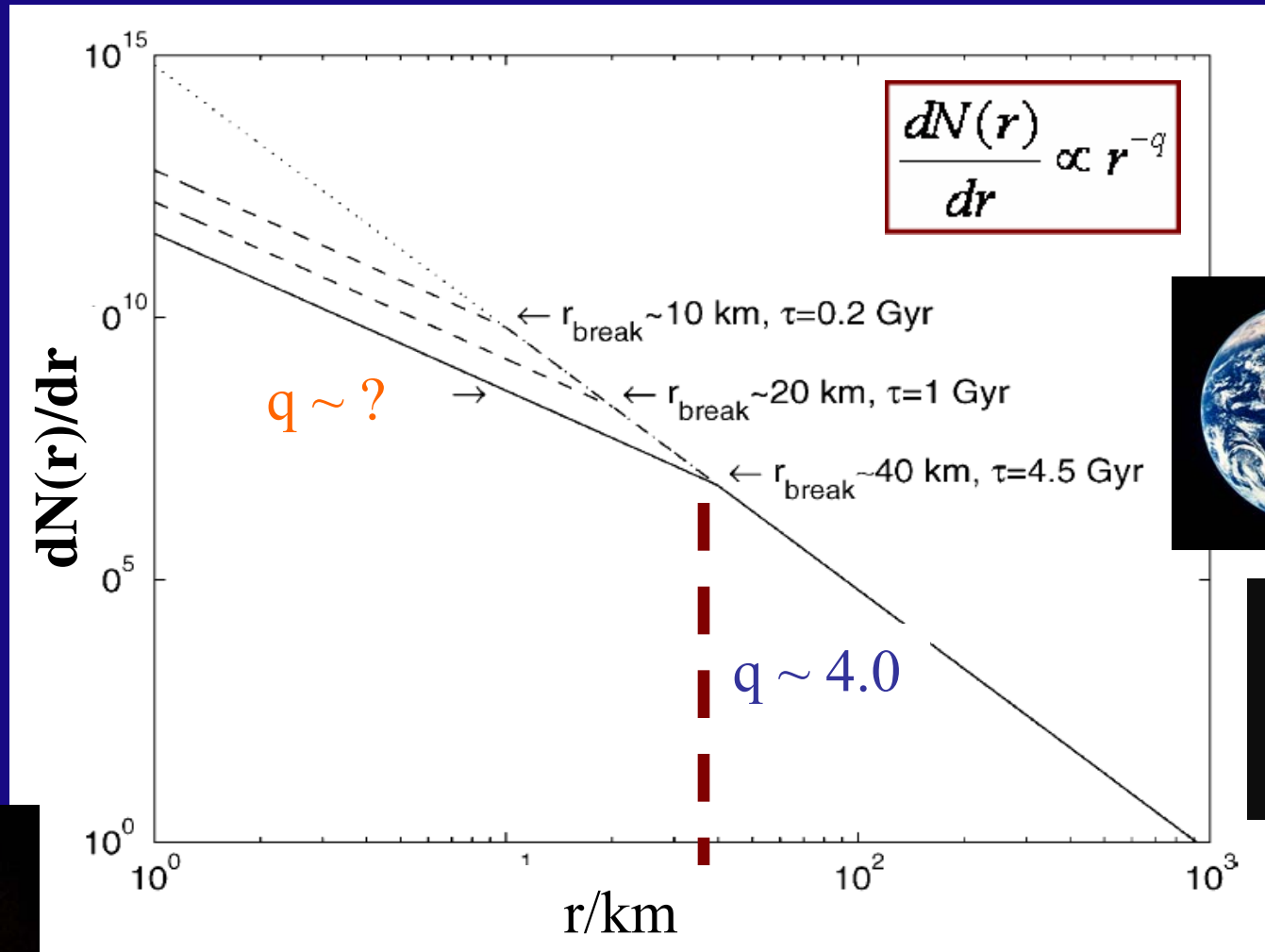
- 1) Only a small fraction of initial mass is converted into protoplanets during runaway growth: $\Sigma \sim \sigma \alpha^{3/4} \sim 10^{-3} \sigma_{\text{MMSN}}$
- 2) Size distribution of runaway tail: $q \sim 4$, equal mass per logarithmic mass bin
- 3) Results also apply to debris disks

For the Kuiper Belt we can successfully explain:

- 1) The total mass in large KBOs ($\Sigma \sim \sigma \alpha^{3/4} \sim 10^{-3} \sigma_{\text{MMSN}}$)
- 2) The slope of KBO size distribution ($q \sim 4$)

This argues strongly against that there was significantly more mass in large Kuiper Belt objects in the past.

The Kuiper Belt Size Distribution

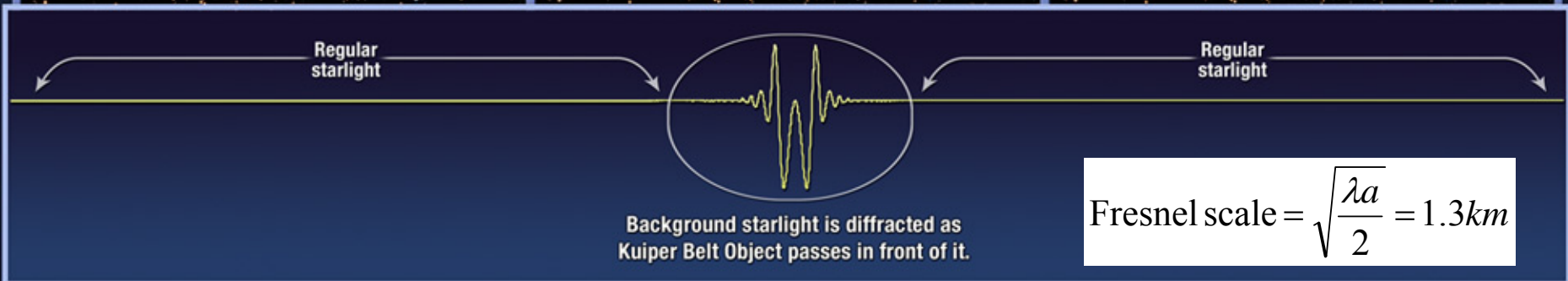


Transiting Kuiper Belt Objects

KBOs < 10km too small to be detected directly

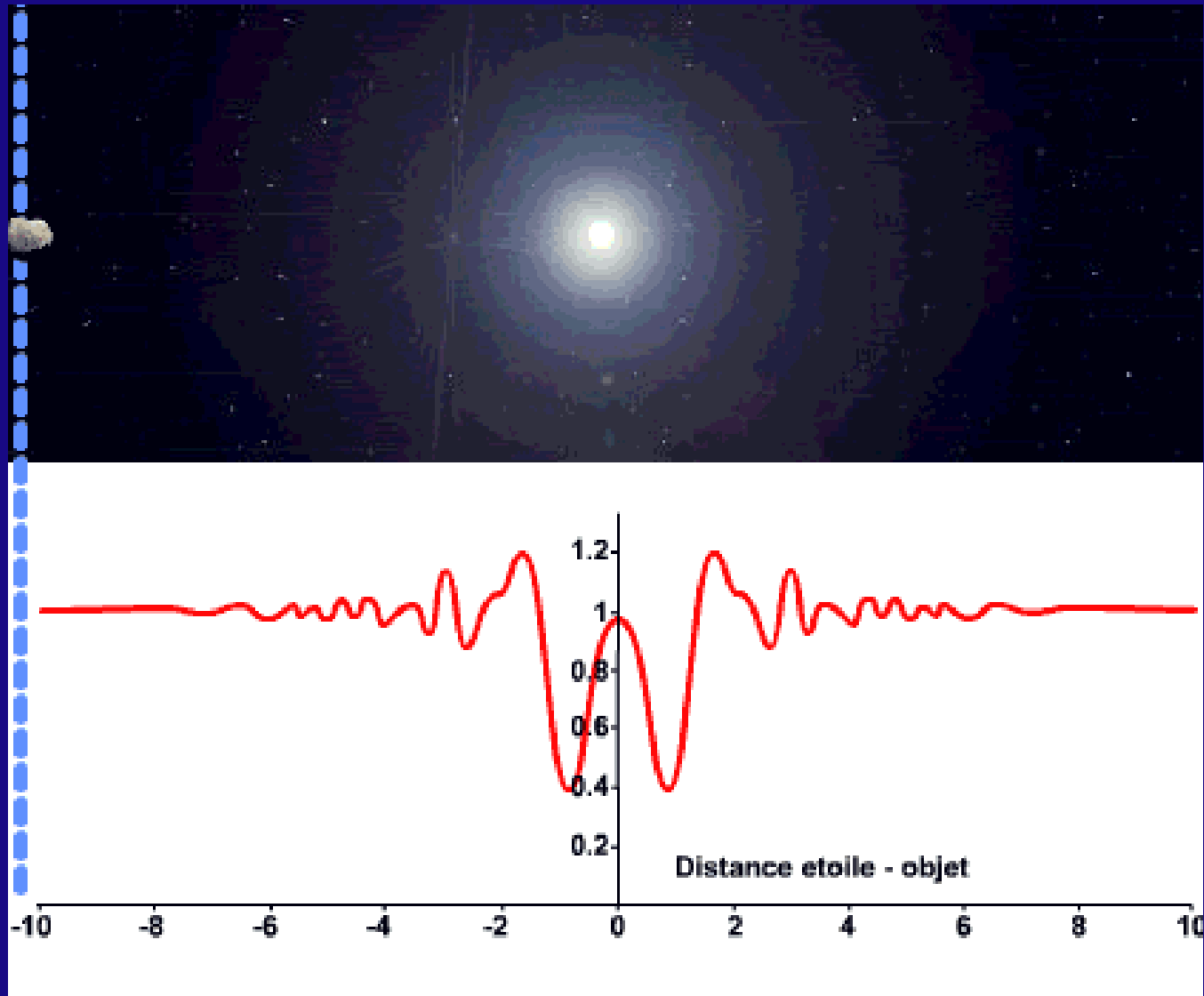
→ Observe indirectly using stellar occultations

(Dyson 1992, Axelrod et al. 1992)



$$\text{Fresnel scale} = \sqrt{\frac{\lambda a}{2}} = 1.3 \text{ km}$$

Transiting Kuiper Belt Objects



(Roques)

Event Duration $\sim 3\text{km}/v_{\text{earth}} \sim 3\text{km}/30\text{km/s} \sim 0.1 \text{ s!}$

Occultation events produced by KBOs are rare & of short duration



Large number of star hours & high frequency



HST Fine Guidance Sensors

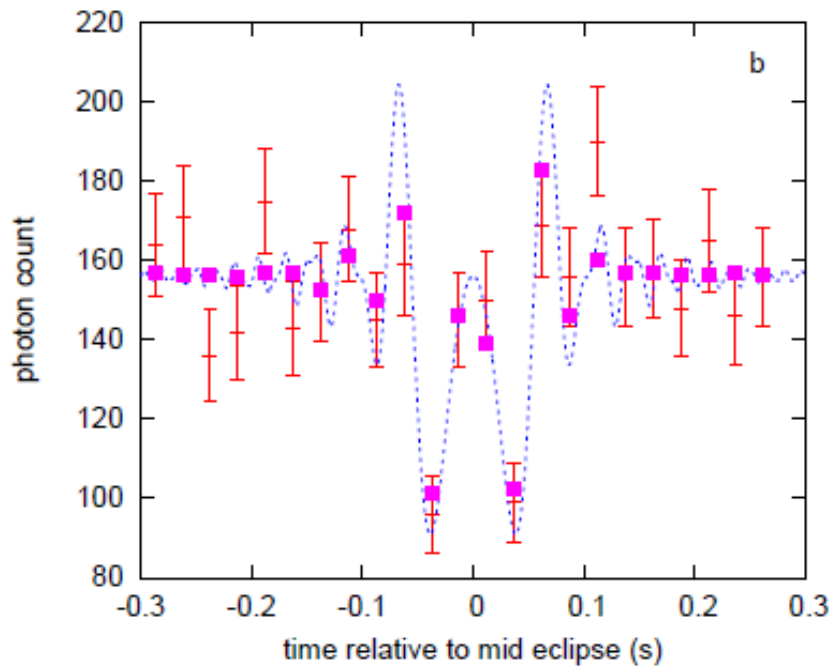
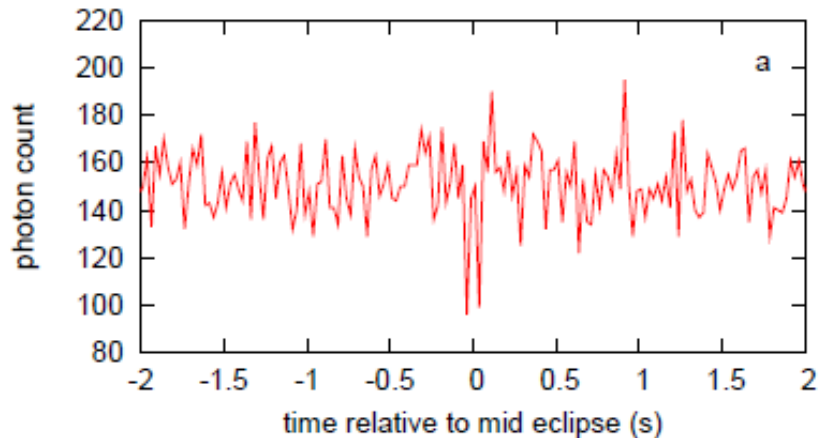
- FGS observations are ideal because

- 1) 40 Hz sampling frequency
- 2) long baseline: 16 years
- 3) space based
- 4) good control sample

$q_2 \sim 4.5$	~ 180 events	no break
$q_2 \sim 3.5$	~ 1 event	break

- $\sim 40,000$ Star hours of observations with $i < 20$ deg
- Typical size that can be detected $r \sim 250\text{m}$





Best fit values:

$$r \sim 520 \text{ m} \quad r \propto \sqrt{\text{amplitude}}$$

$$a \sim 45 \text{ AU}$$

Chi-squared fit:

$$\chi^2 / \text{dof} = 20.1 / 21$$

From the observations we know:

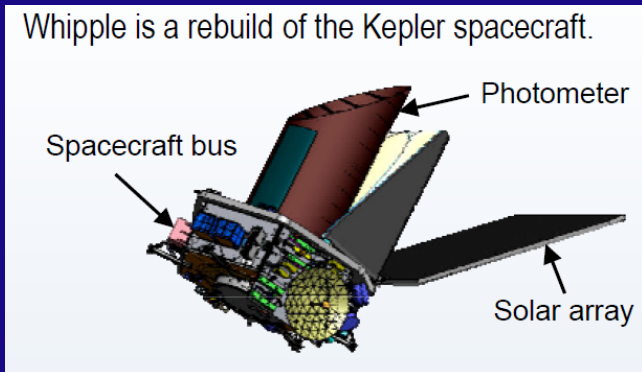
- $\theta_{\text{Star}} / \theta_{\text{Fresnel}} \sim 0.3$
- Ecliptic latitude +14 deg
- Compared PMT readings
- Checked second FGS
- No correlated noise
- Examined the engineering telemetry for HST
- Less than 2% chance to be false-positive

Implications

- Break in KBO Size Distribution \longrightarrow Collisional evolution
- Small KBO size distribution similar to Centaurs ($q \sim 4$, Sheppard et al. 2000) \longrightarrow Kuiper Belt source region of Centaurs
- Inferred KBO abundance consistent with required supply rate for Jupiter Family Comets (Volk & Malhotra 2008, Chiang & Pan 2010)

Future

- Analyze the remaining 66% to the data
- Whipple Mission



$$q = 3.9 \pm 0.3$$

$$N(r > 250m) = 2.1_{-1.7}^{+4.8} \times 10^7 \text{ deg}^{-2}$$

