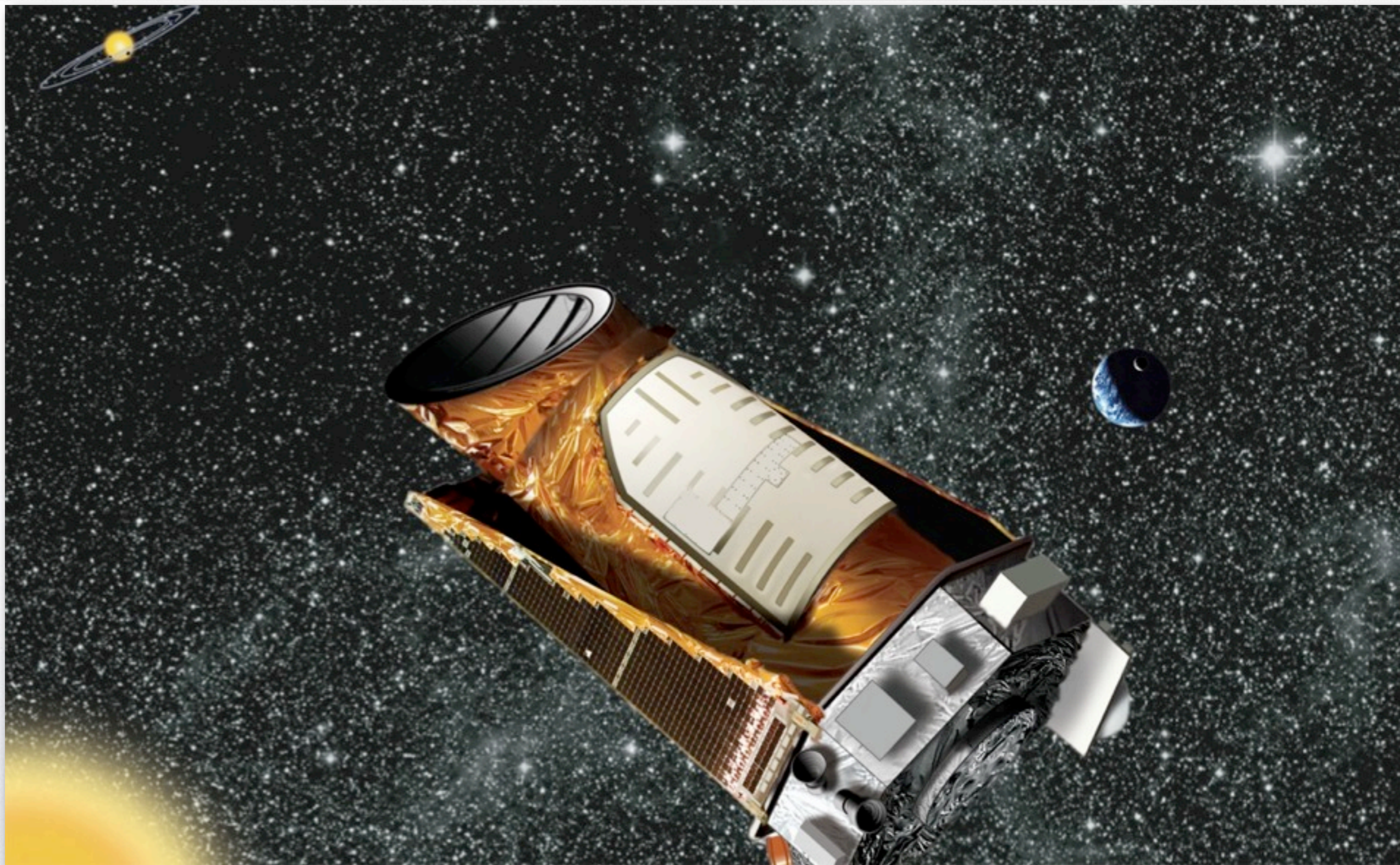
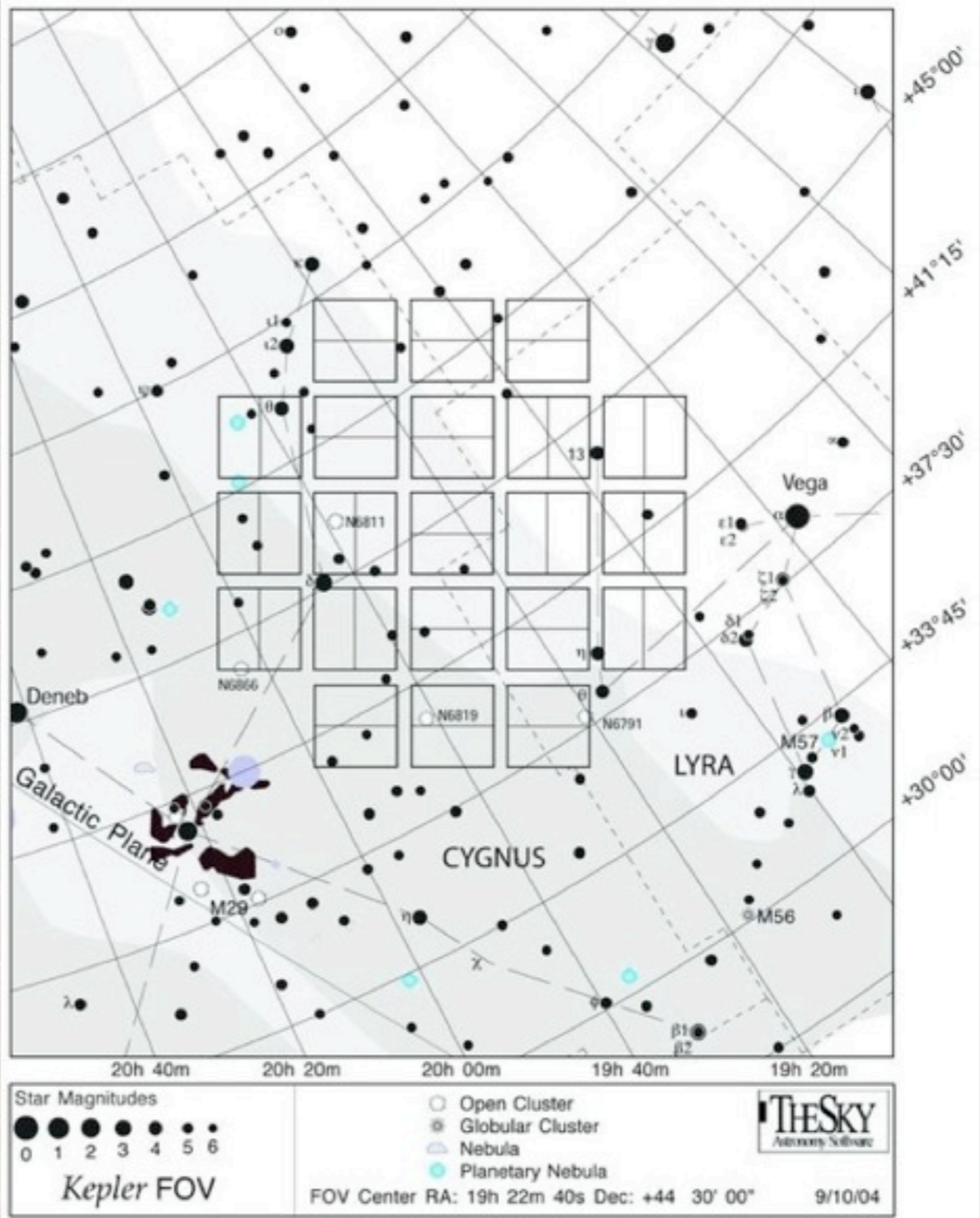
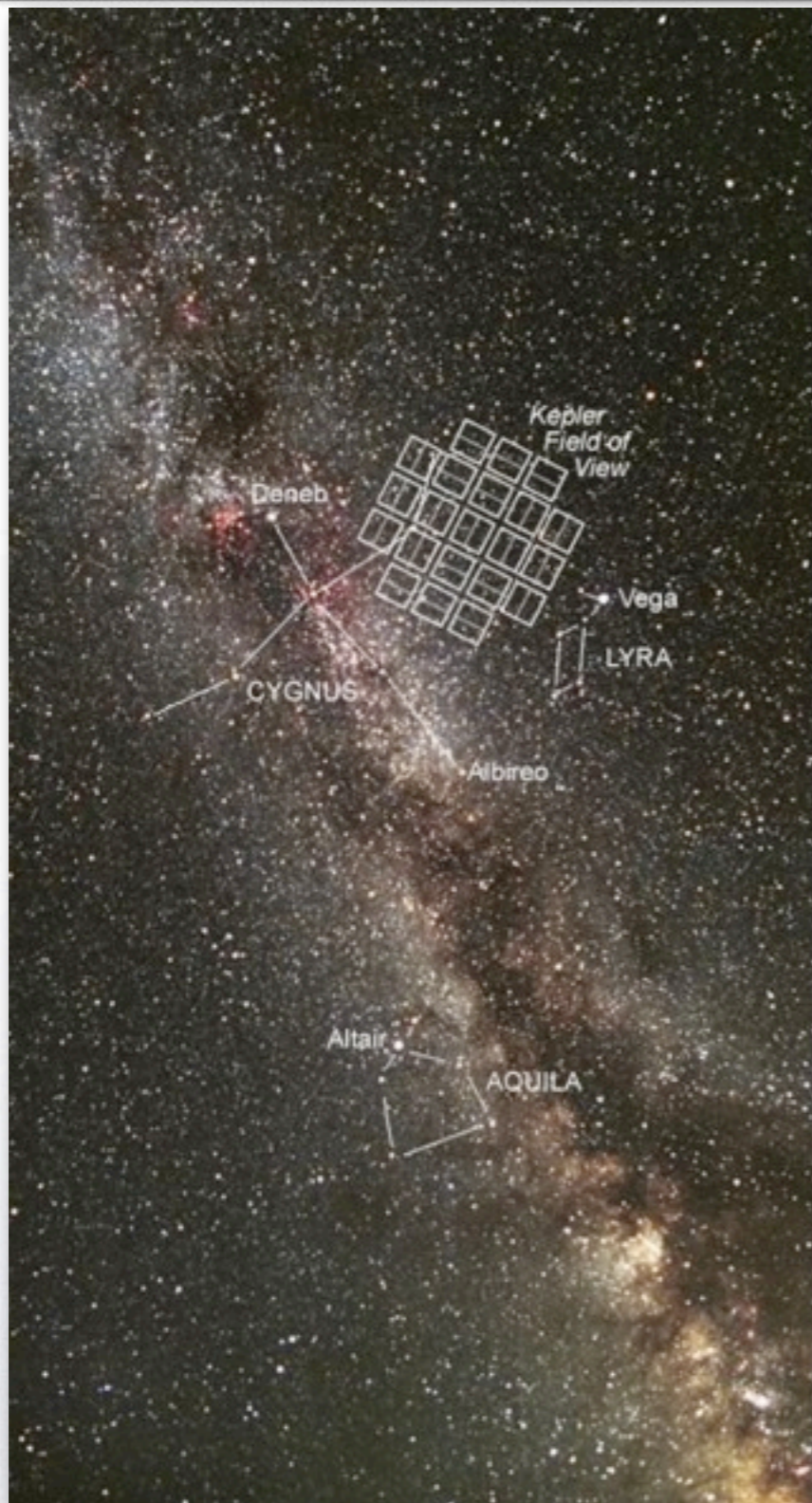


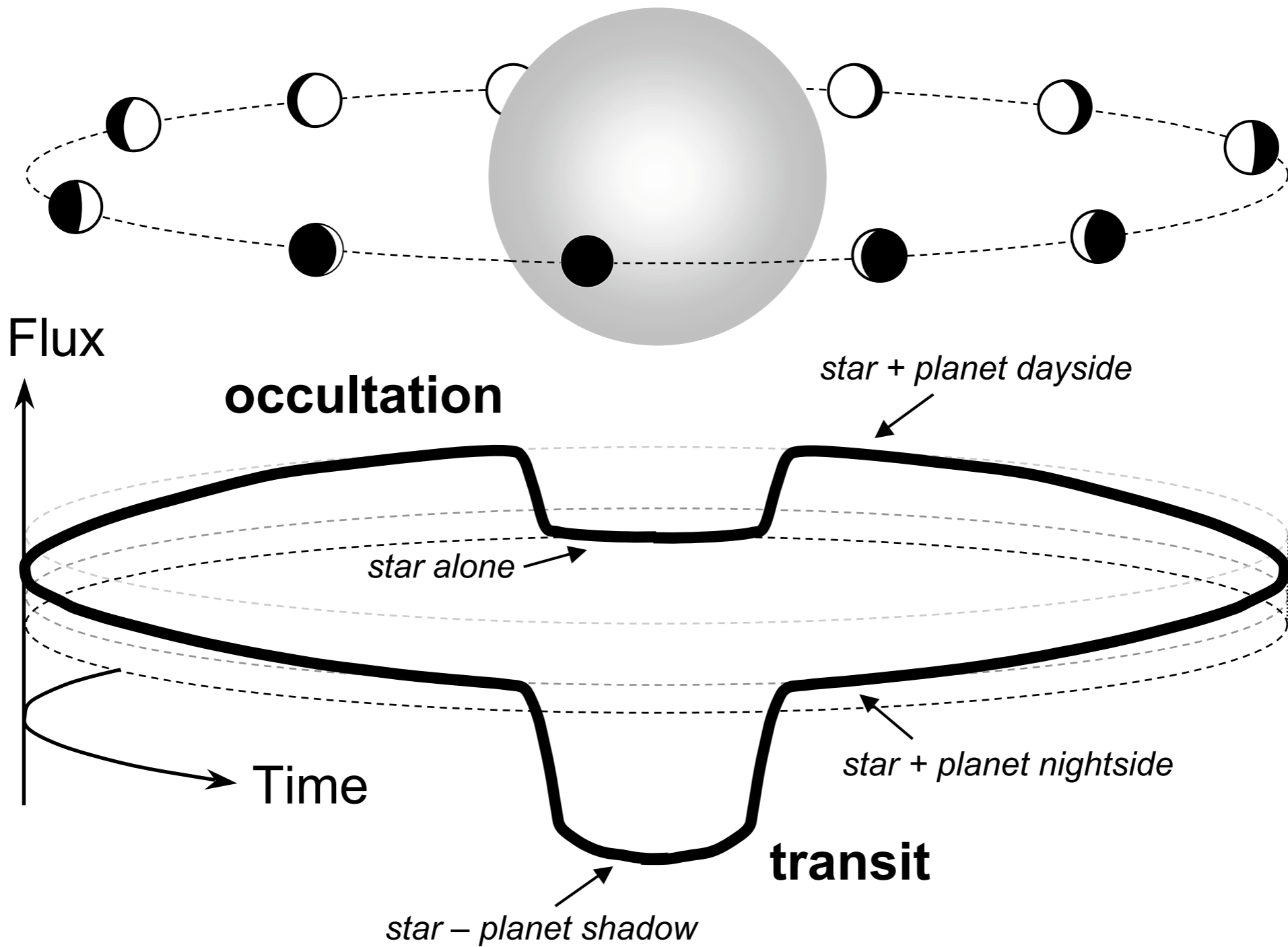
Kepler's Multi-Eclipsing Hierarchical Triples: “Photodynamical Fits” & Accurate Masses and Radii

Josh Carter
Hubble Fellow
(Smithsonian Astrophysical Observatory)

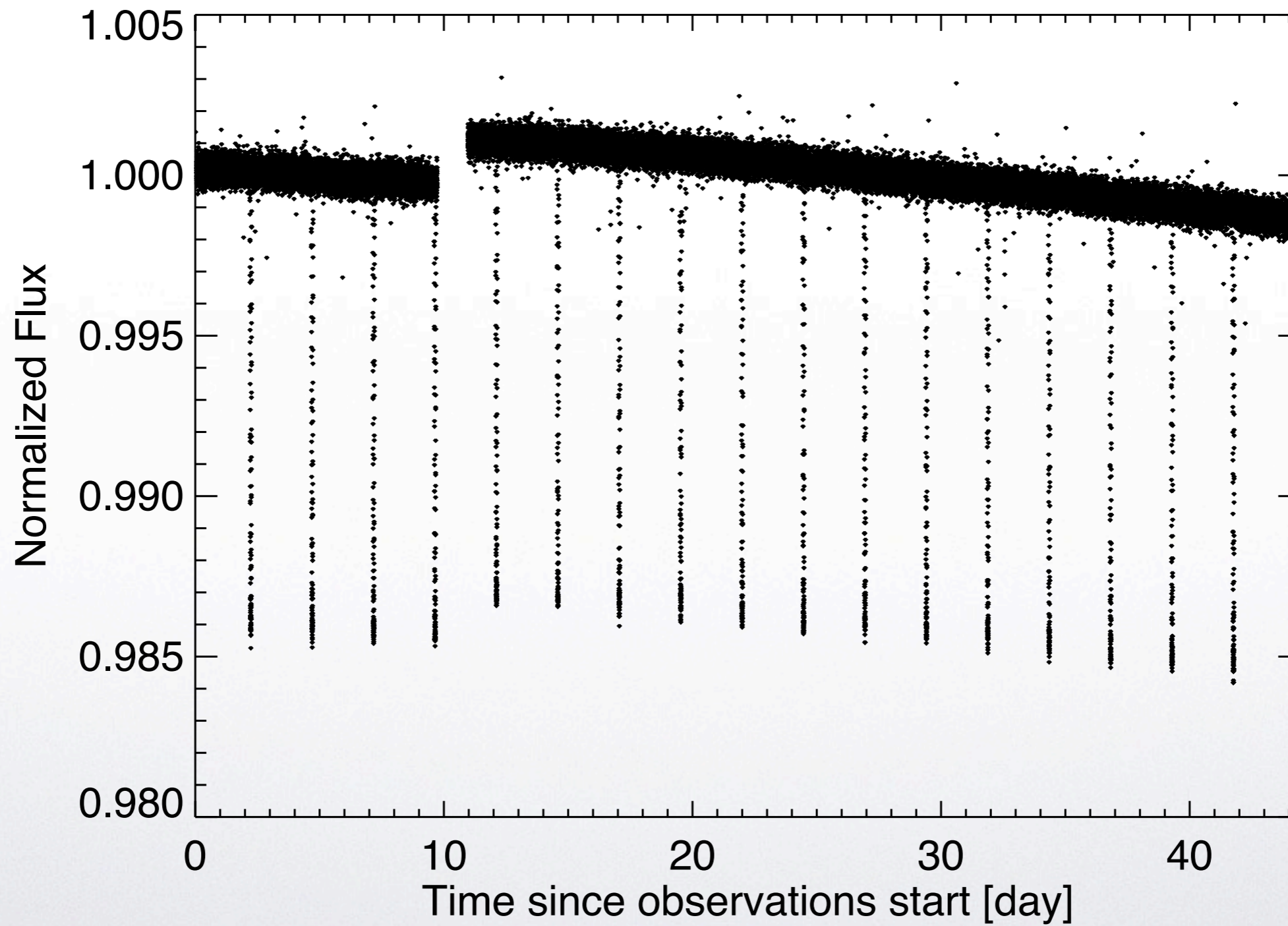
Kepler



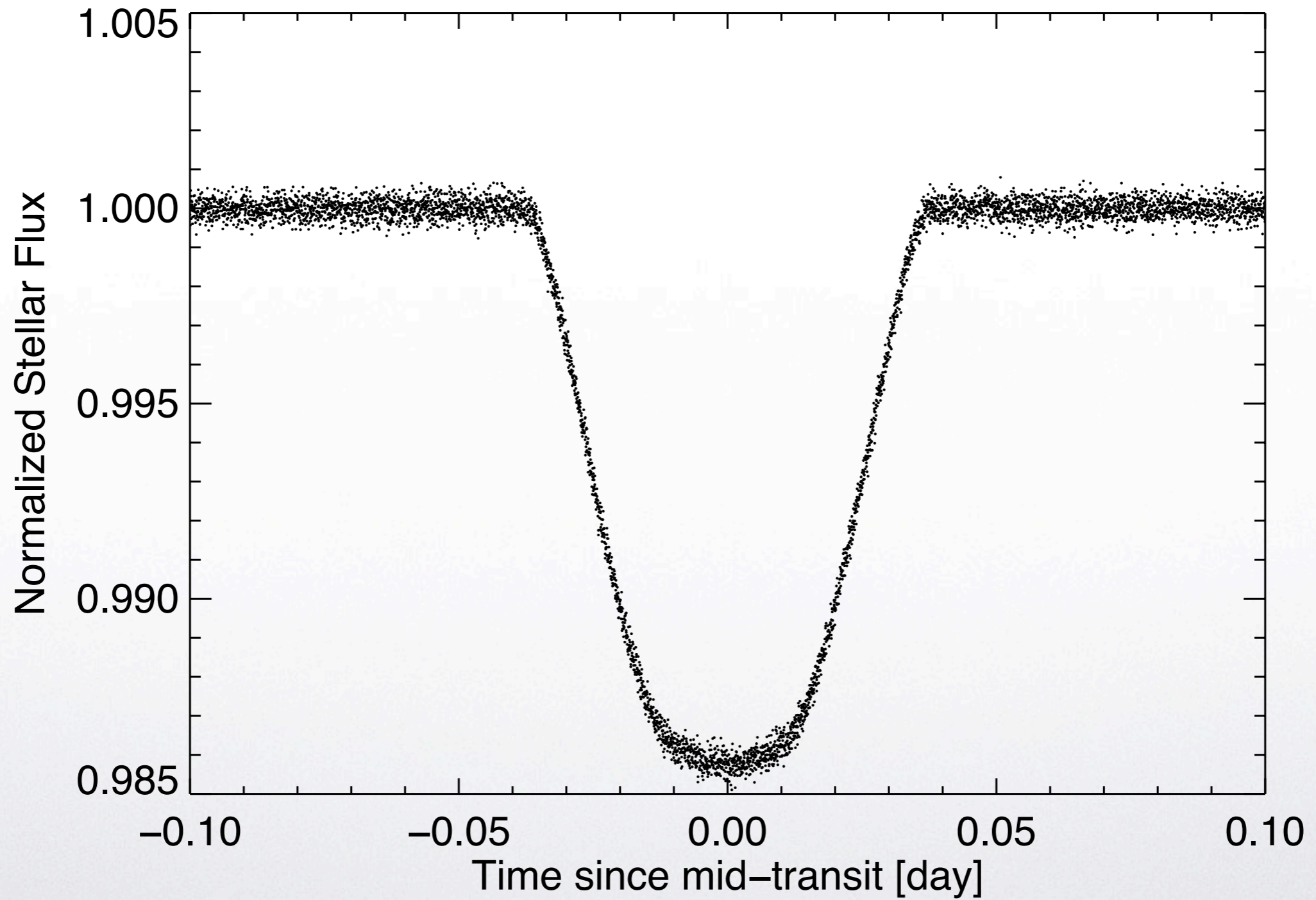




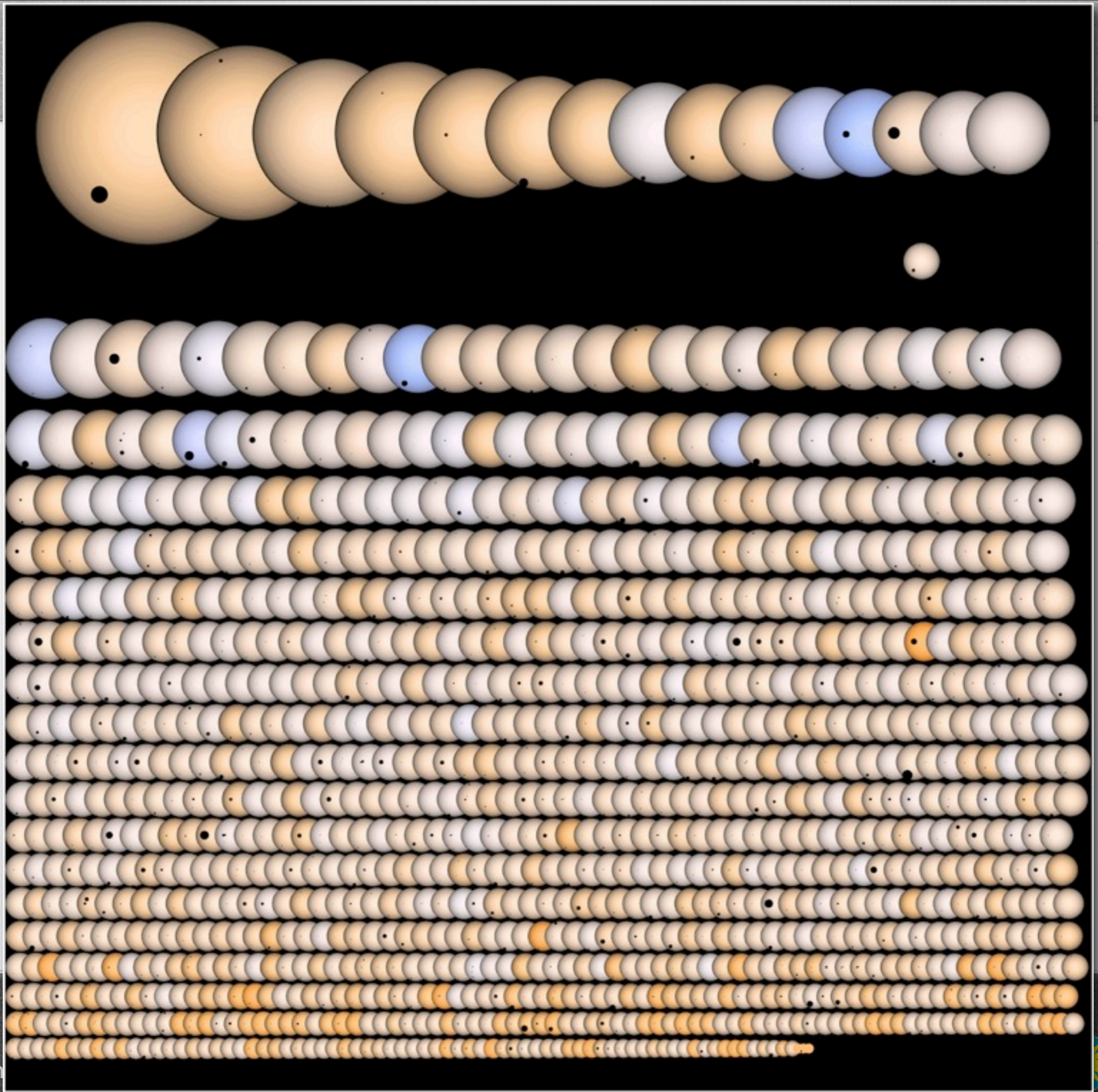
Winn (2008)



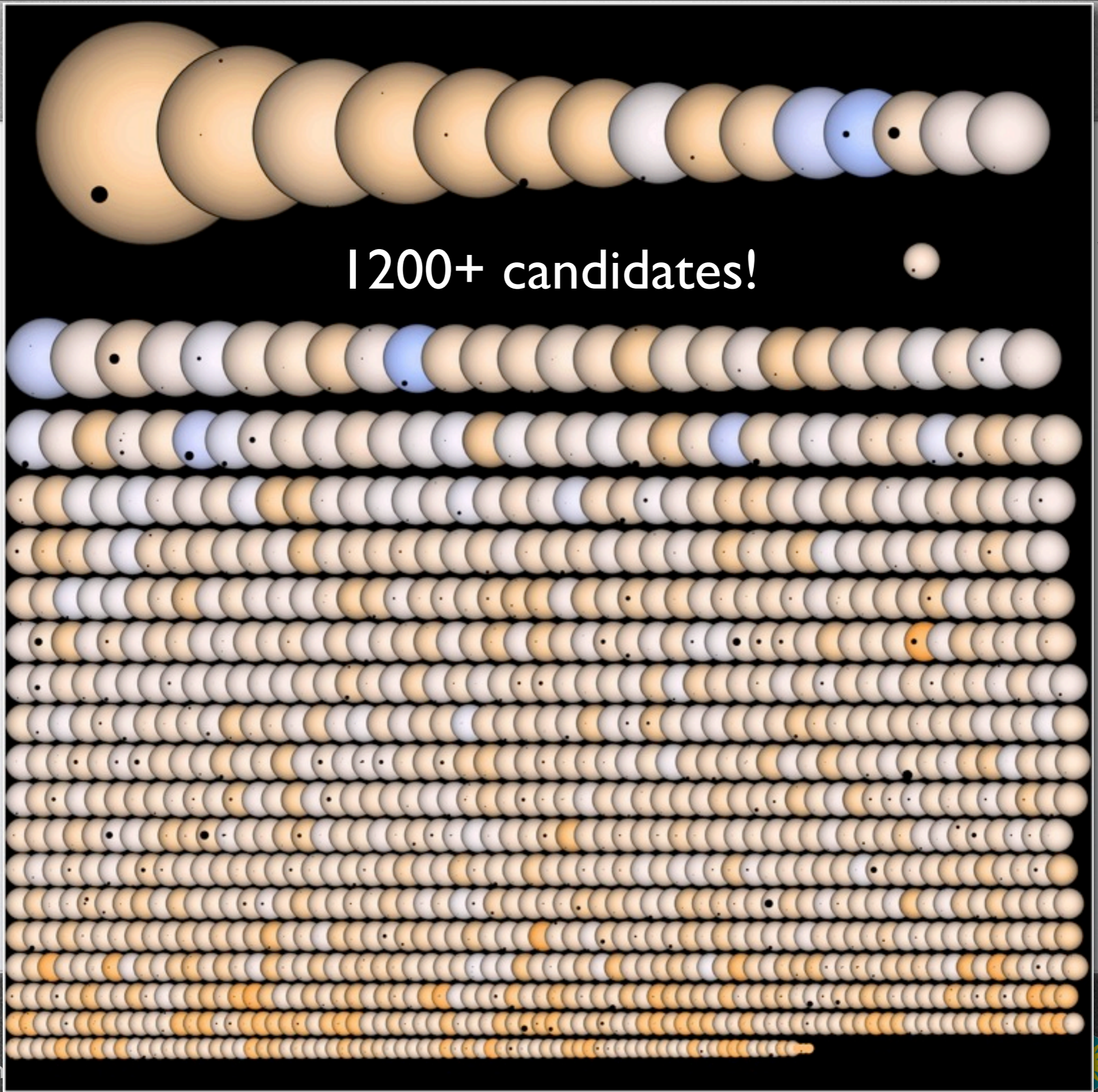
Kepler-1 = TrES-2



credit:
J. Rowe



credit:
J. Rowe



1200+ candidates!

Characteristics of planetary candidates observed by *Kepler*, II: Analysis of the first four months of data

William J. Borucki^{0,1}, David G. Koch¹, Gibor Basri², Natalie Batalha³, Timothy M. Brown⁵, Stephen T. Bryson¹, Douglas Caldwell⁶, Jørgen Christensen-Dalsgaard⁷, William D. Cochran⁸, Edna DeYore⁶, Edward W. Dunham⁹, Thomas N. Gautier III¹¹, John C. Greer¹⁰, Ronald

Kepler-9: A System of Multiple Planets Transiting a Sun-Like Star, Confirmed by Timing Variations

Matthew J. Holman,^{1*} Daniel C. Fabrycky,¹ Darin Ragozzine,¹ Eric B. Ford,² Jason H. Steffen,³ William F. Welsh,⁴ Jack J. Lissauer,^{5,6} David W. Latham,¹ Geoffrey W. Marcy,⁷ Lucianne M. Walkowicz,⁷ Natalie M. Batalha,⁸ Jon M. Jenkins,^{5,9} Jason F. Rowe,⁵

KEPLER'S FIRST ROCKY PLANET: KEPLER-10b*

NATALIE M. BATALHA¹, WILLIAM J. BORUCKI², STEPHEN T. BRYSON², LARS A. BUCHHAVE³, DOUGLAS A. CALDWELL⁴, JØRGEN CHRISTENSEN-DALSGAARD^{5,6}, DAVID CIARDI⁷, EDWARD W. DUNHAM⁸, FRANCOIS FRESSIN³, THOMAS N. GAUTIER III⁹, RONALD L. GILLILAND¹⁰, MICHAEL R. HAAS², STEVE B. HOWELL¹¹, JON M. JENKINS⁴, HANS KJELDSSEN⁵, DAVID G. KOCH², EDNA DEYORE⁶, JASON F. ROWE⁵, GEORGE W. MARCY¹², JASON H. STEFFEN³, DANIEL C. FABRYCKY¹, WILLIAM F. WELSH⁴

A Closely-Packed System of Low-Mass, Low-Density Planets Transiting Kepler-11

Jack J. Lissauer¹, Daniel C. Fabrycky², Eric B. Ford³, William J. Borucki¹, Francois Fressin⁴, Geoffrey W. Marcy⁵, Jerome A. Orosz⁶, Jason F. Rowe⁷, Guillermo Torres⁴, William F. Welsh⁶, Natalie M. Batalha⁸, Stephen T. Bryson¹, Lars A. Buchhave⁹

Kepler Eclipsing Binary Stars. II. 2165 Eclipsing Binaries in the Second Data Release

Robert W. Slawson

SETI Institute, 189 Bernardo Ave., Mountain View, CA 94043

rslawson@seti.org

Andrej Prša

KEPLER OBSERVATIONS OF TRANSITING HOT COMPACT OBJECTS

JASON F. ROWE^{1,15}, WILLIAM J. BORUCKI¹, DAVID KOCH¹, STEVE B. HOWELL², GIBOR BASRI³, NATALIE BATALHA⁴, TIMOTHY M. BROWN⁵, DOUGLAS CALDWELL⁶, WILLIAM D. COCHRAN⁷, EDWARD DUNHAM⁸, ANDREA K. DUPREE⁹, JONATHAN J. FORTNEY¹⁰, THOMAS N. GAUTIER III¹¹, RONALD L. GILLILAND¹², JON JENKINS⁶, DAVID W. LATHAM⁹.

A THIRD HOT WHITE DWARF COMPANION DETECTED BY *KEPLER*

JOSHUA A. CARTER^{1,2,3}, SAUL RAPPAPORT¹, & DANIEL FABRYCKY^{2,3,4}

Accepted for publication in The Astrophysical Journal

KOI-54: THE *KEPLER* DISCOVERY OF TIDALLY-EXCITED PULSATIONS AND BRIGHTENINGS IN A HIGHLY ECCENTRIC BINARY

WILLIAM F. WELSH¹, JEROME A. OROSZ¹, CONNY AERTS², TIMOTHY BROWN^{3,17}, ERIK BRUGAMYER⁴, WILLIAM COCHRAN⁴, RONALD L. GILLILAND⁵, JOYCE ANN GUZIK⁶, DONALD W. KURTZ⁷, DAVID LATHAM⁸, GEOFF MARCY⁹, SAMUEL N. QUINN⁸, WOLFGANG ZIMA², CHRISTOPHER ALLEN¹⁶, NATALIE BATALHA^{10,11}, STEVE BRYSON¹¹, LARS BUCHHAVE⁸, DOUGLAS A. CALDWELL^{11,12}, THOMAS N. GAUTIER¹³, STEVEN HOWELL¹⁴, K. KINEMUCHI^{11,15}, KHADEEJAH A. IBRAHIM¹⁶.

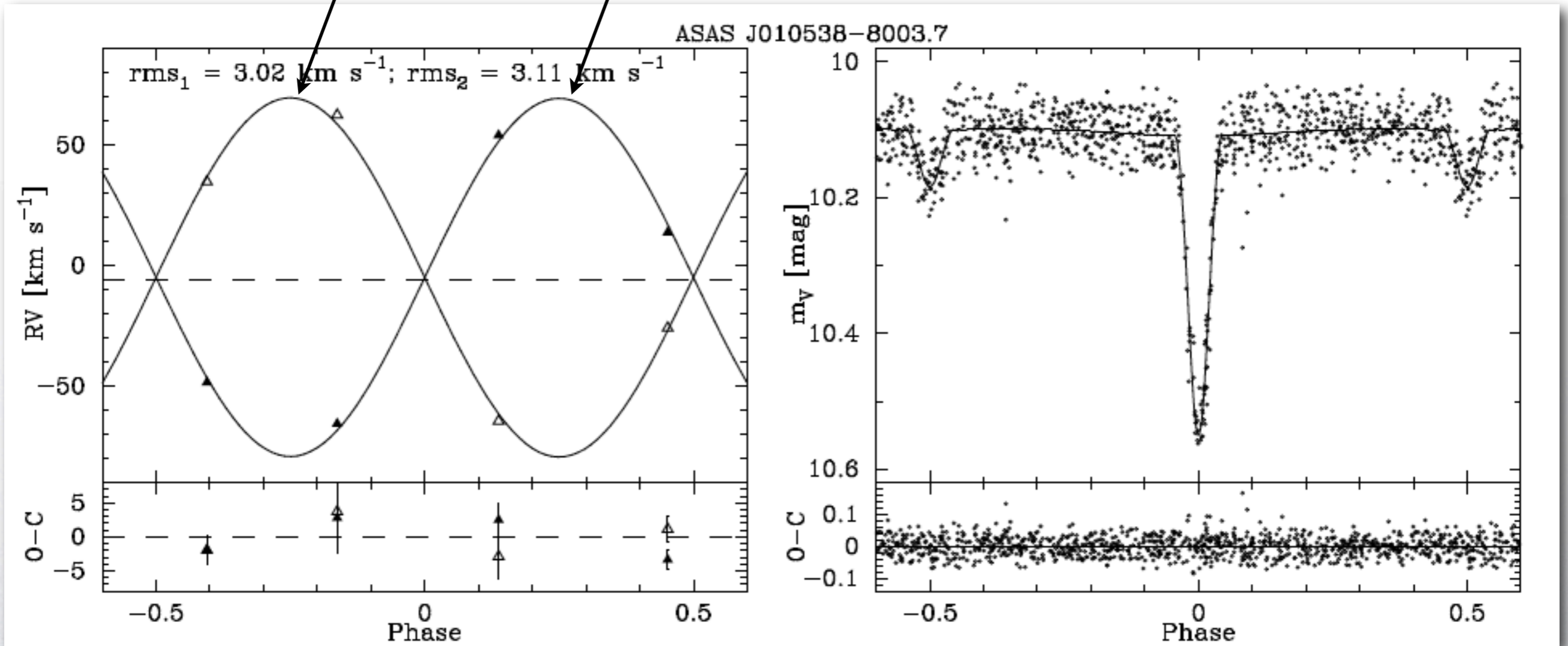
KOI-126: A Triply Eclipsing Hierarchical Triple with Two Low-Mass Stars

Joshua A. Carter,^{1*} Daniel C. Fabrycky,² Darin Ragozzine,¹ Matthew J. Holman,¹ Samuel N. Quinn,¹ David W. Latham,¹ Lars A. Buchhave,^{1,3} Jeffrey Van Cleve,^{4,7} William D. Cochran,⁵ Miles T. Cote,⁴



Reflex of **A** due to **B**

Reflex of **B** due to **A**



Hełminiak, Konacki, Ratajczak, Muterspaugh (2009)

Observables

From the
light curve:

$$\begin{aligned} & * \frac{M_A}{R_A^3} (1 + q) \\ & \frac{M_B}{R_B^3} (1 + q^{-1}) \\ & \sin i \end{aligned}$$

From the RV:

$$\begin{aligned} f(M_A, M_B) &= \frac{M_A \sin^3 i}{(1 + q^{-1})^2} \\ f(M_B, M_A) &= \frac{M_B \sin^3 i}{(1 + q)^2} \end{aligned}$$

* Seager, Mallén-Ornelas (2003)

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↓
Mass ratio, q

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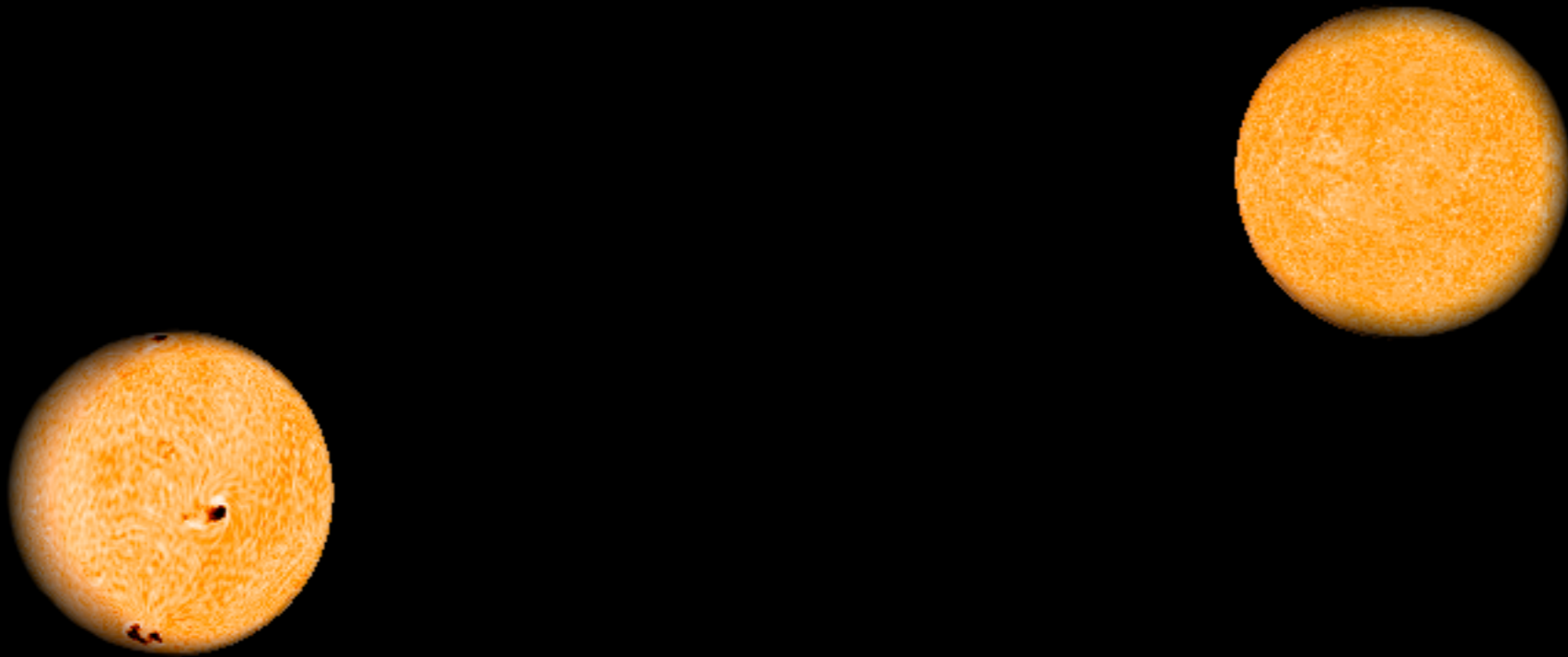
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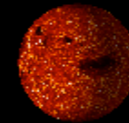
Mass ratio, q

Masses and Radii

* Seager, Mallén-Ornelas (2003)







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$$\frac{M_B}{R_B^3} (1 + q^{-1})$$

$$\sin i$$

From the RV:

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$$f(M_B, M_A) = \frac{M_B \sin^3 i}{(1 + q)^2}$$

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Masses and Radii!

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~~Mass ratio, q~~

~~Masses and Radii!~~



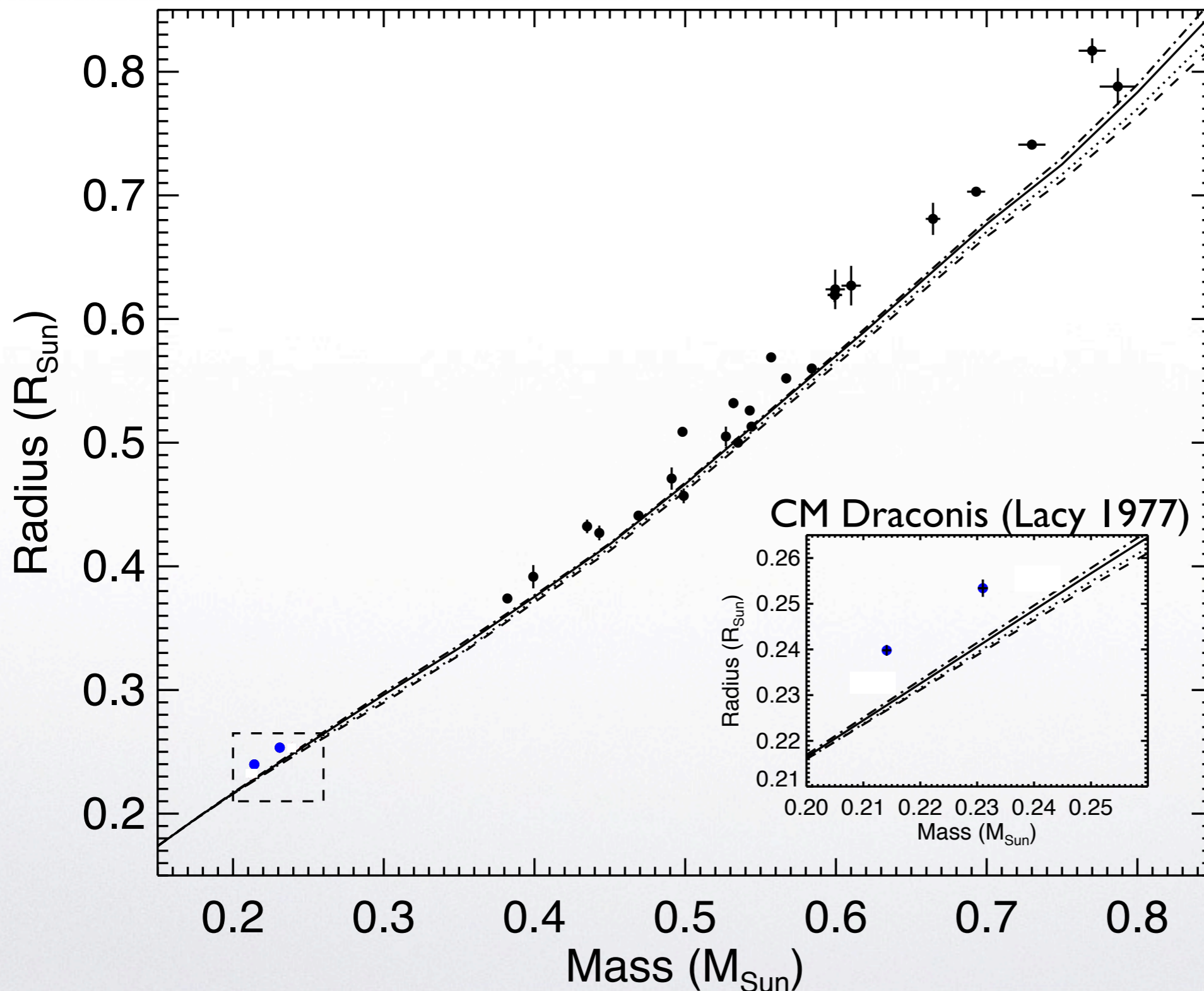
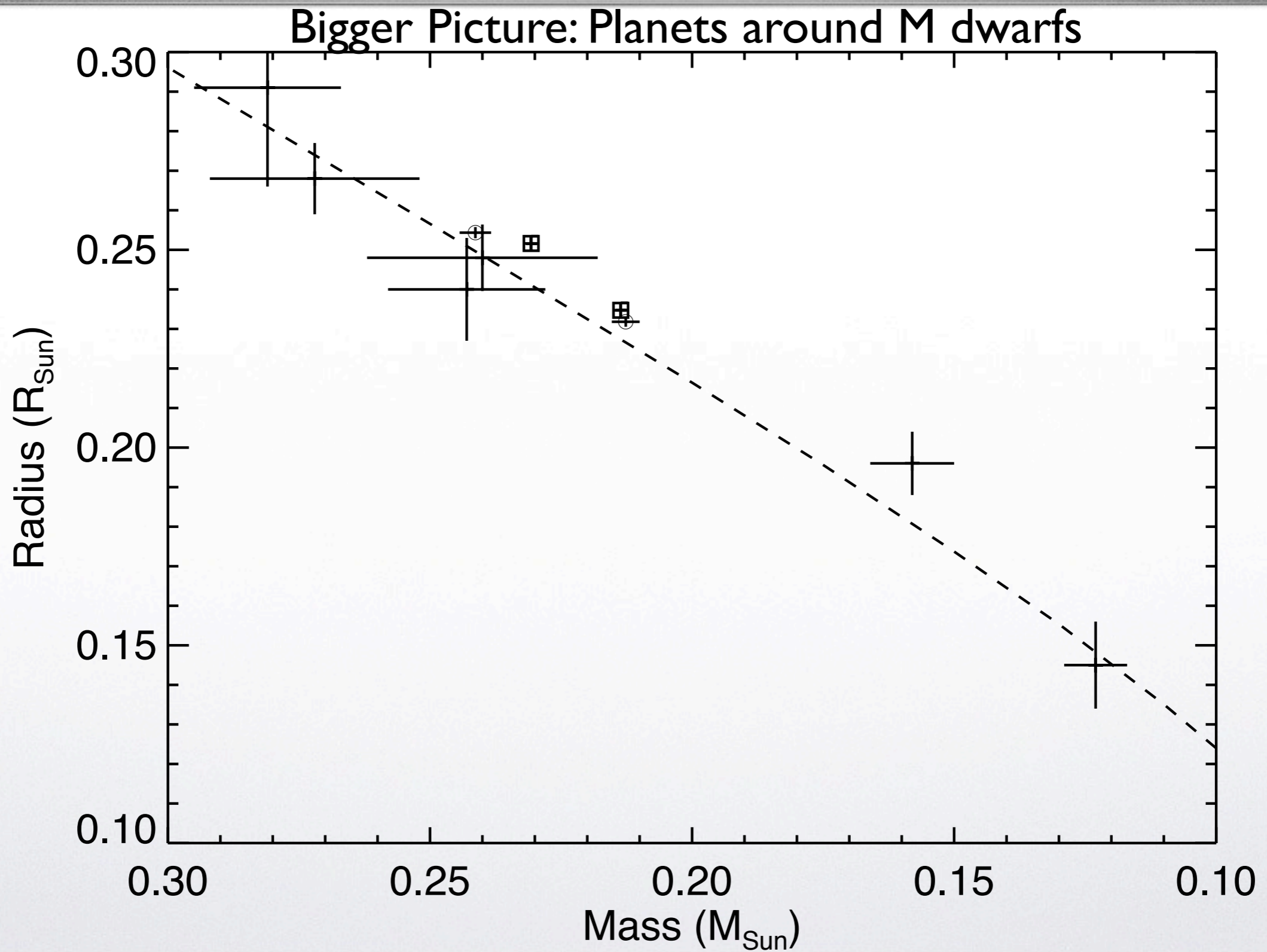
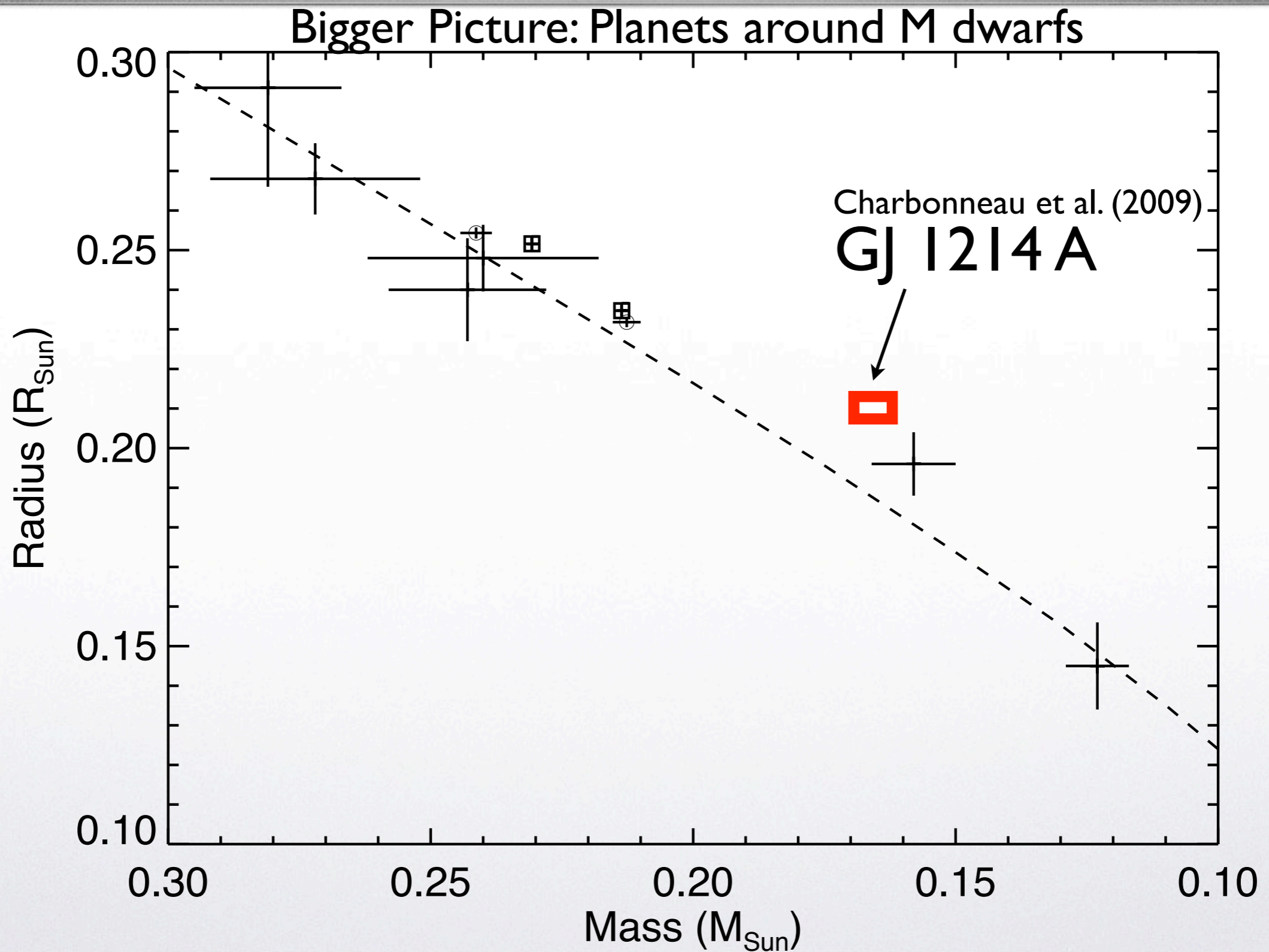
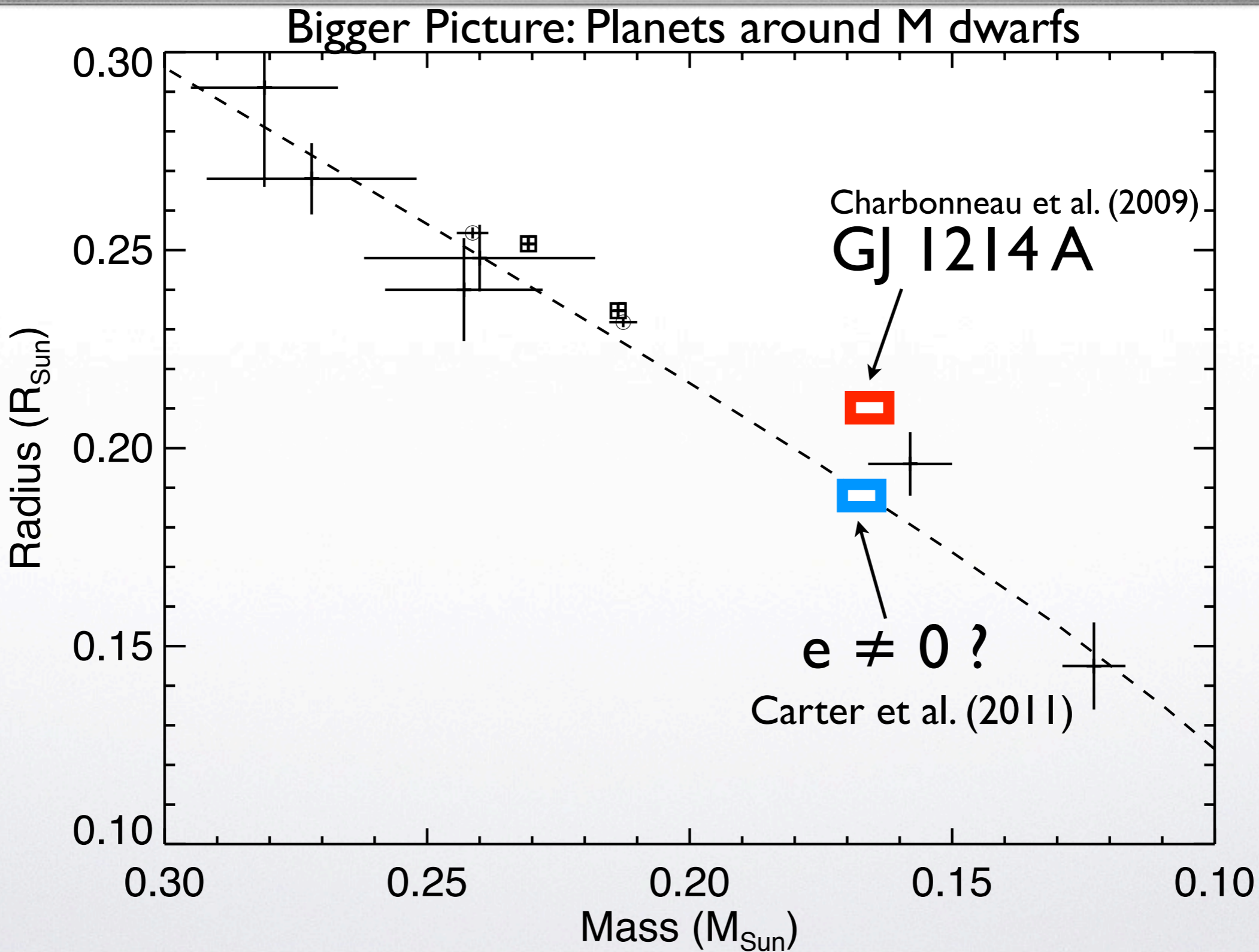
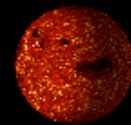


Figure modified from
Carter et al. (2011)
Data from Kraus et al. (2011),
Cakirli, Ibanoglu, Dervisoglu (2010)

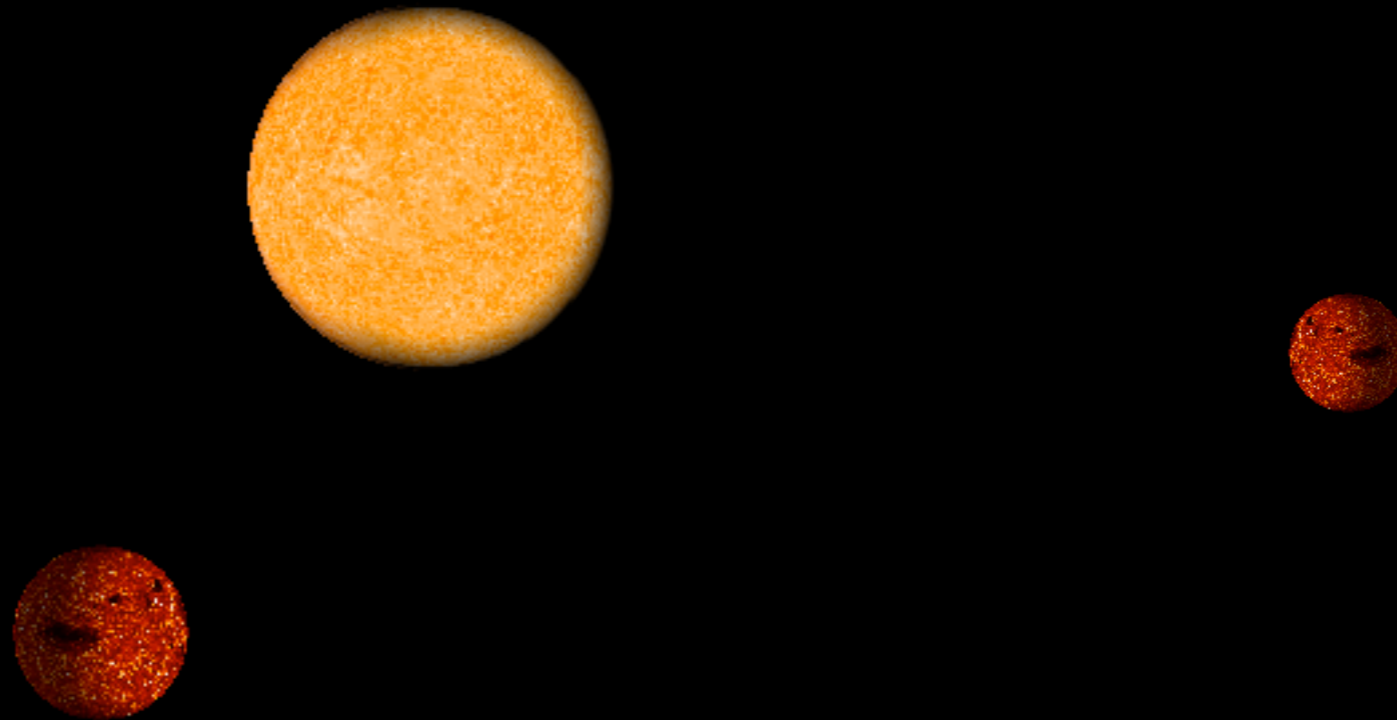


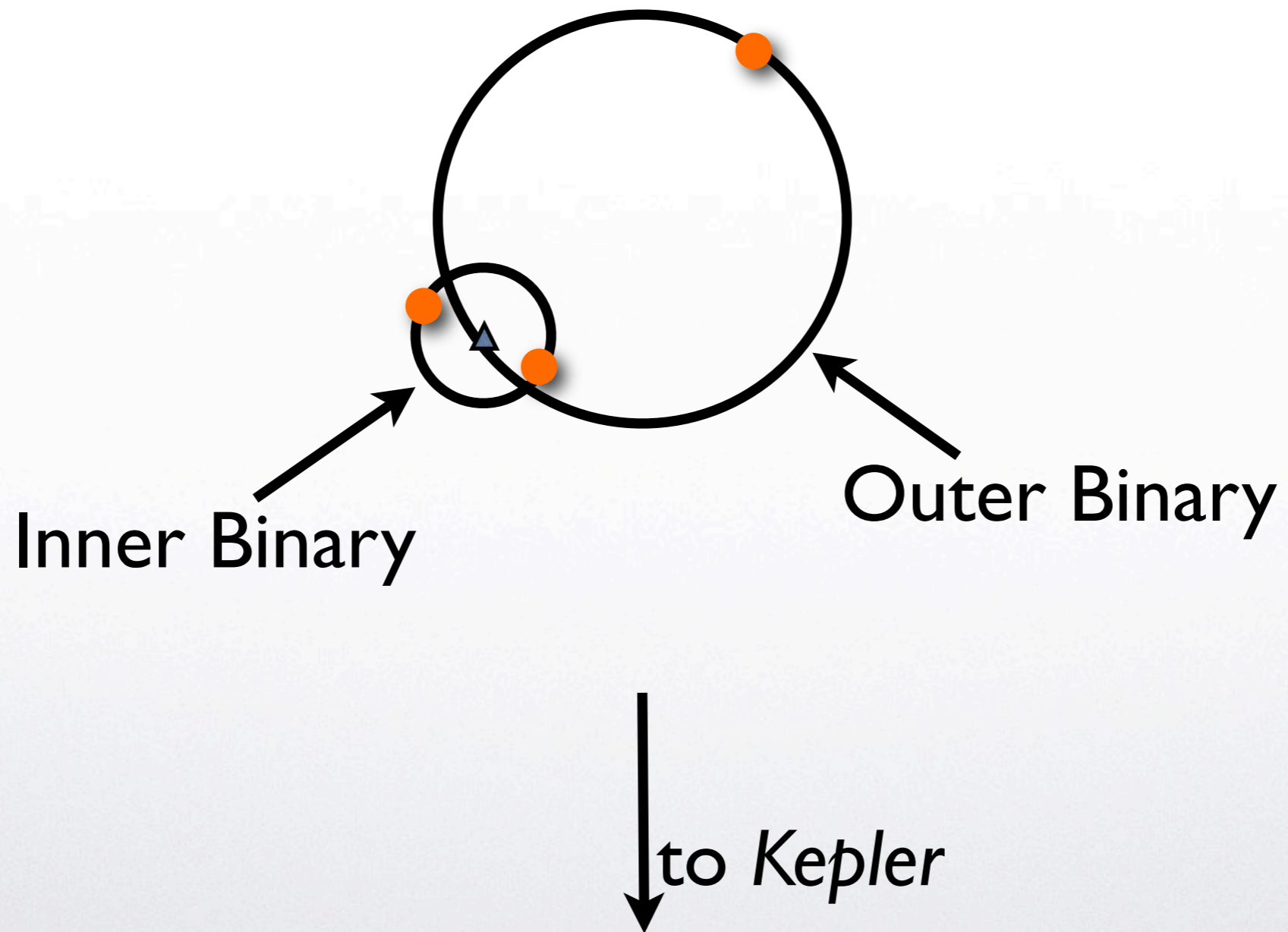




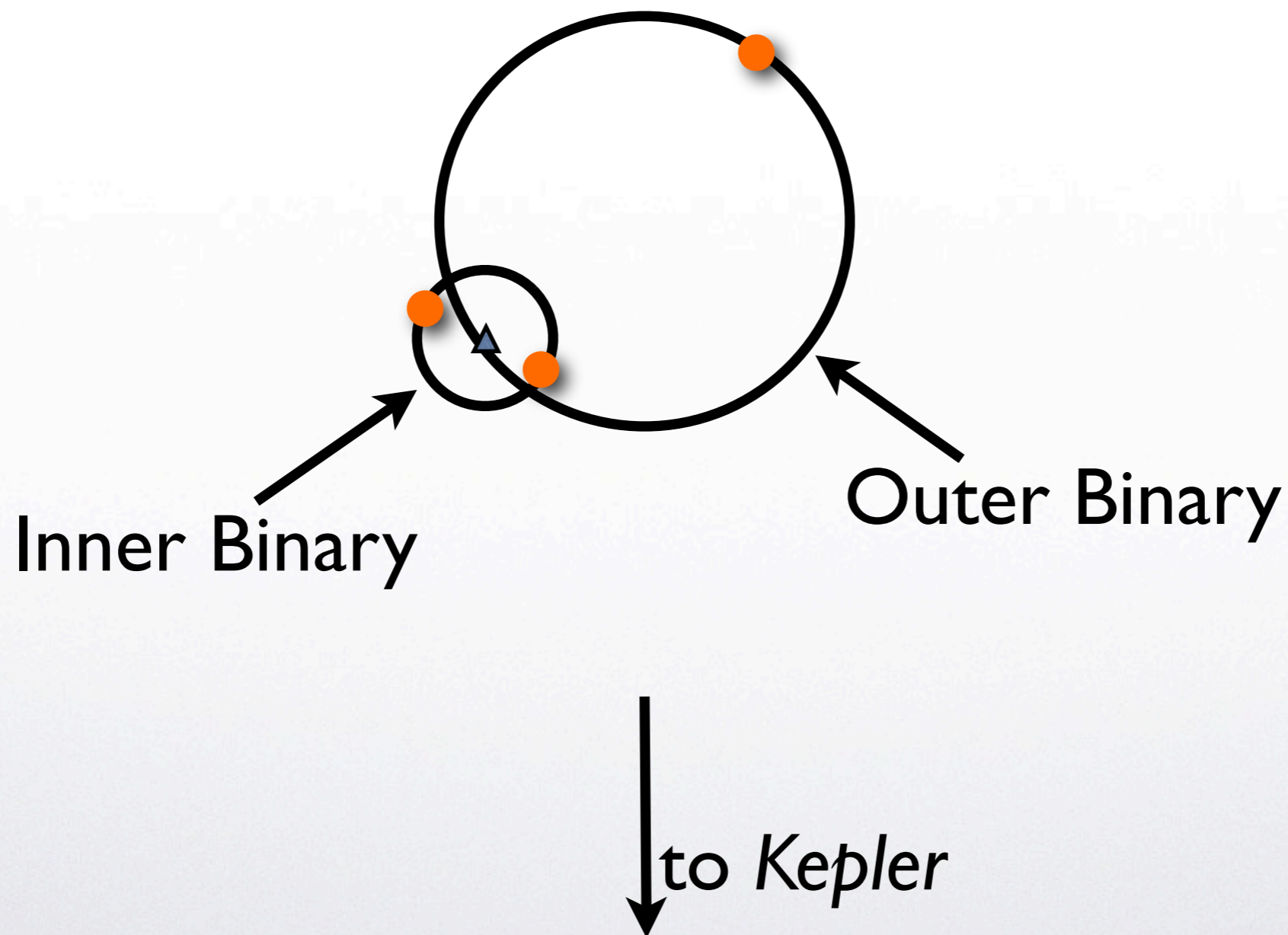


Multi-Eclipsing Hierarchical Triples



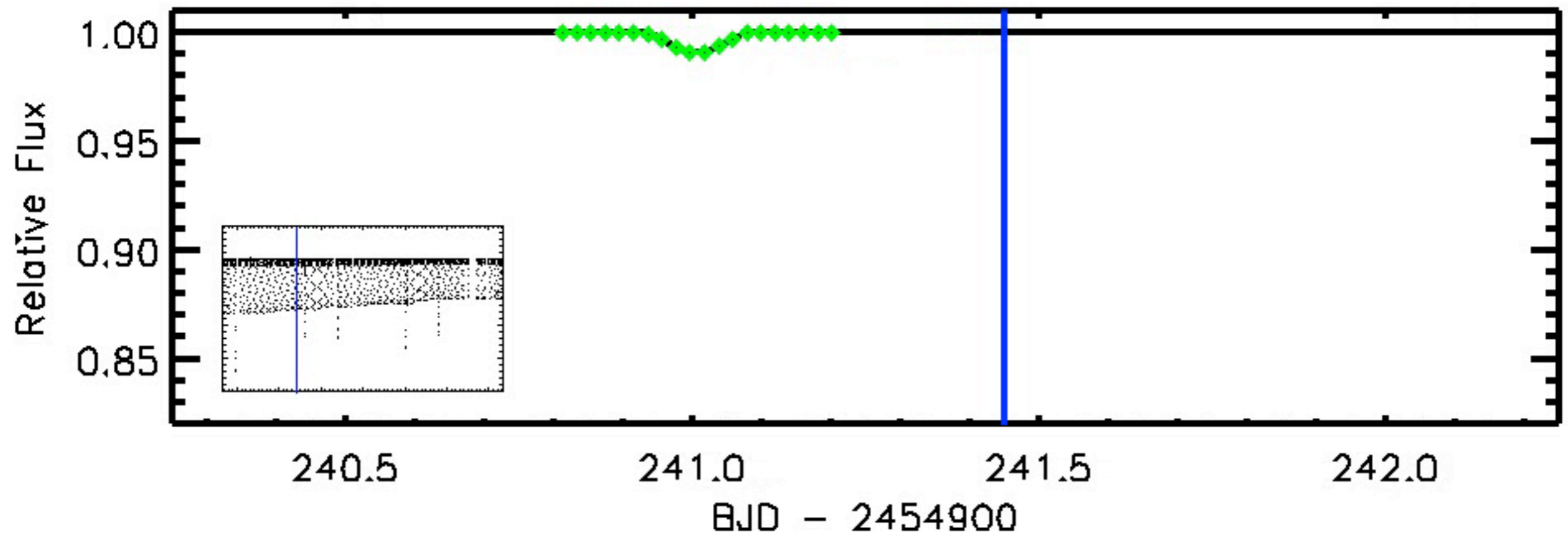
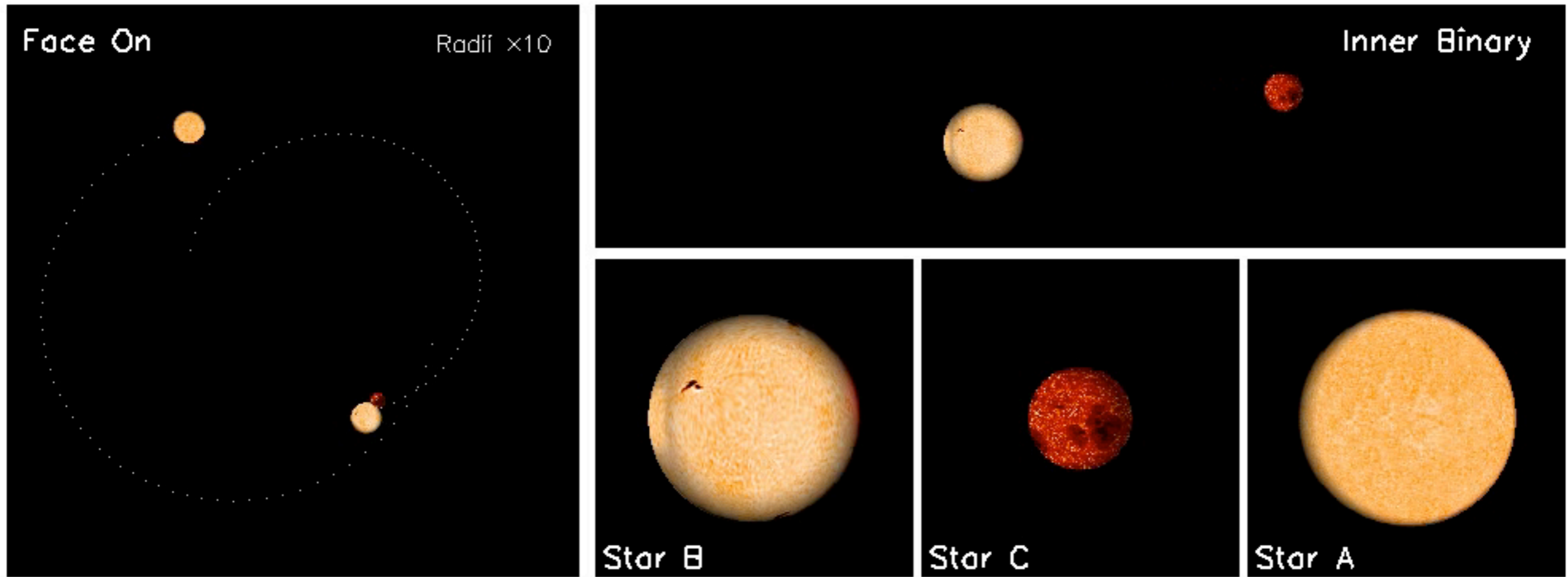


Multi-Eclipsing Hierarchical Triples





KIC-7289157

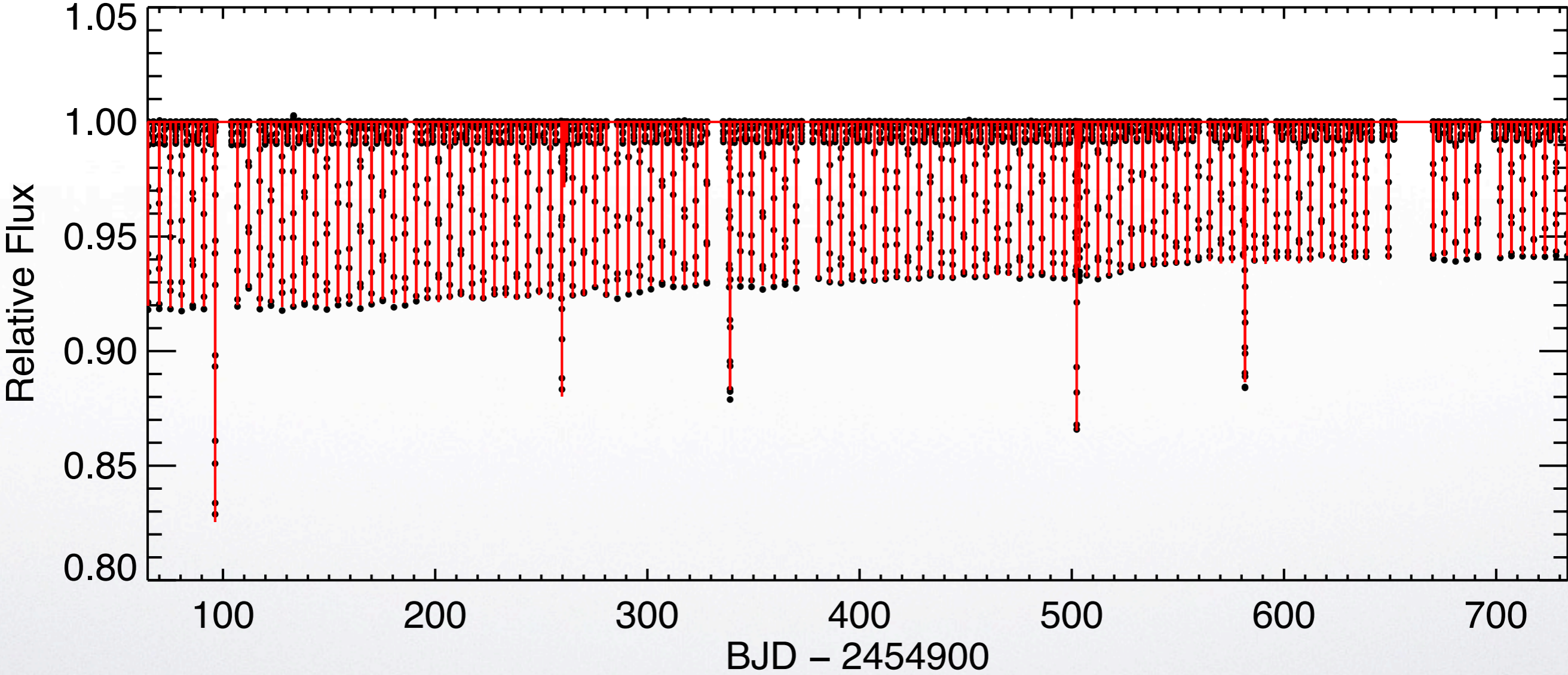


- The dynamical interaction between the stars is encoded in a variable light curve morphology:
 - Non-linear conjunction times
 - Variable impact parameters (between eclipses and during eclipse)
 - Accelerations transverse to the line-of-sight (between eclipses and during eclipse)

Eclipsing Hierarchical Triples

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In the works... KIC 7289157



- Dynamical:

- ➡ Newton’s Equations + Post-Newtonian acceleration in close, “inner” binary

- ➡ Optional, additional perturbing accelerations in inner binary:

- ➡ Non-dissipative equilibrium tide (“prolate distortion”, k_2)

- ➡ Rotationally-induced oblate distortion (k_2 , spin frequency)

- ➡ Tidal damping (Q); negligible on observation timescales

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- Photometric: Geometrical 3-body eclipse model

Observables

From the
light curve:

$$\frac{M_A}{R_A^3}$$

$$\frac{M_B}{R_B^3}$$

$$\frac{M_C}{R_C^3}$$

$$\frac{M_B}{M_A}, \frac{M_C}{M_A}, \frac{M_B}{M_C}$$

From the RV (of A):

$$f(M_A, M_B + M_C) = \frac{(M_B + M_C) \sin^3 i}{(1 + q_{A,B+C}^{-1})^2}$$

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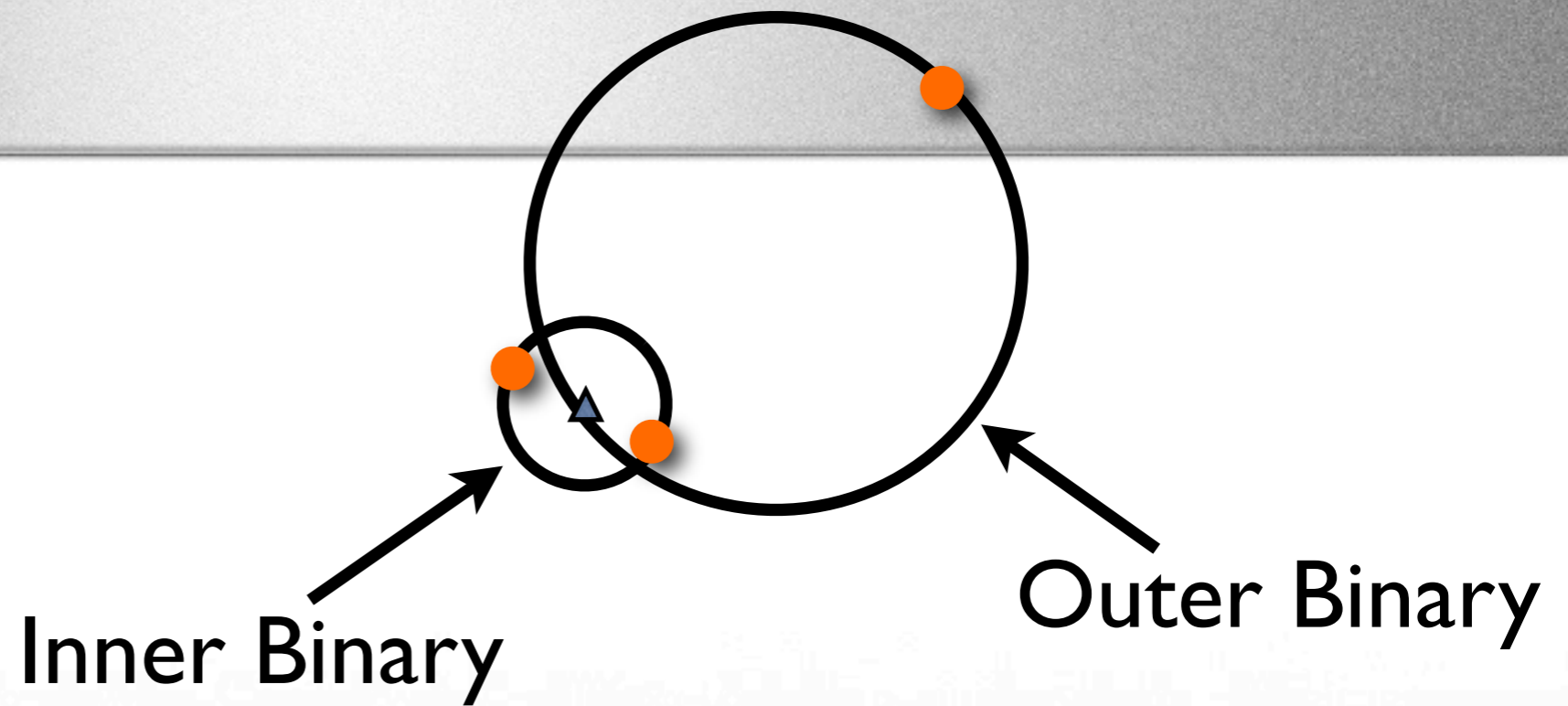
$$\frac{M_C}{R_C^3}$$

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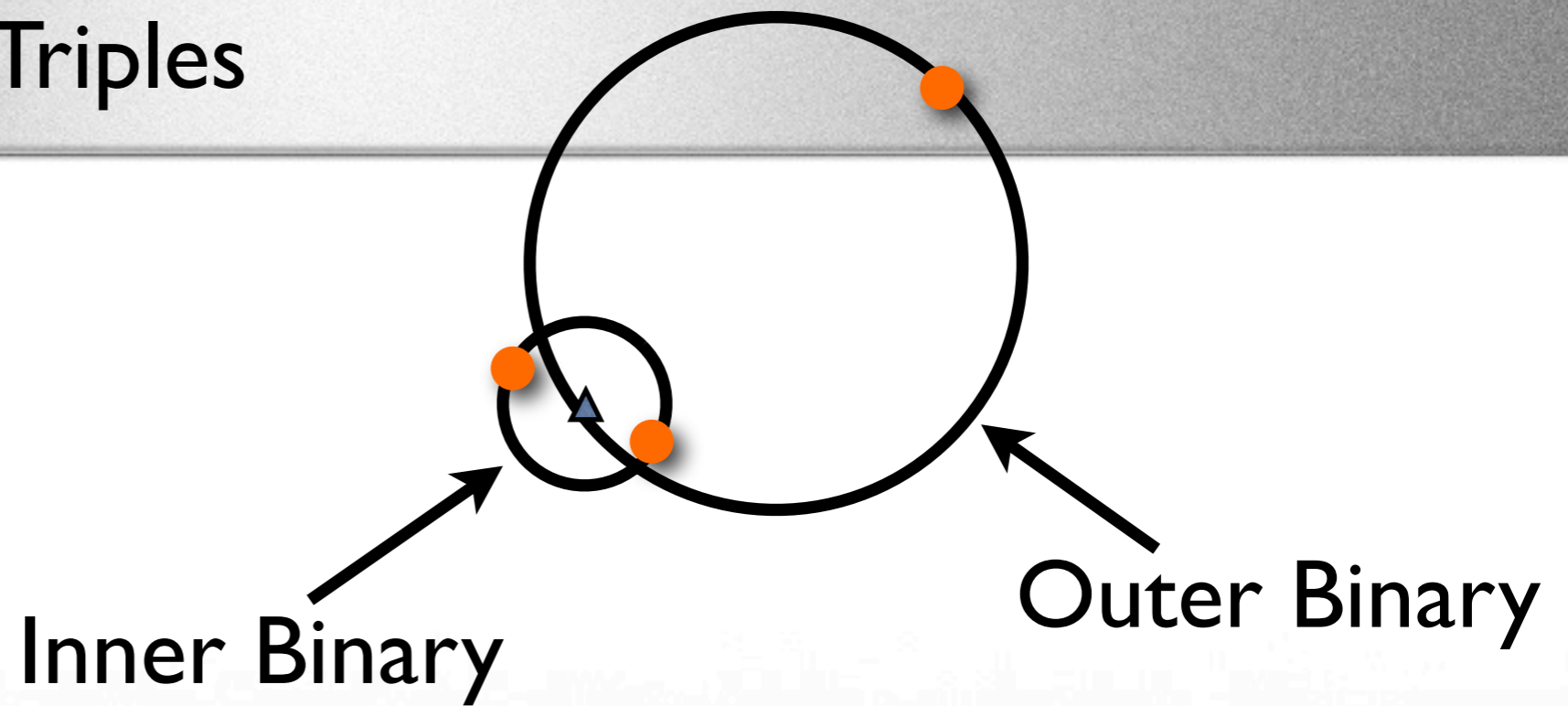
$$f(M_A, M_B + M_C) = \frac{(M_B + M_C) \sin^3 i}{(1 + q_{A,B+C}^{-1})^2}$$

Masses and Radii!



- Timescale for secular (orbit averaged) variations in the orbital elements depends on the period ratio squared, mass ratios; need to be short enough to see some action in a human lifetime:
- Short periods (< 1 yr), small period ratios (20:1 or better)

Eclipsing Hierarchical Triples



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- *Kepler* is observationally biased towards detecting multi-eclipsing dynamical triples: and we* find them!

3. Interesting Objects in the Catalog

3.1. Tertiary Eclipses

The search for circumbinary planets in the *Kepler* data includes looking for transits with multiple components (e.g. Deeg et al. 1998; Doyle et al. 2000). Transit patterns with multiple components are caused by a slowly moving planet crossing in front of the eclipsing binary; it is alternately silhouetted by the motion of the background binary stars as they orbit about each other. Circumbinary transits can thus produce predictable but non-periodic features of various

Slawson et al. (2011)

*Thanks to the hard work of Jerry Orosz, Laurance Doyle, Bill Welsh and the rest of Kepler EB team...

Eclipsing Hierarchical Triples

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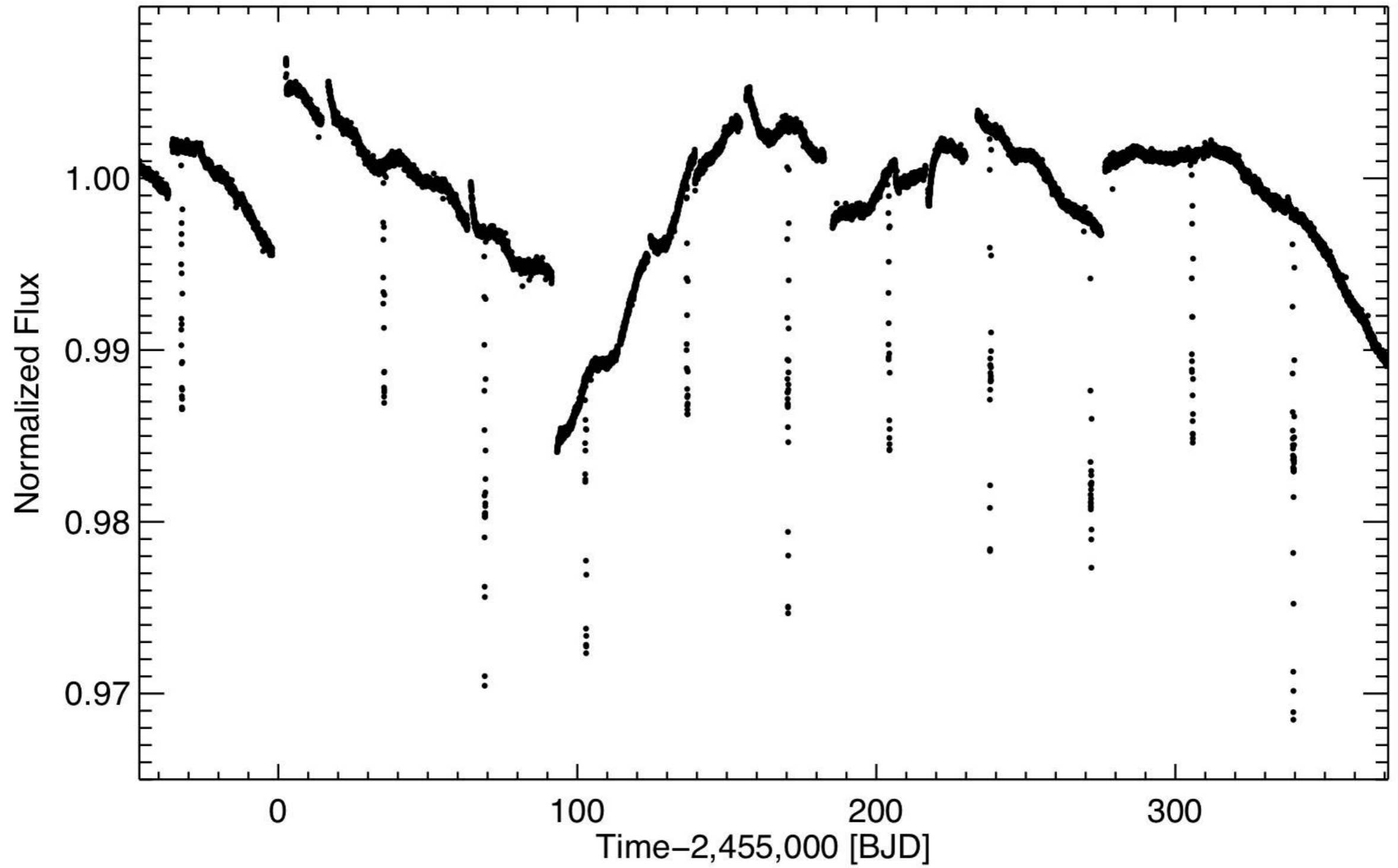
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KOI-126: A Triply Eclipsing Hierarchical Triple with Two Low-Mass Stars

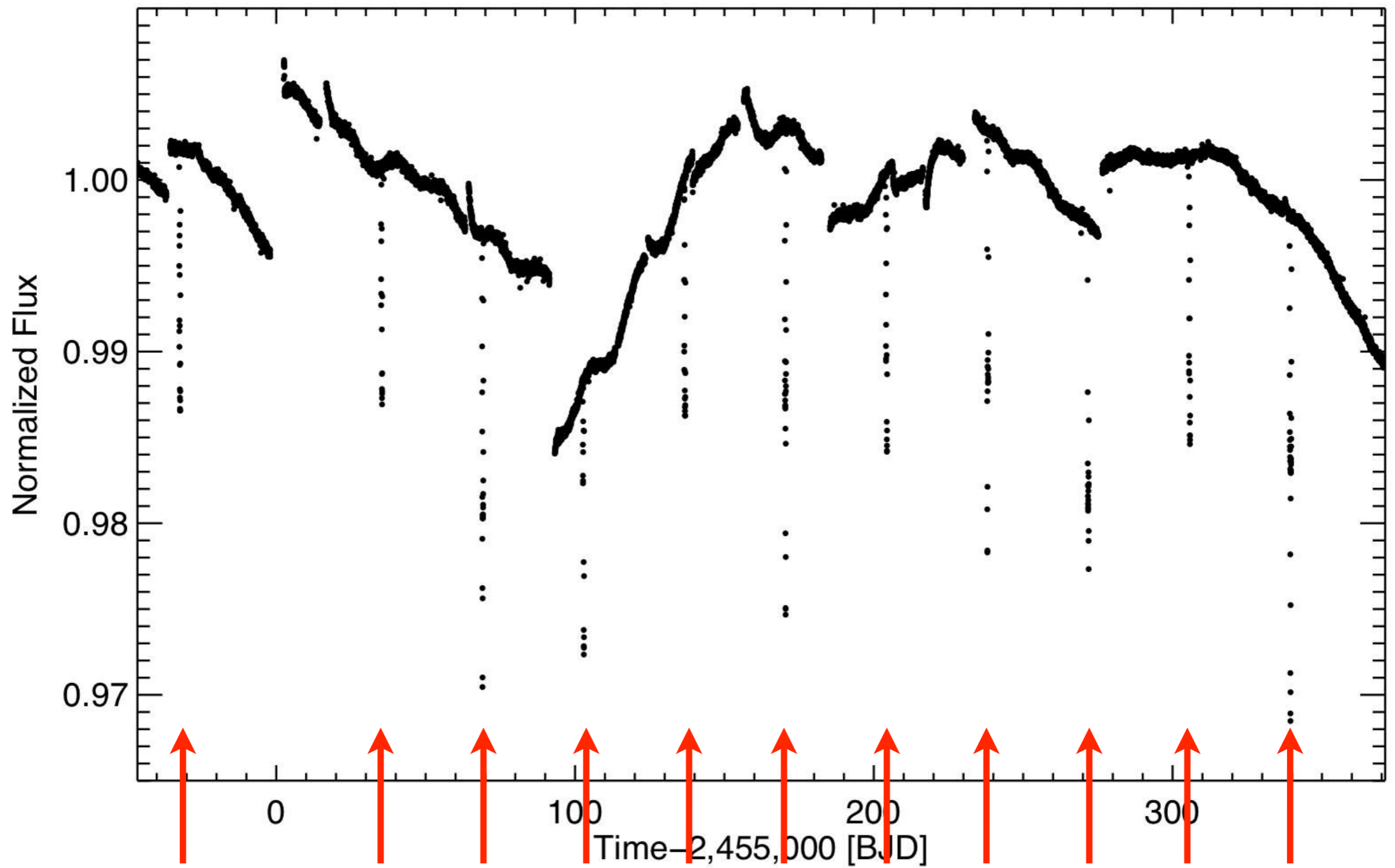
Joshua A. Carter,^{1*} Daniel C. Fabrycky,² Darin Ragozzine,¹ Matthew J. Holman,¹ Samuel N. Quinn,¹ David W. Latham,¹ Lars A. Buchhave,^{1,3} Jeffrey Van Cleve,^{4,7} William D. Cochran,⁵ Miles T. Cote,⁴

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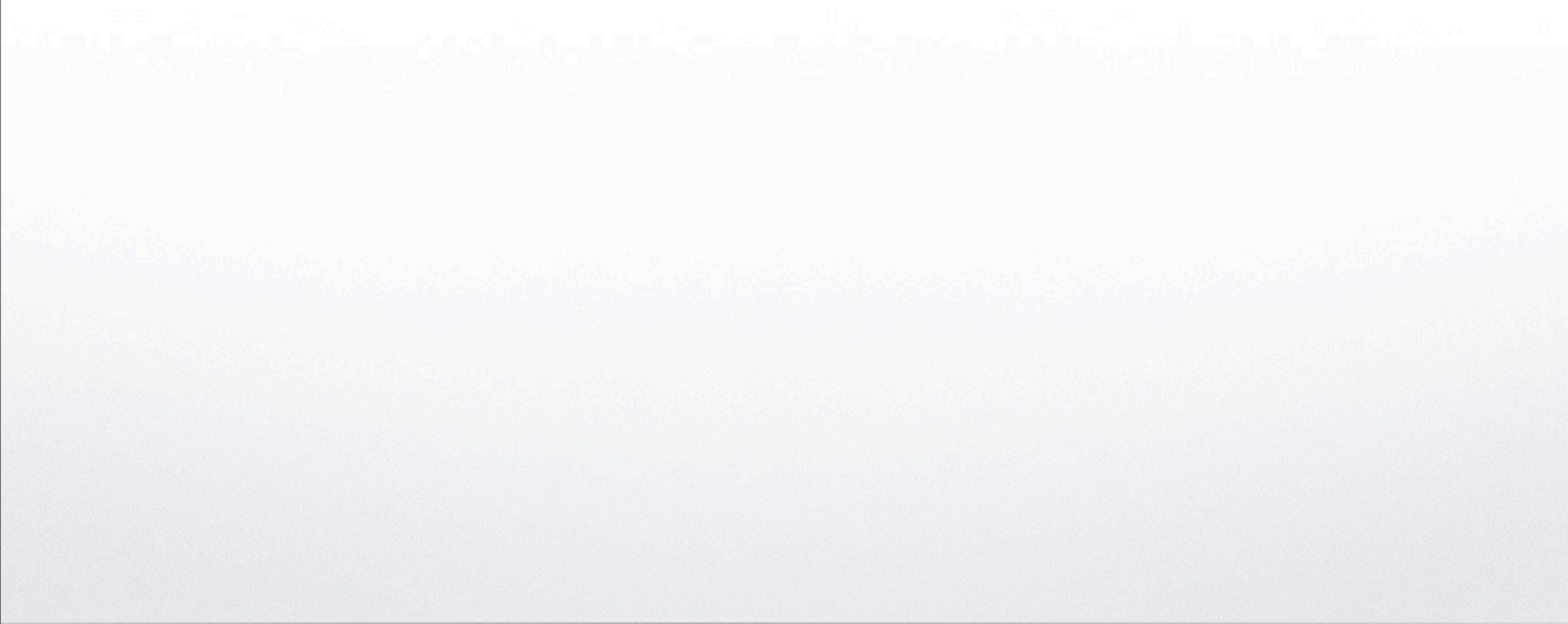
KOI-126



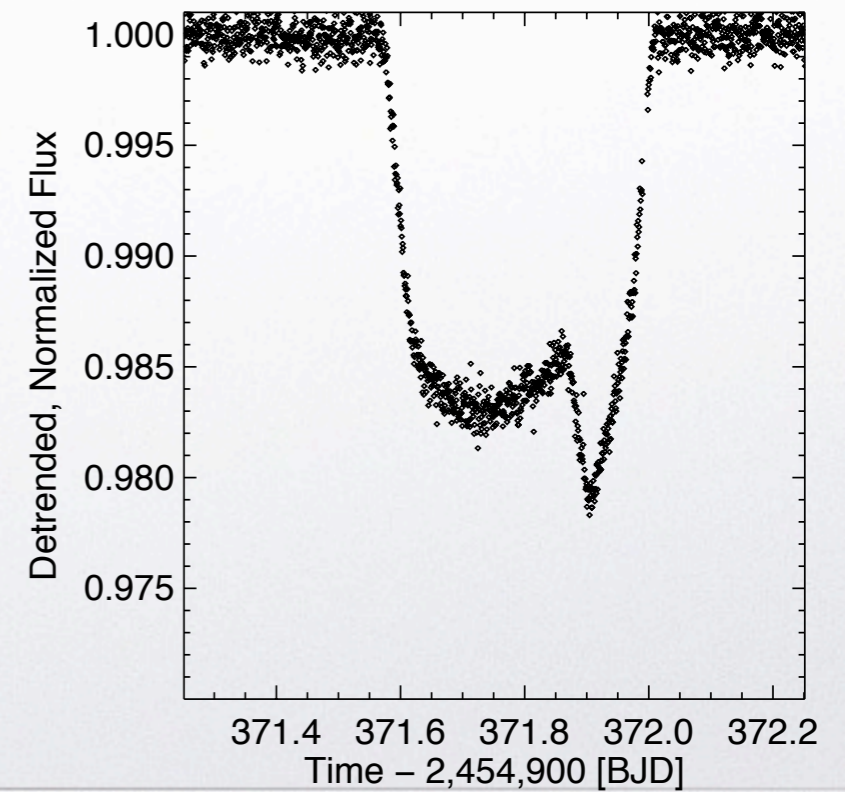
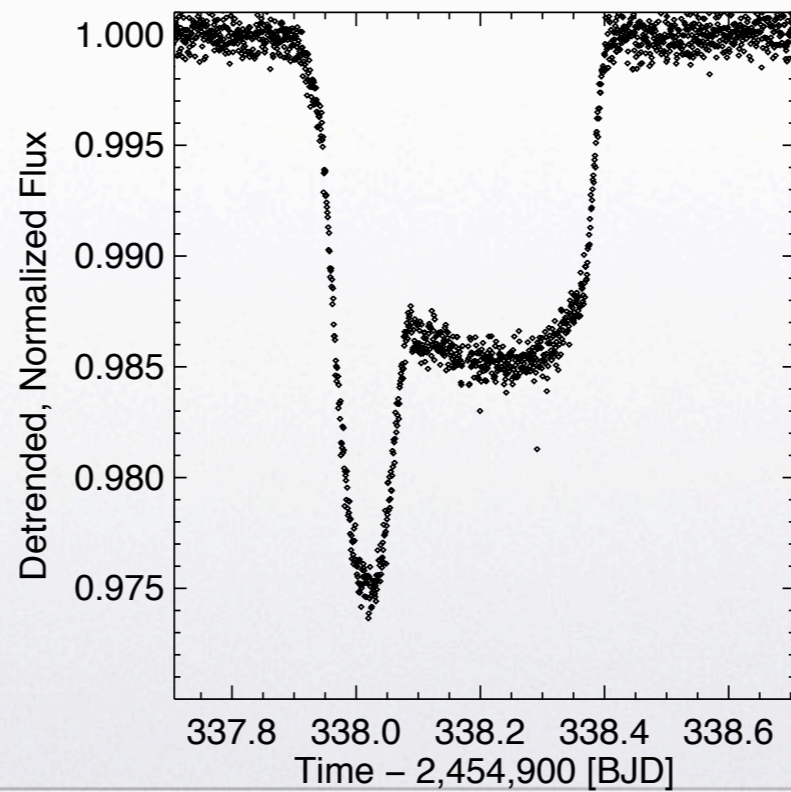
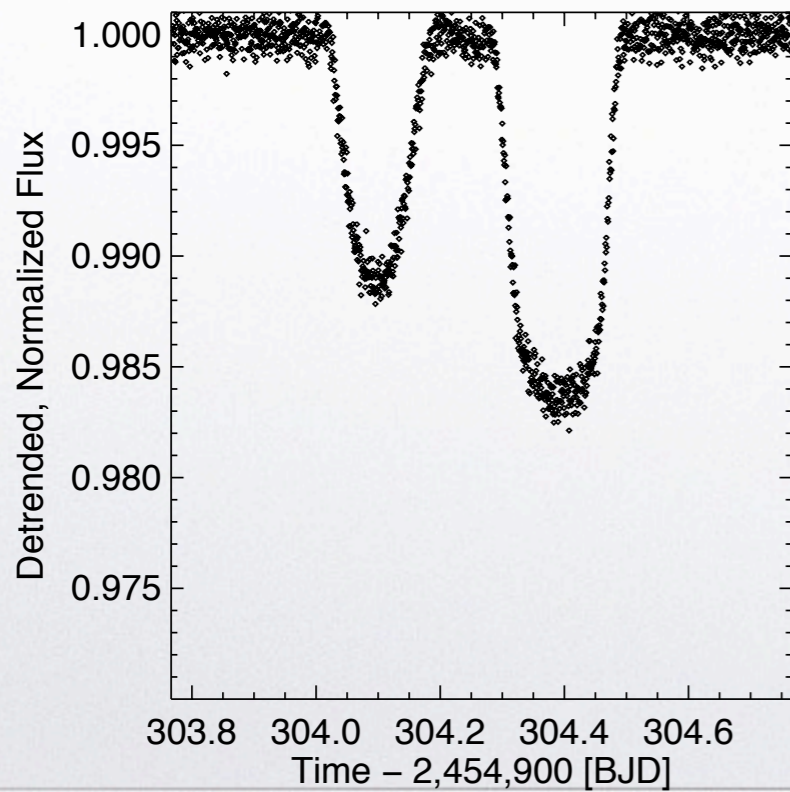
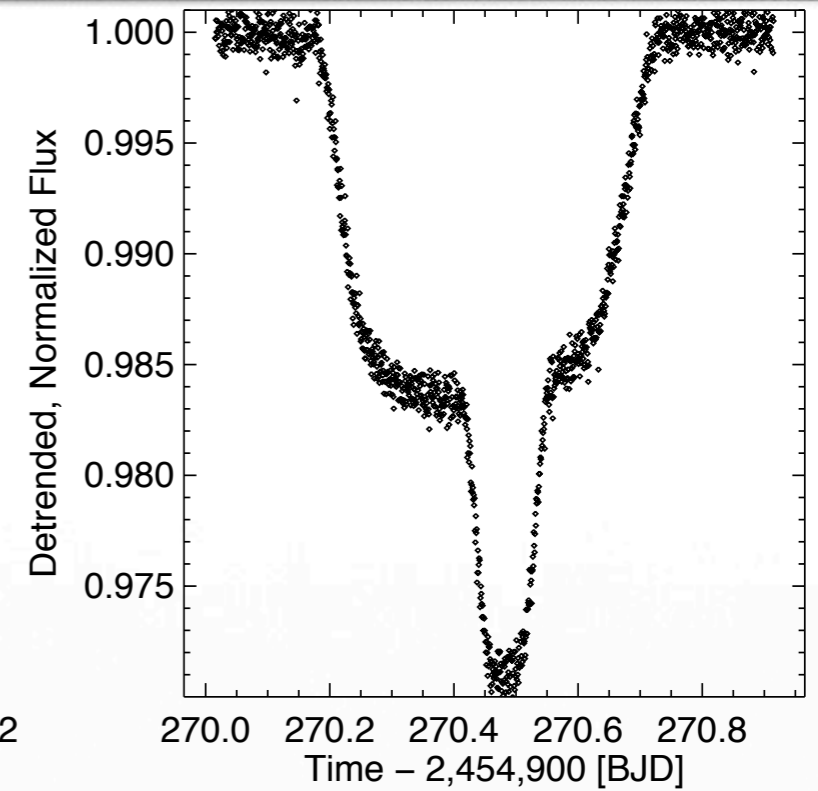
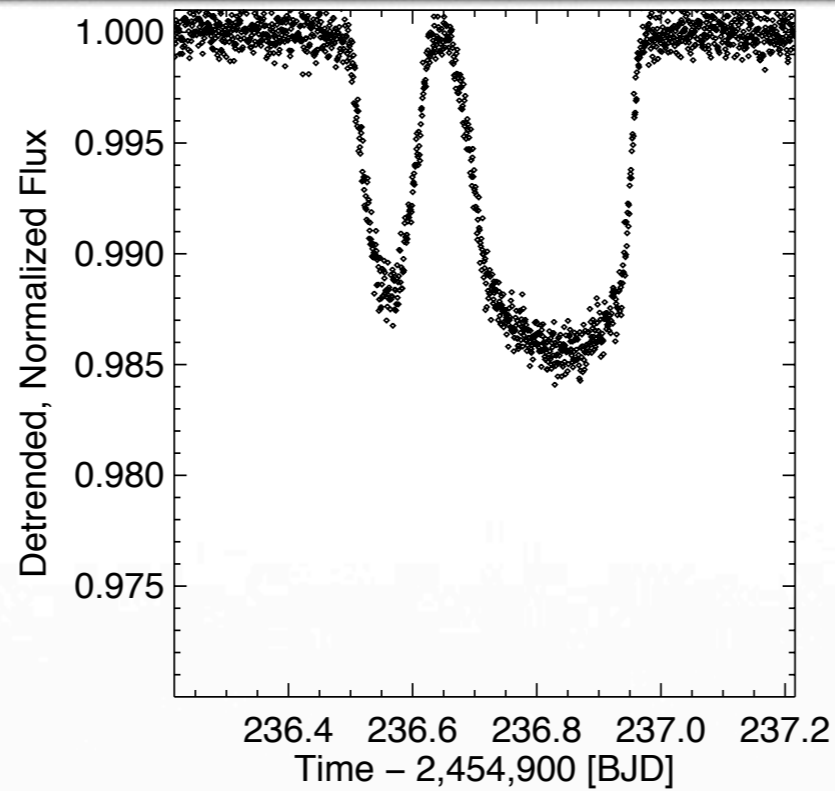
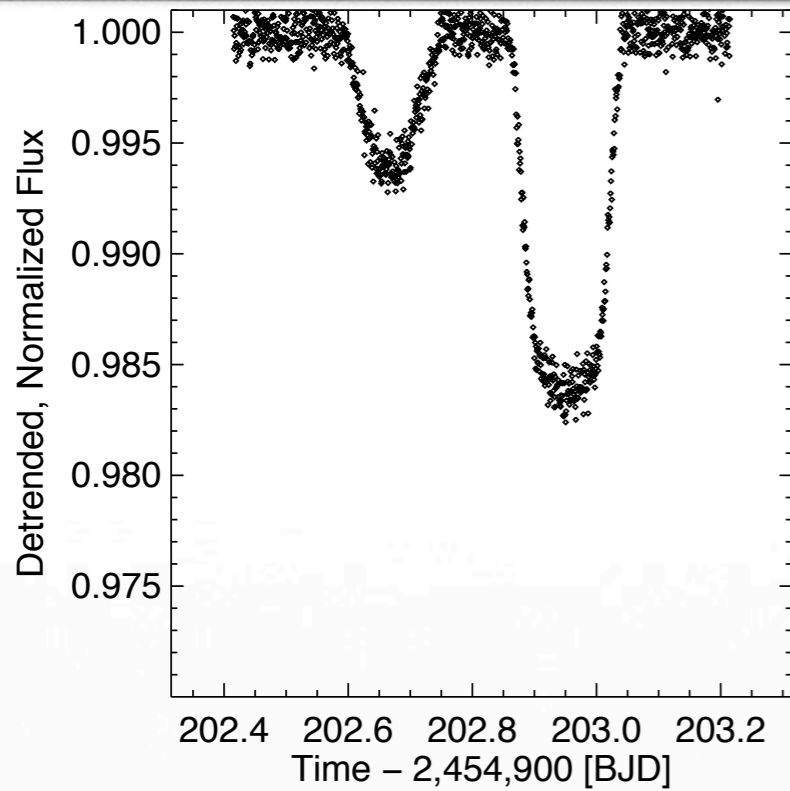
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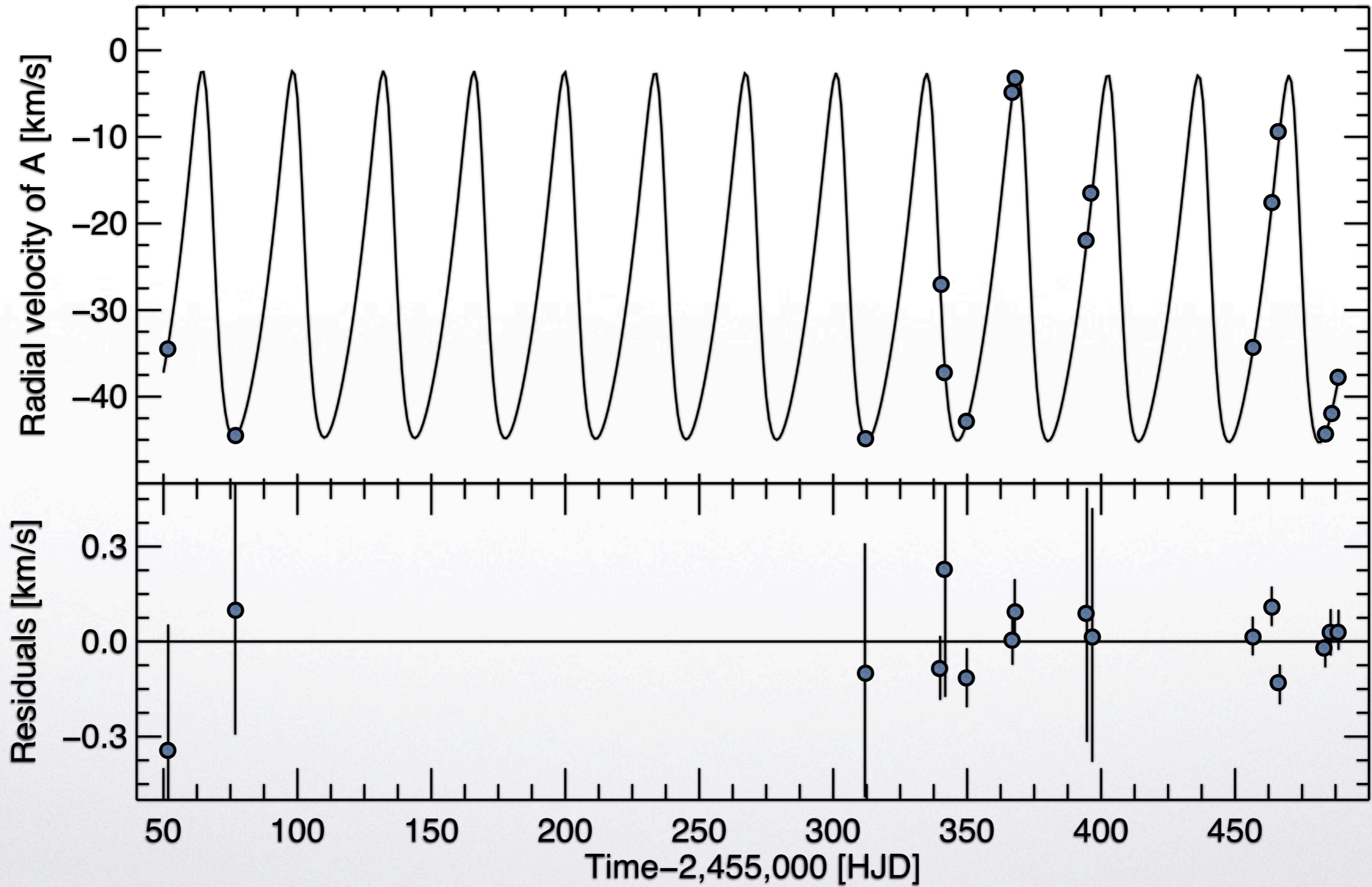
KOI-126: Light Curve Close-up



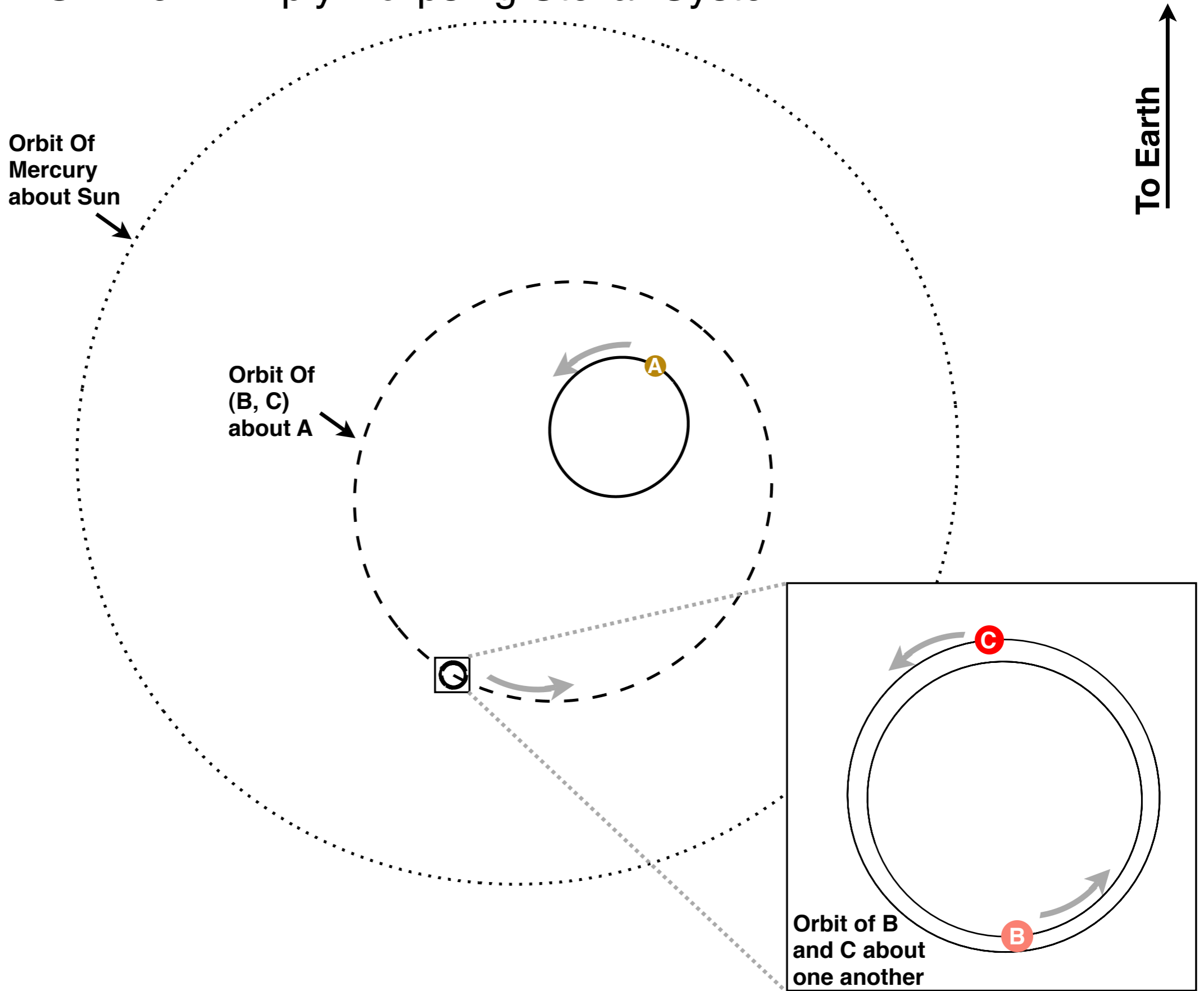
KOI-126: Light Curve Close-up



KOI-126



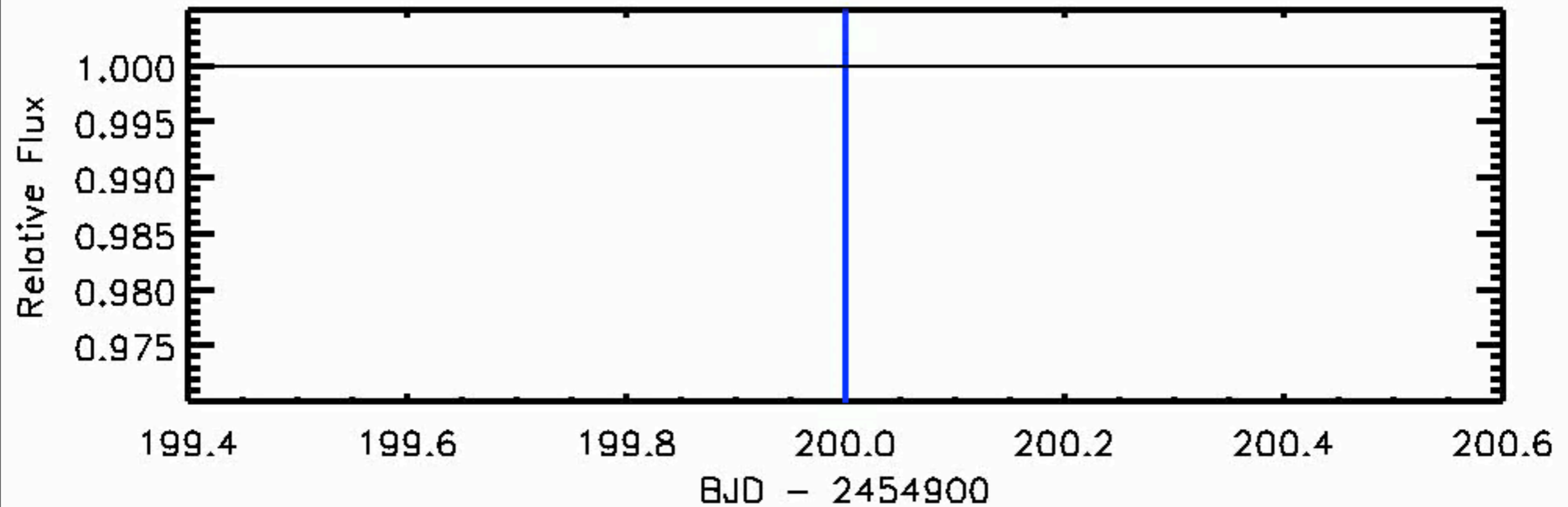
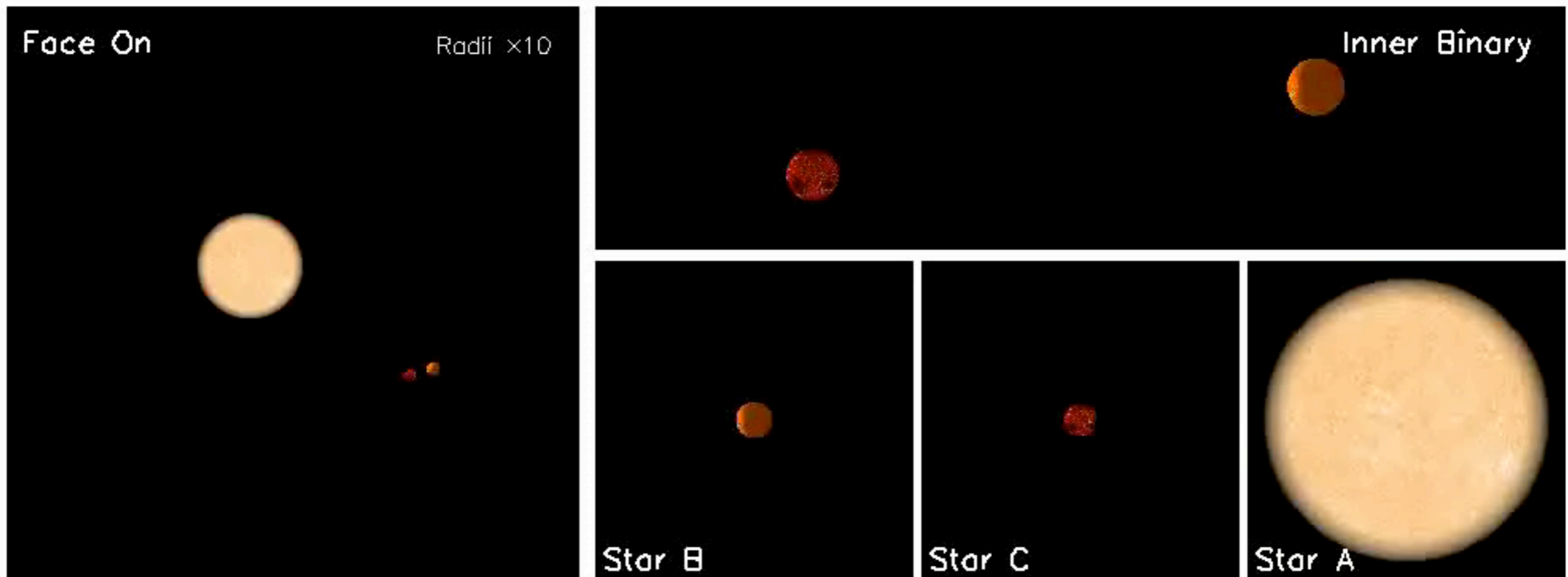
KOI-126: A Triply-Eclipsing Stellar System



Orbits and Stars to Scale

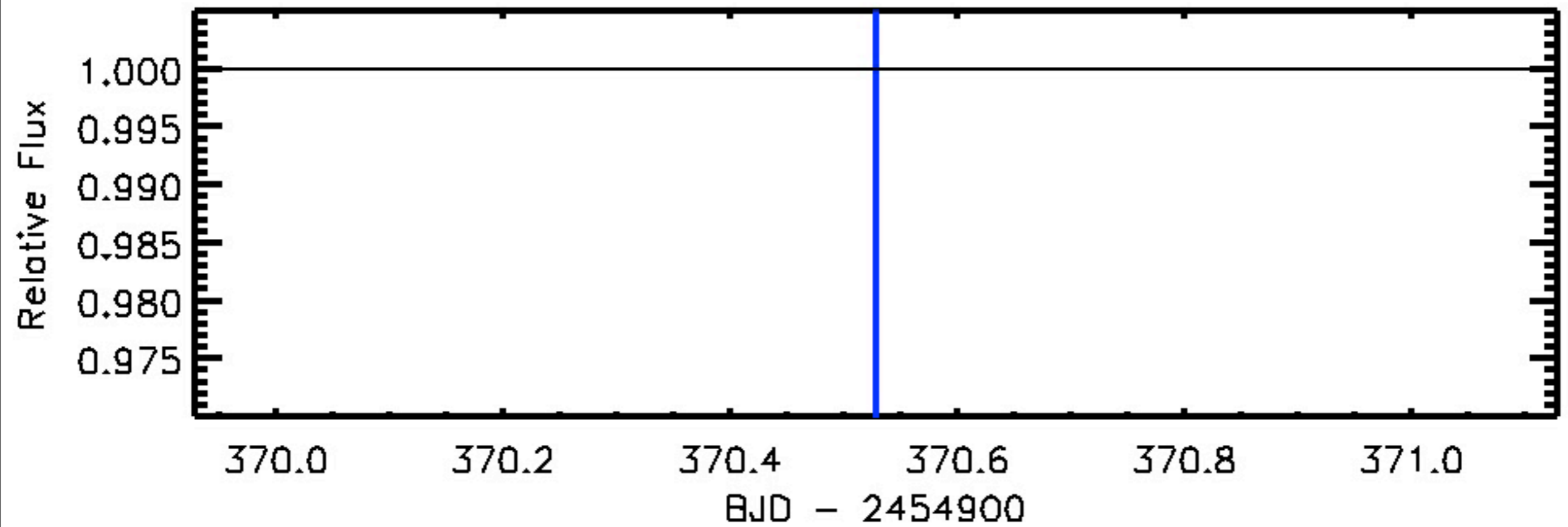
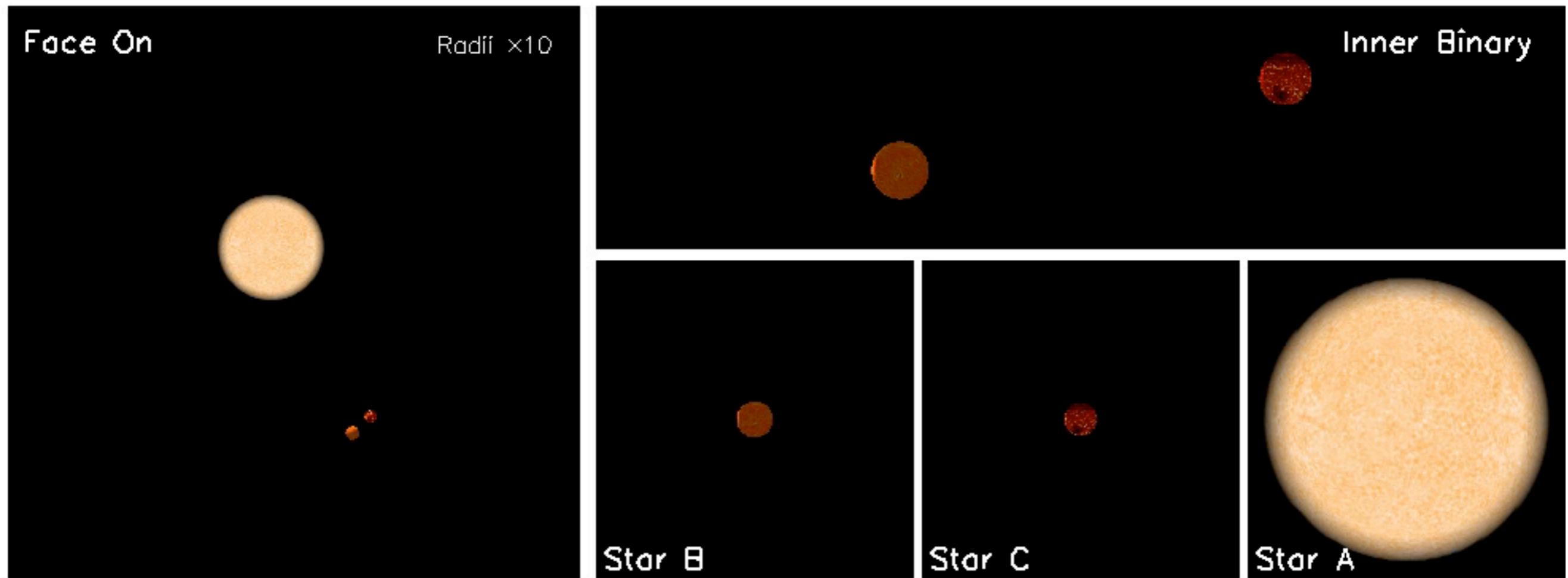


KOI-126

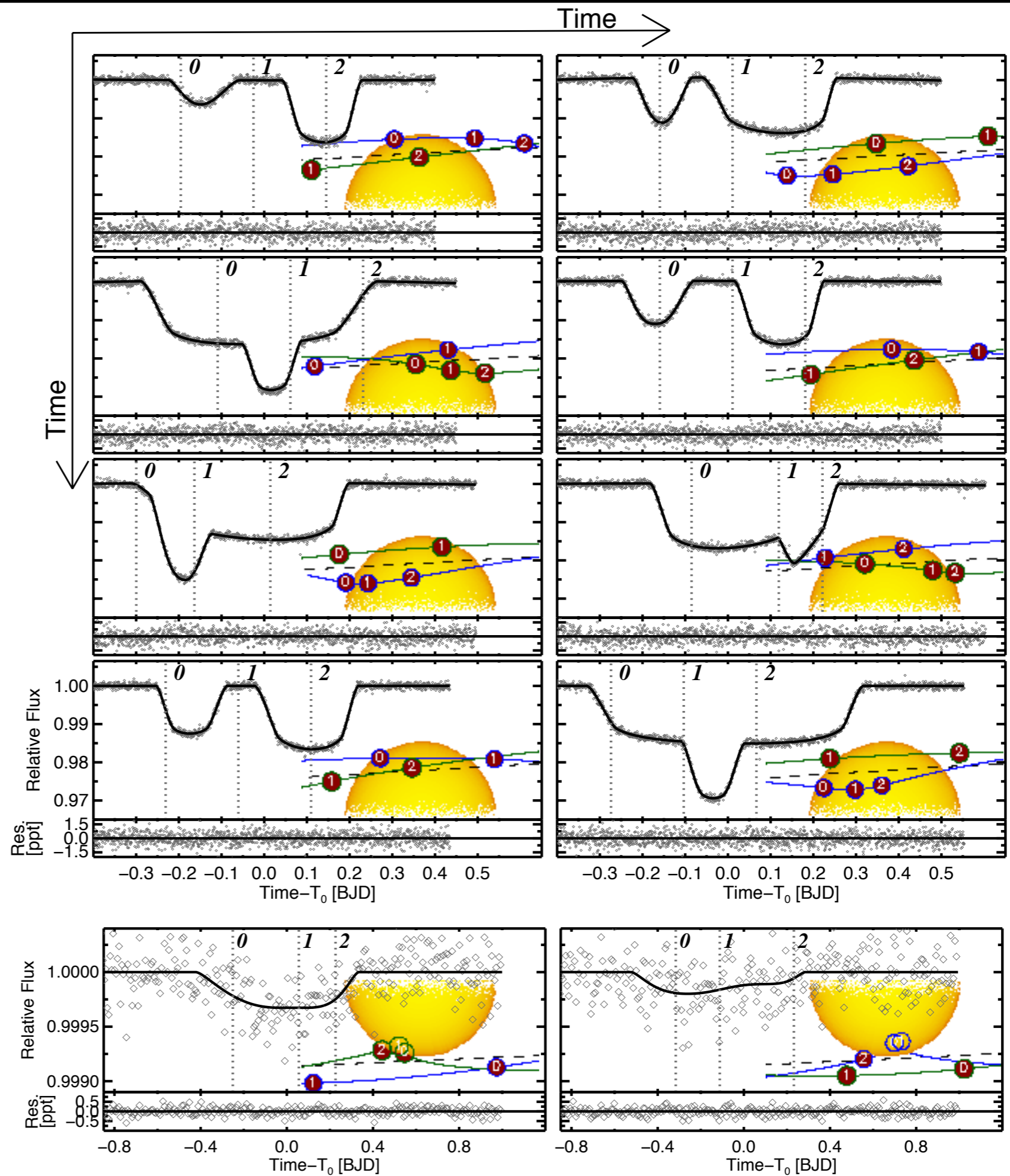


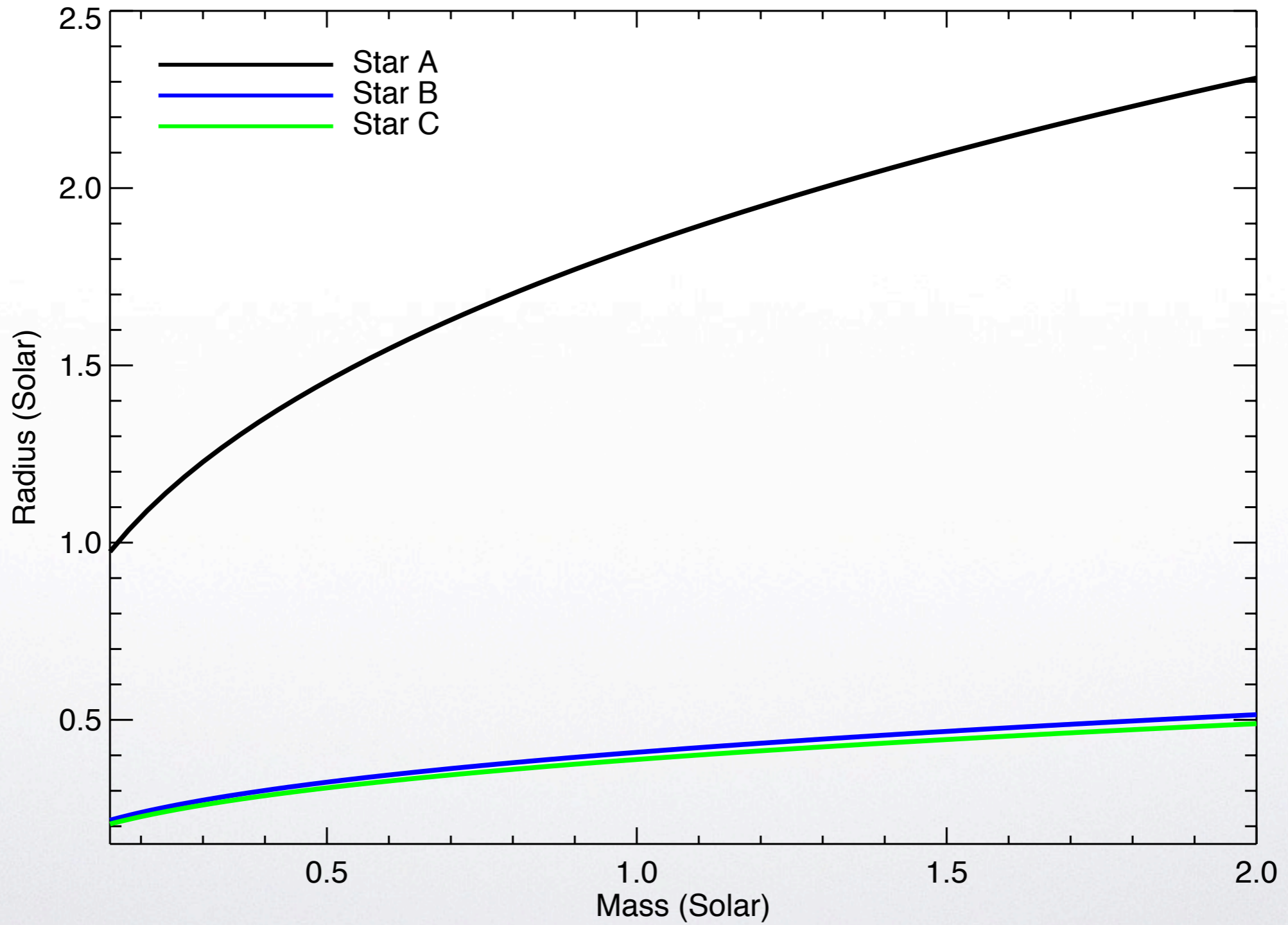


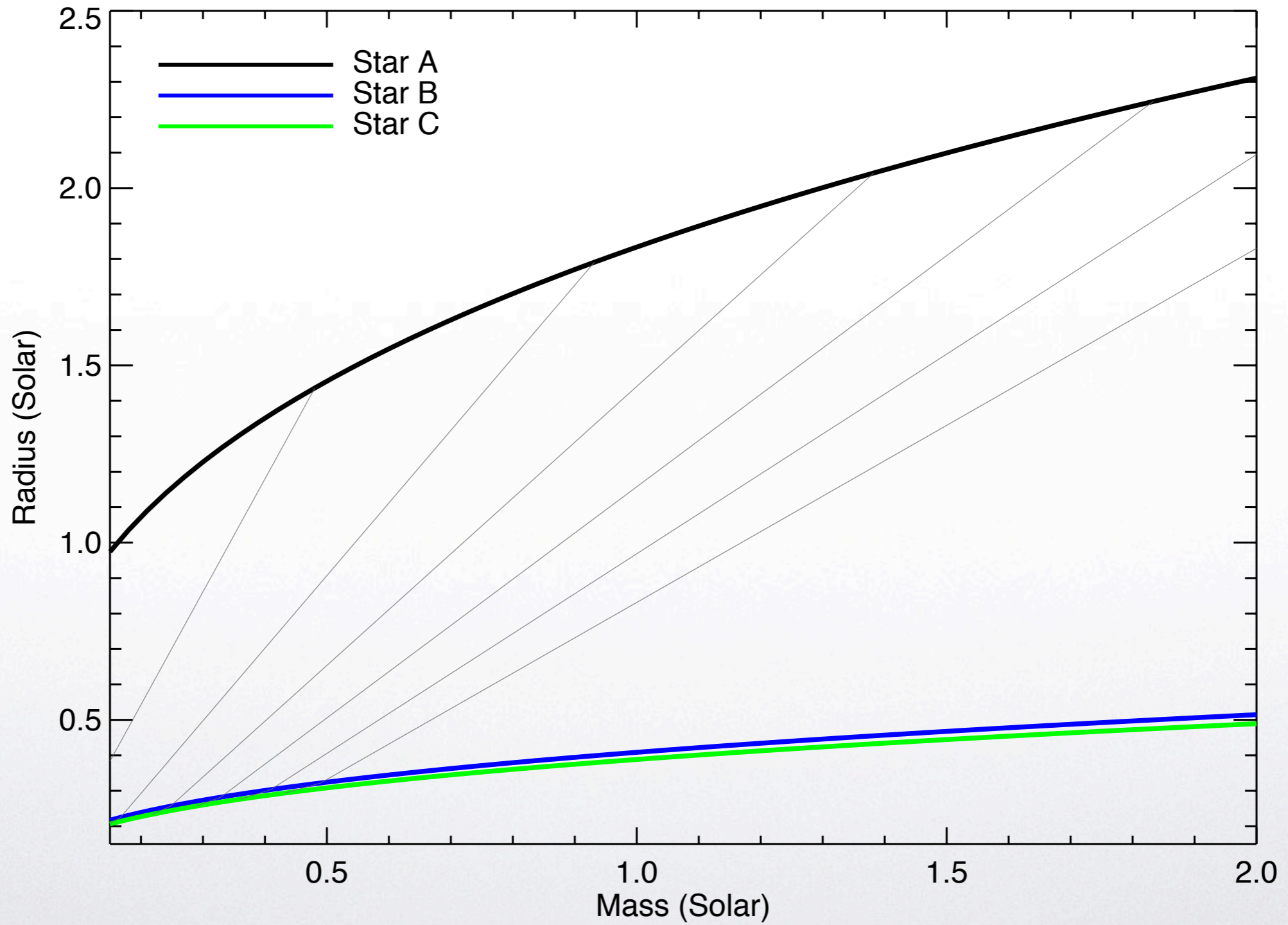
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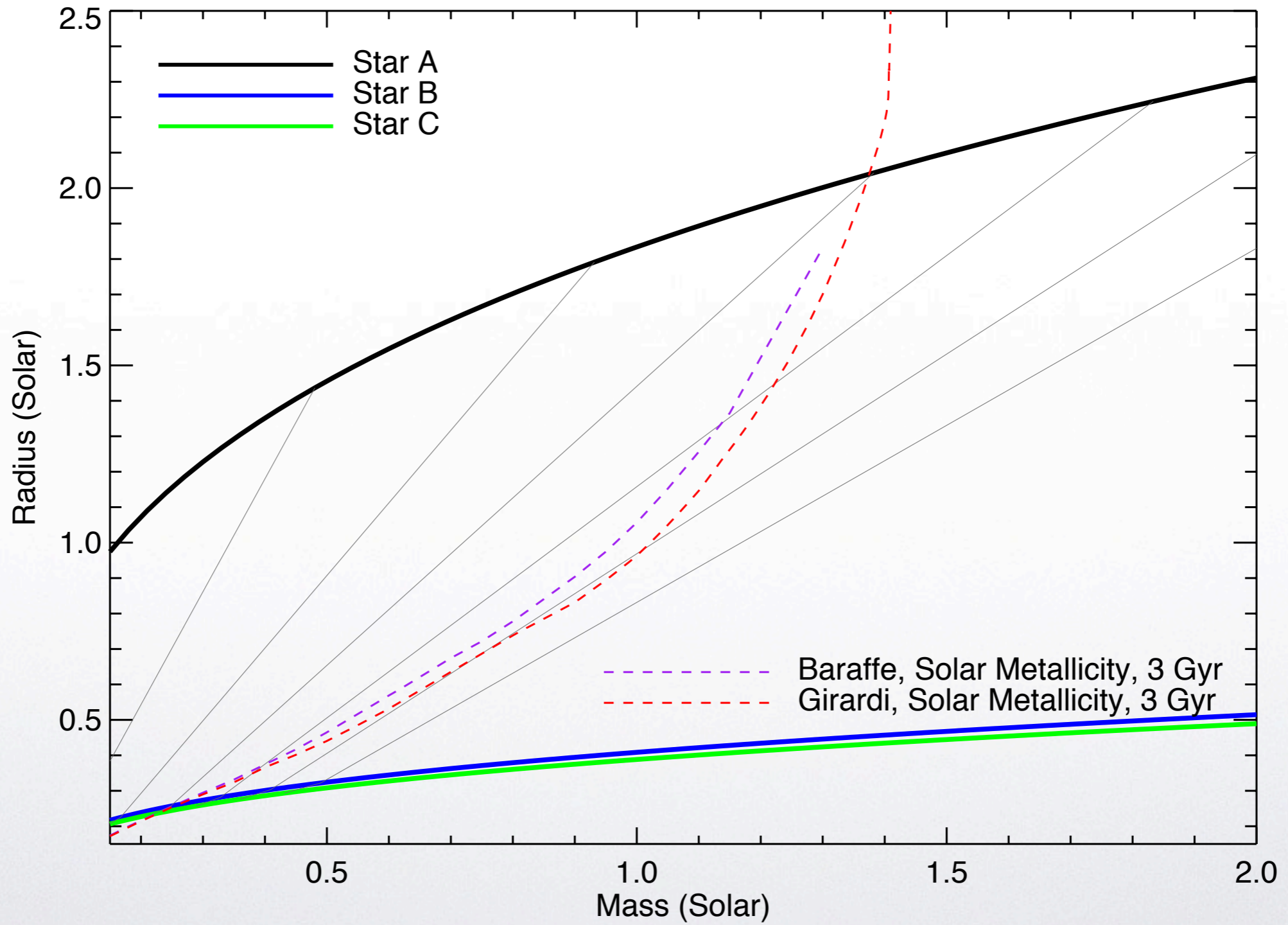


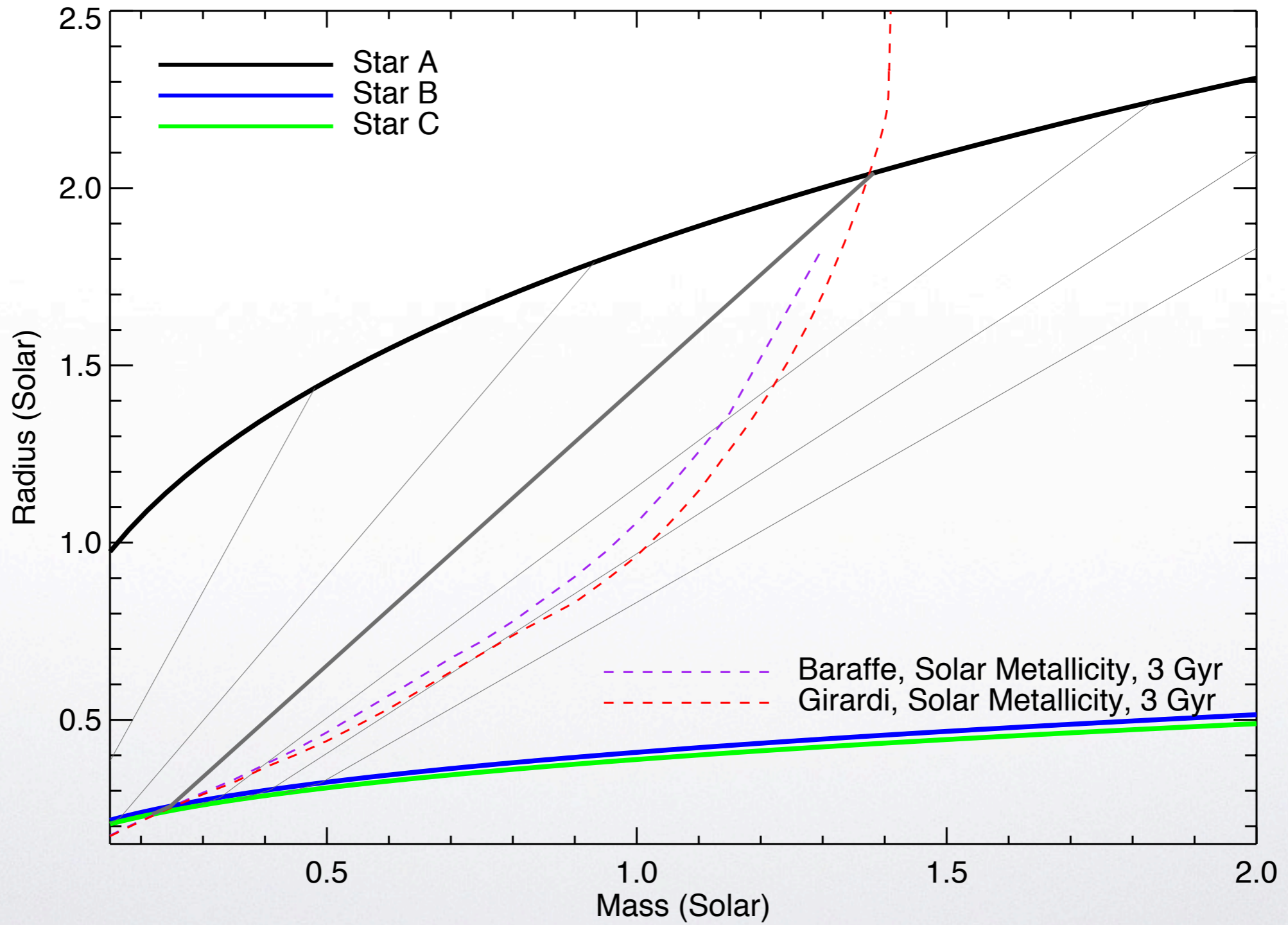
KOI-126

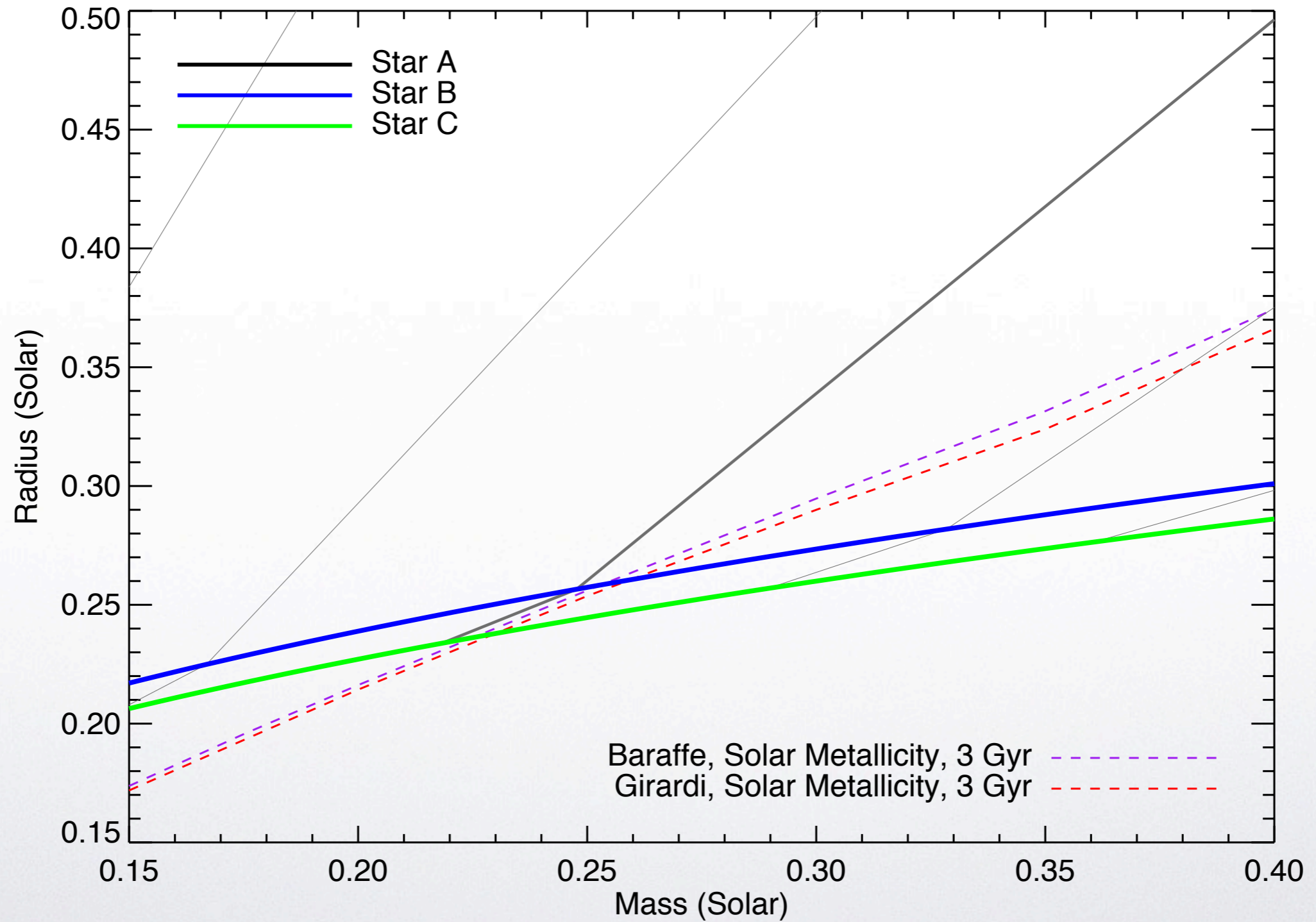












Parameter	Value
Masses	
M_A	$1.347 \pm 0.032 M_{\odot}$
M_B	$0.2413 \pm 0.0030 M_{\odot}$
M_C	$0.2127 \pm 0.0026 M_{\odot}$
Radii	
R_A	$2.0254 \pm 0.0098 R_{\odot}$
R_B	$0.2543 \pm 0.0014 R_{\odot}$
R_C	$0.2318 \pm 0.0013 R_{\odot}$

Parameter	Value
Masses	~2%
M_A	$1.347 \pm 0.032 M_{\odot}$
M_B	$0.2413 \pm 0.0030 M_{\odot}$
M_C	$0.2127 \pm 0.0026 M_{\odot}$
Radii	~0.5%
R_A	$2.0254 \pm 0.0098 R_{\odot}$
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- System metallicity and age courtesy of KOI-126 A:
 - $[Fe/H] \sim 0.15$
 - Age $\sim 4 \pm 1$ Gyr



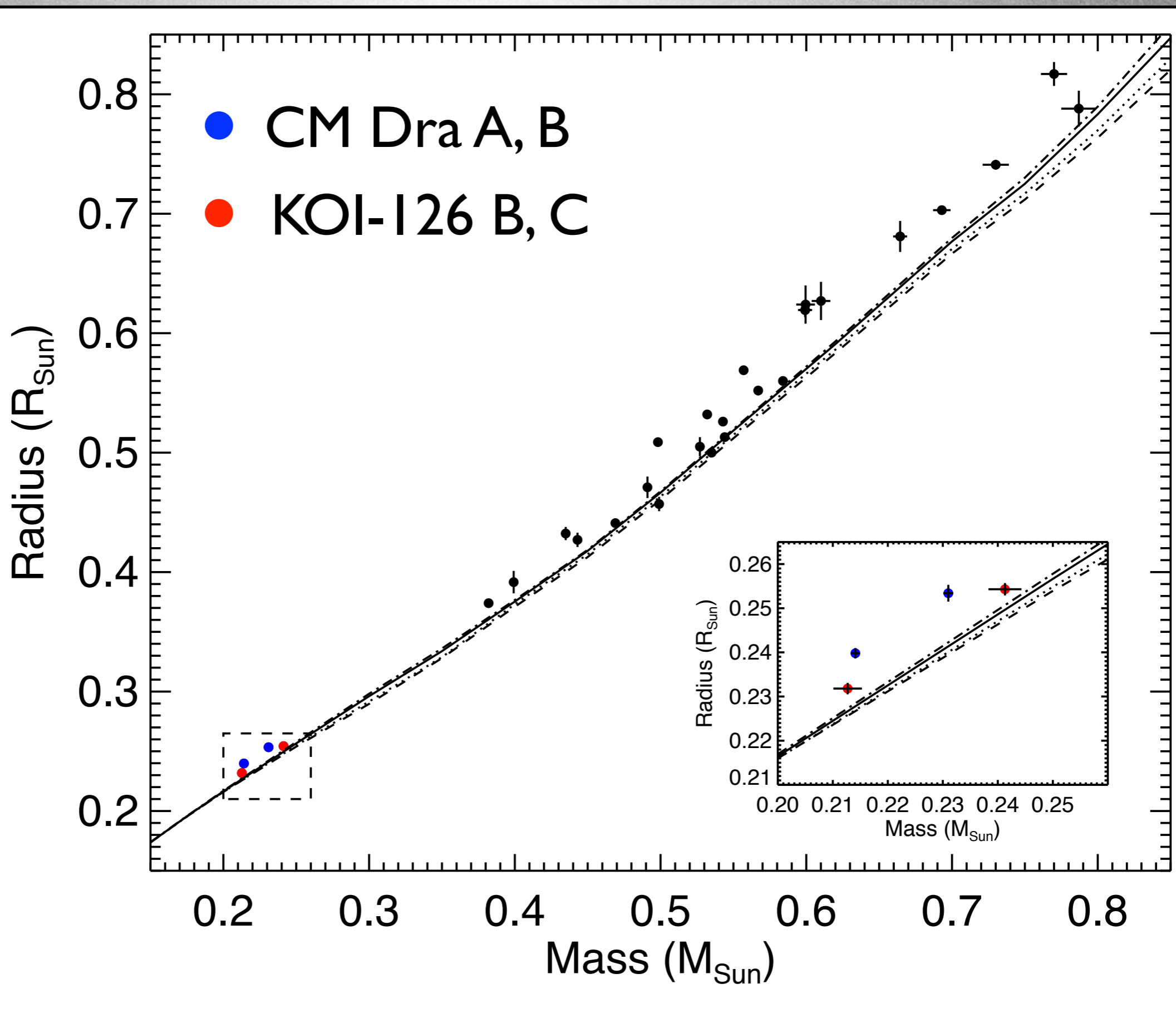
RESEARCH COMPUTING
Harvard University
Faculty of Arts and Sciences



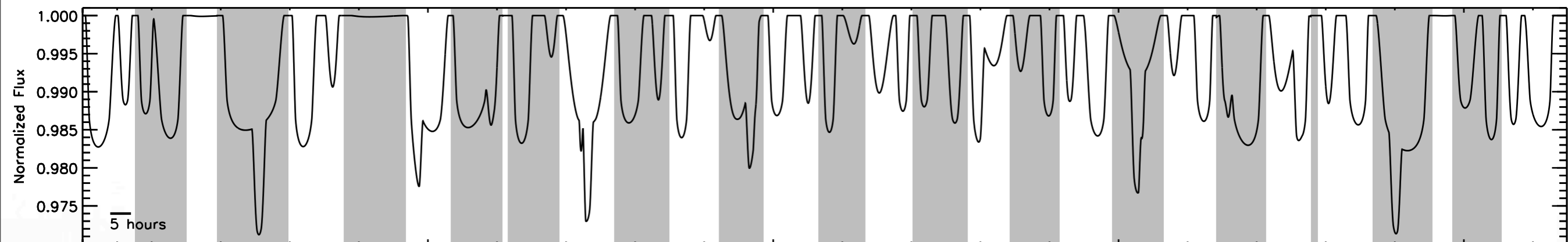
Parameter	Value
Masses	$\sim 2\%$
M_A	$1.347 \pm 0.032 M_\odot$
M_B	$0.2413 \pm 0.0030 M_\odot$
M_C	$0.2127 \pm 0.0026 M_\odot$
Radii	$\sim 0.5\%$
R_A	$2.0254 \pm 0.0098 R_\odot$
R_B	$0.2543 \pm 0.0014 R_\odot$
R_C	$0.2318 \pm 0.0013 R_\odot$

- System metallicity and age courtesy of KOI-126 A:
 - $[Fe/H] \sim 0.15$
 - Age $\sim 4 \pm 1$ Gyr

KOI-126 B,C

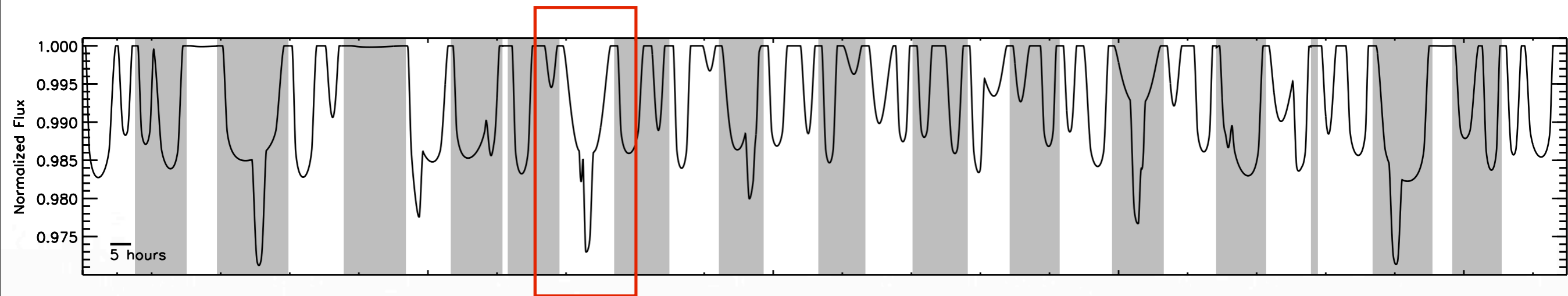


KOI-126: More to come



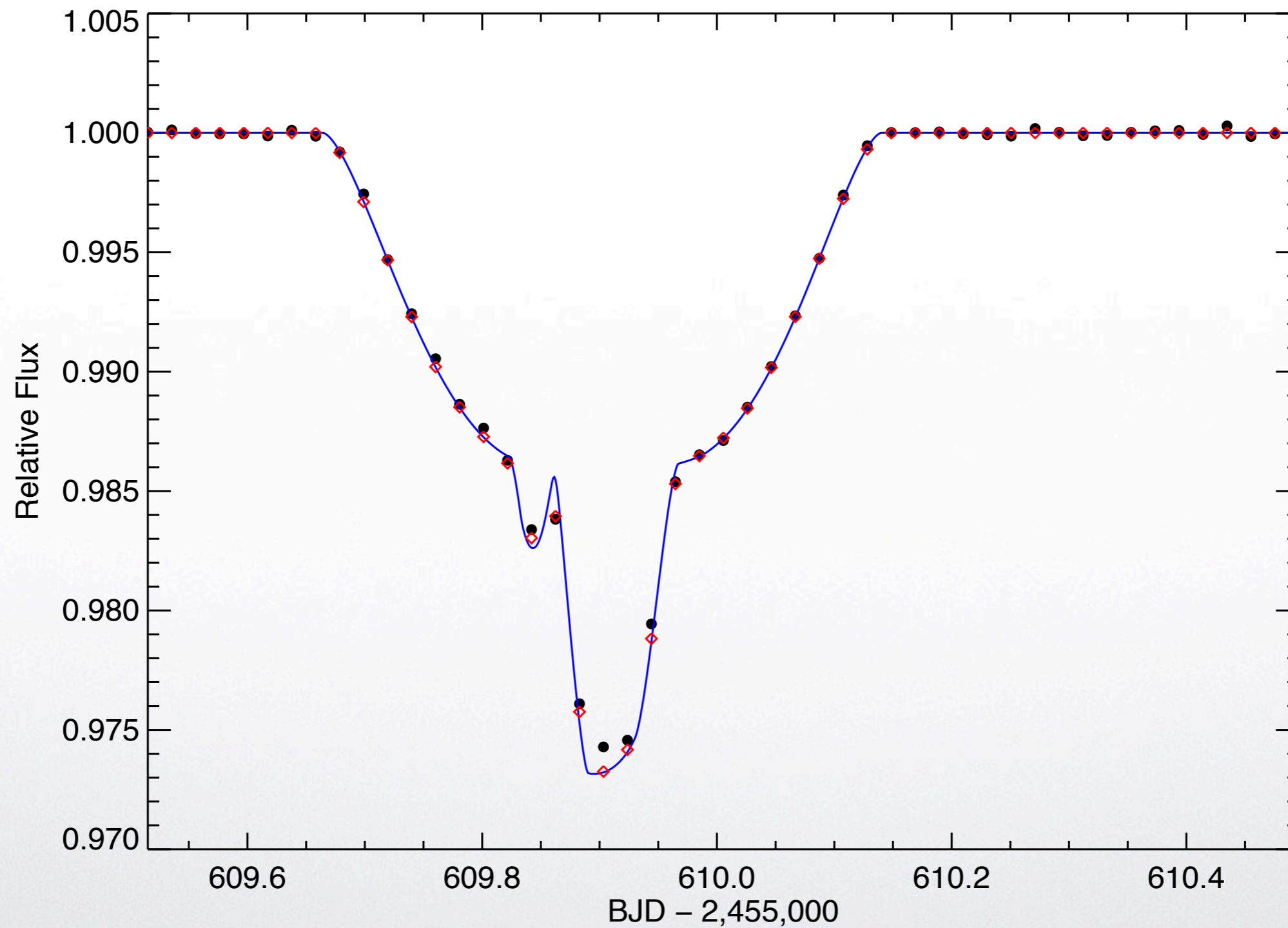
- Mass and radius determinations to better than a fraction of a percent
- $k_2 < 0.6$ @ 95% conf. with current data
- $k_2 \sim 0.1$ measured to $\sim 1\%$ with full mission data.

KOI-126: More to come



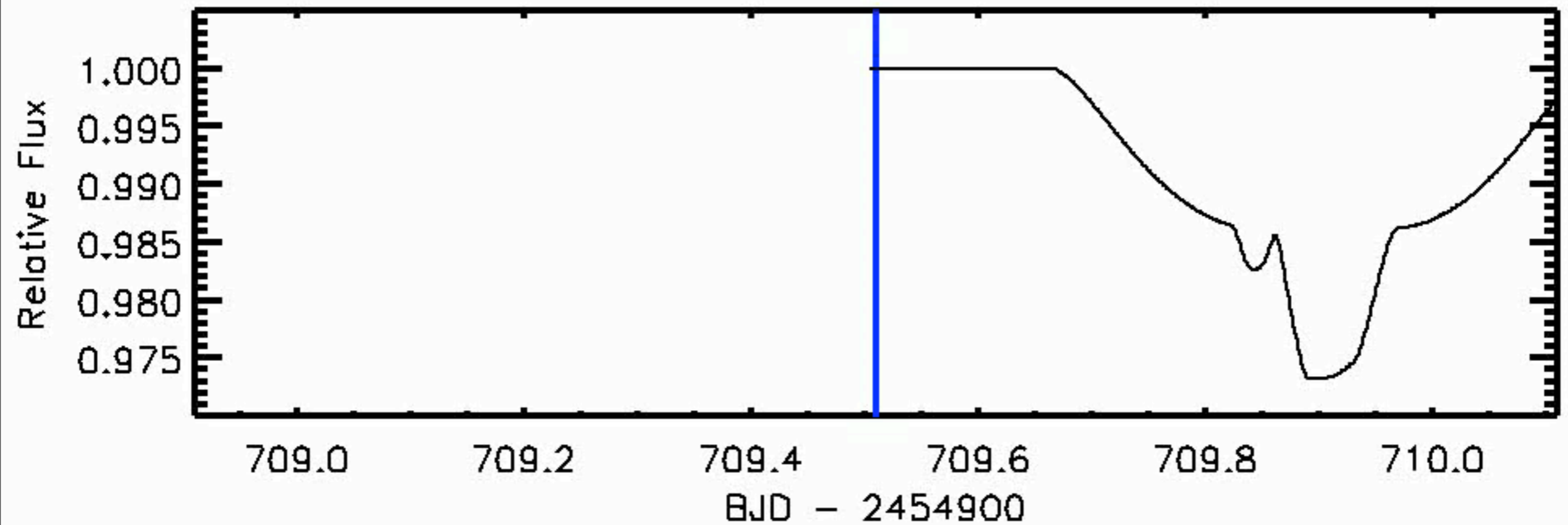
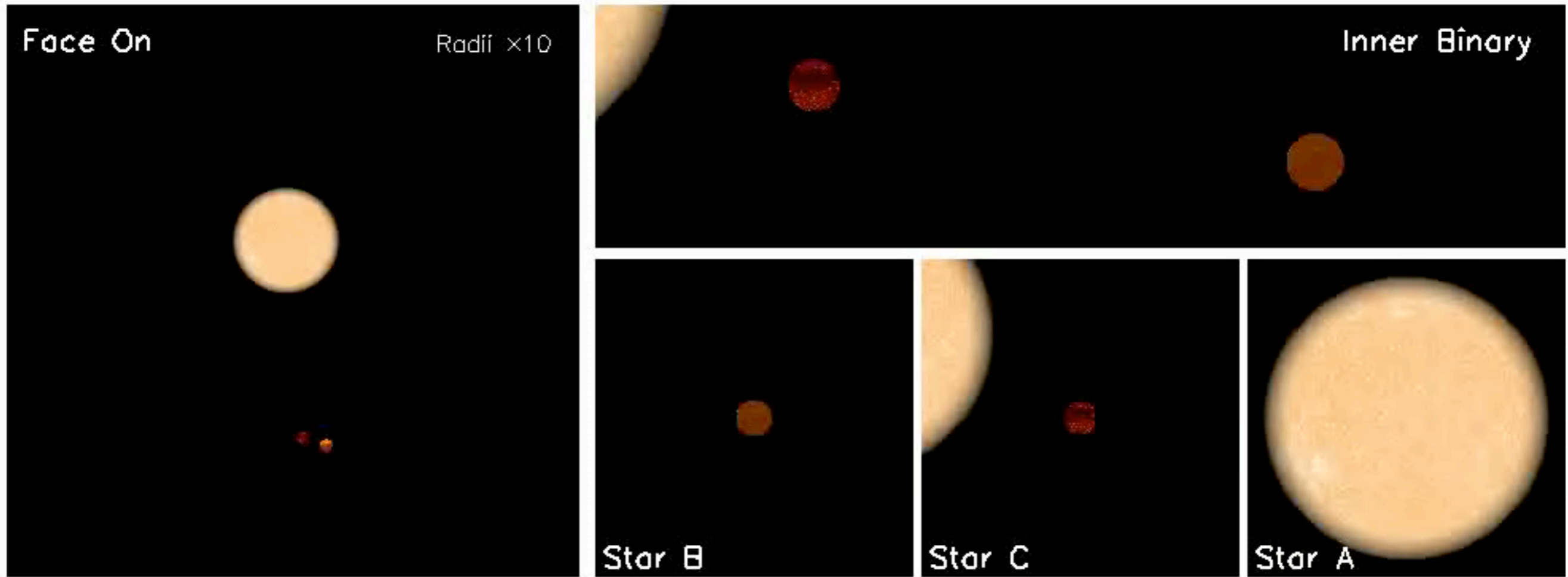
- Mass and radius determinations to better than a fraction of a percent
- $k_2 < 0.6$ @ 95% conf. with current data
- $k_2 \sim 0.1$ measured to $\sim 1\%$ with full mission data.

KOI-126: Syzygy! (aka "Mutual Event")

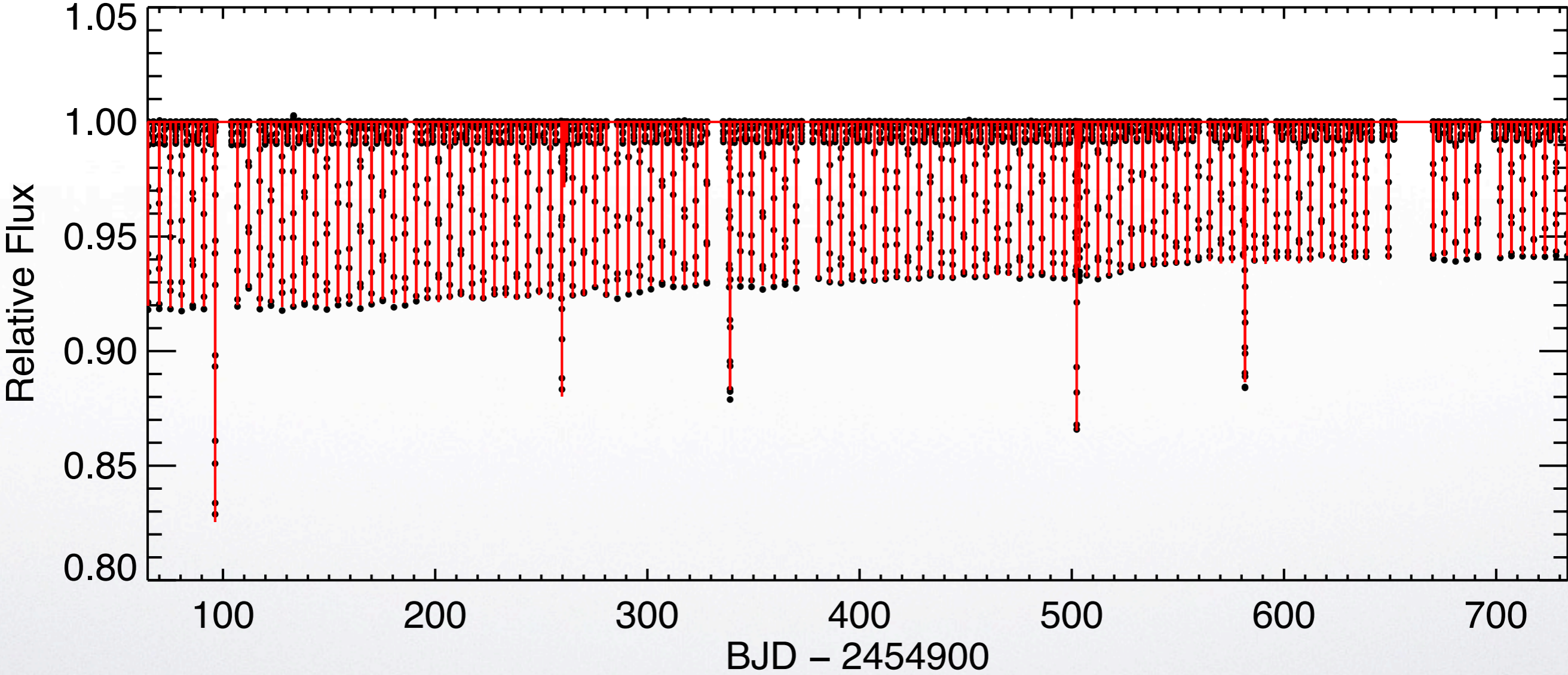




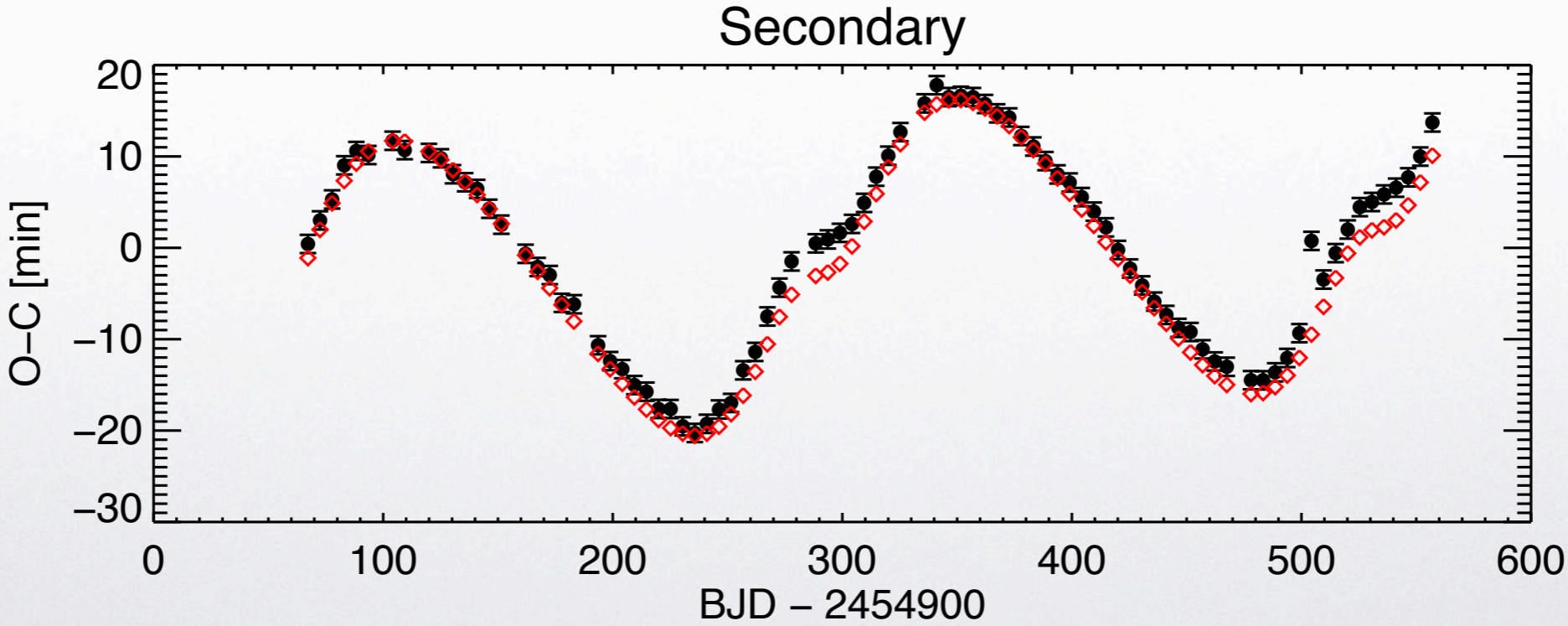
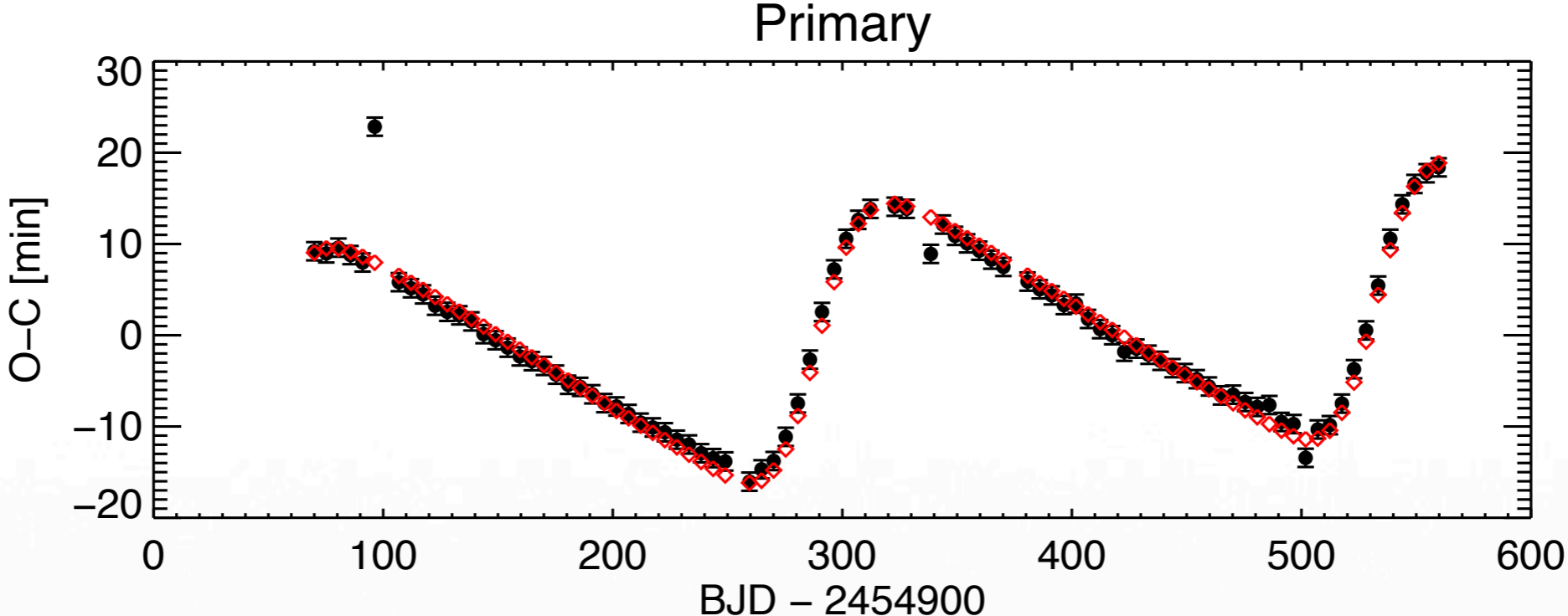
KOI-126



In the works... KIC 7289157

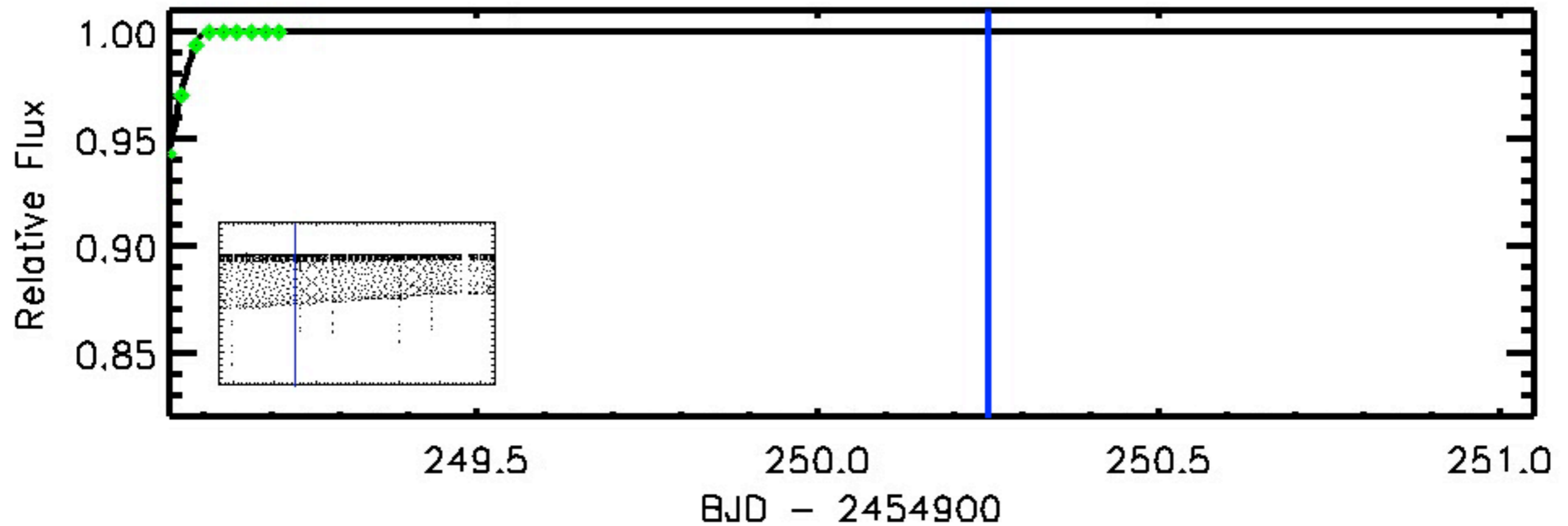
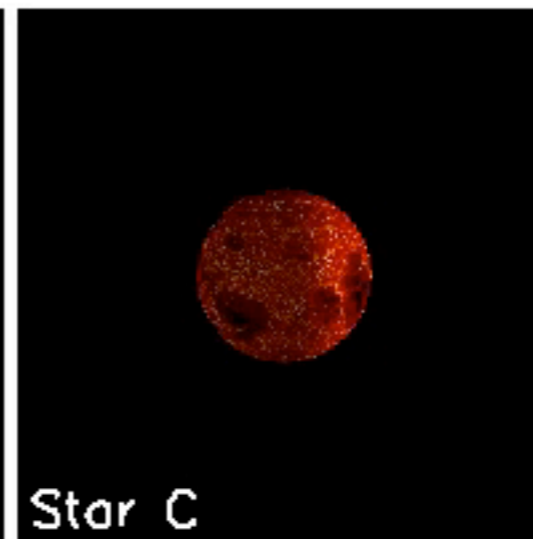
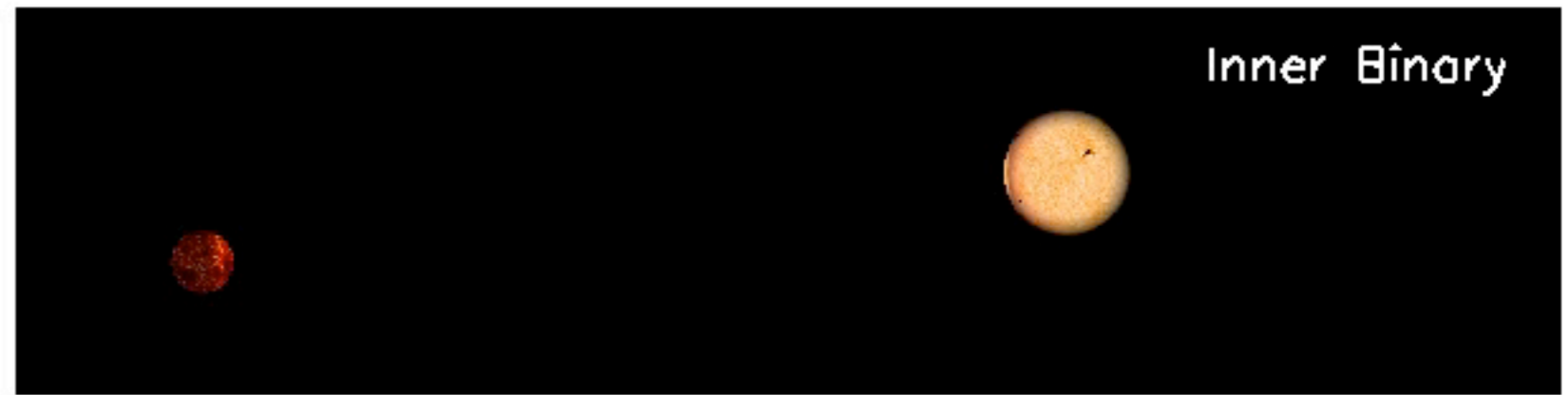
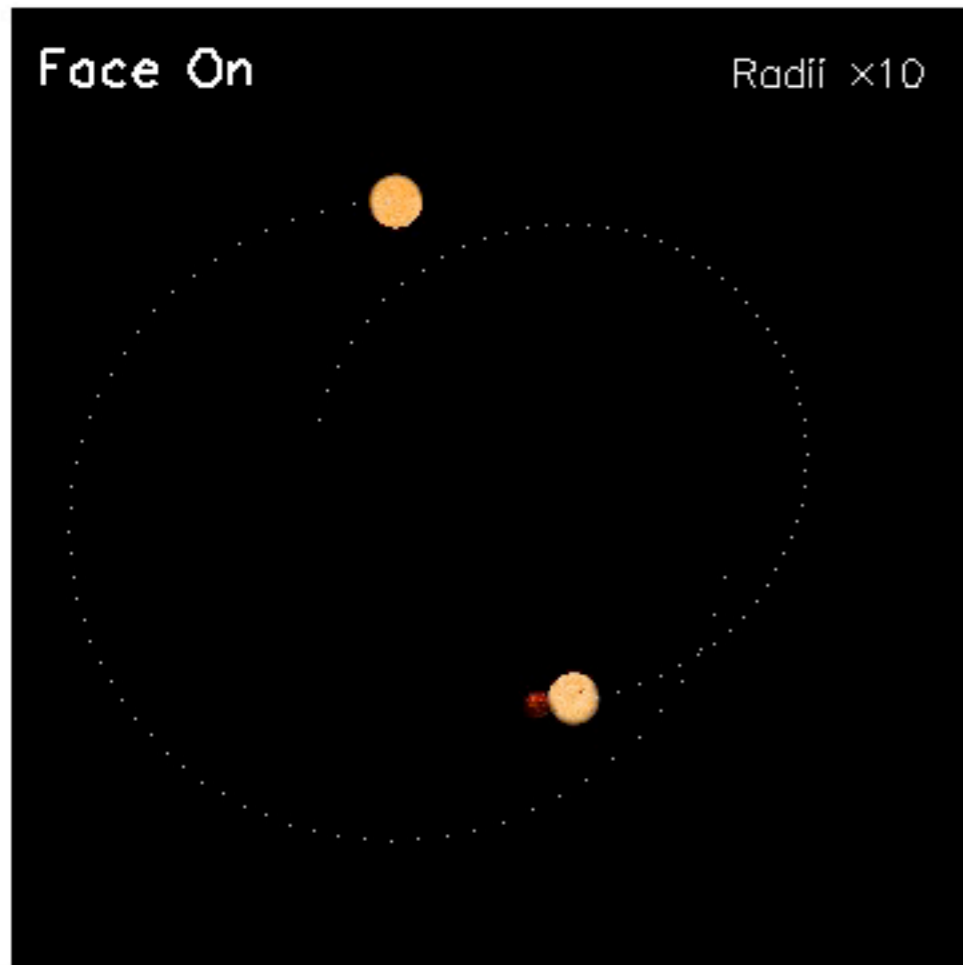


In the works... KIC 7289157

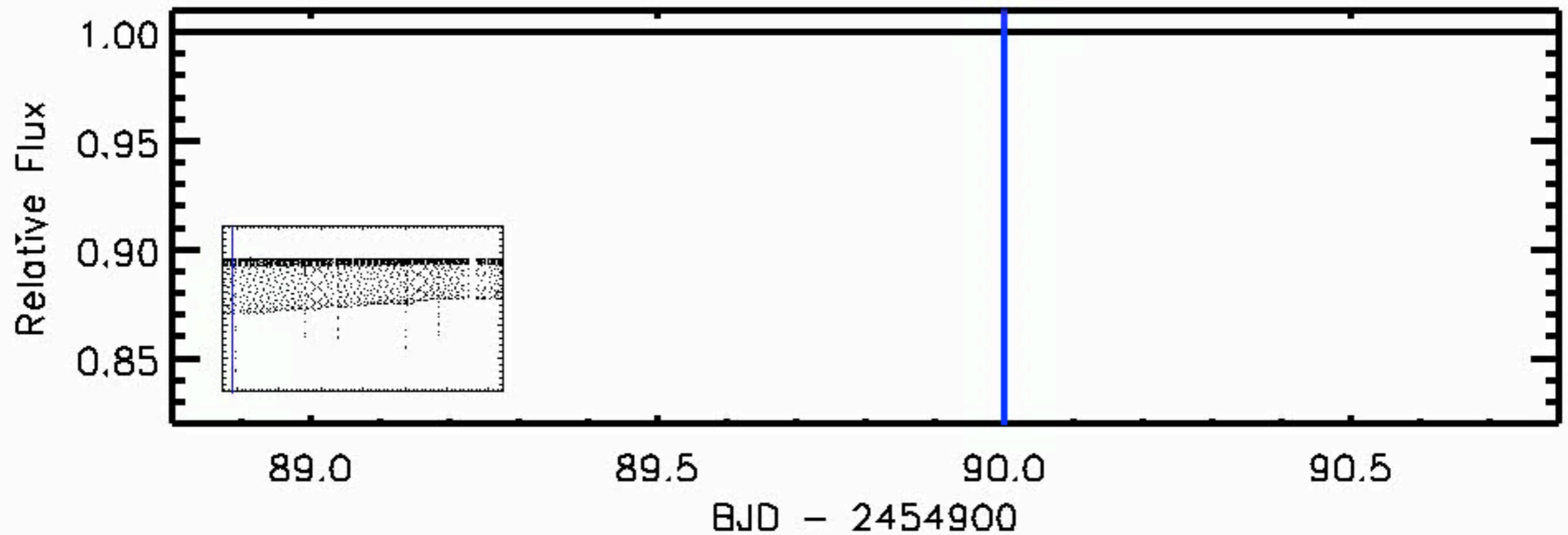
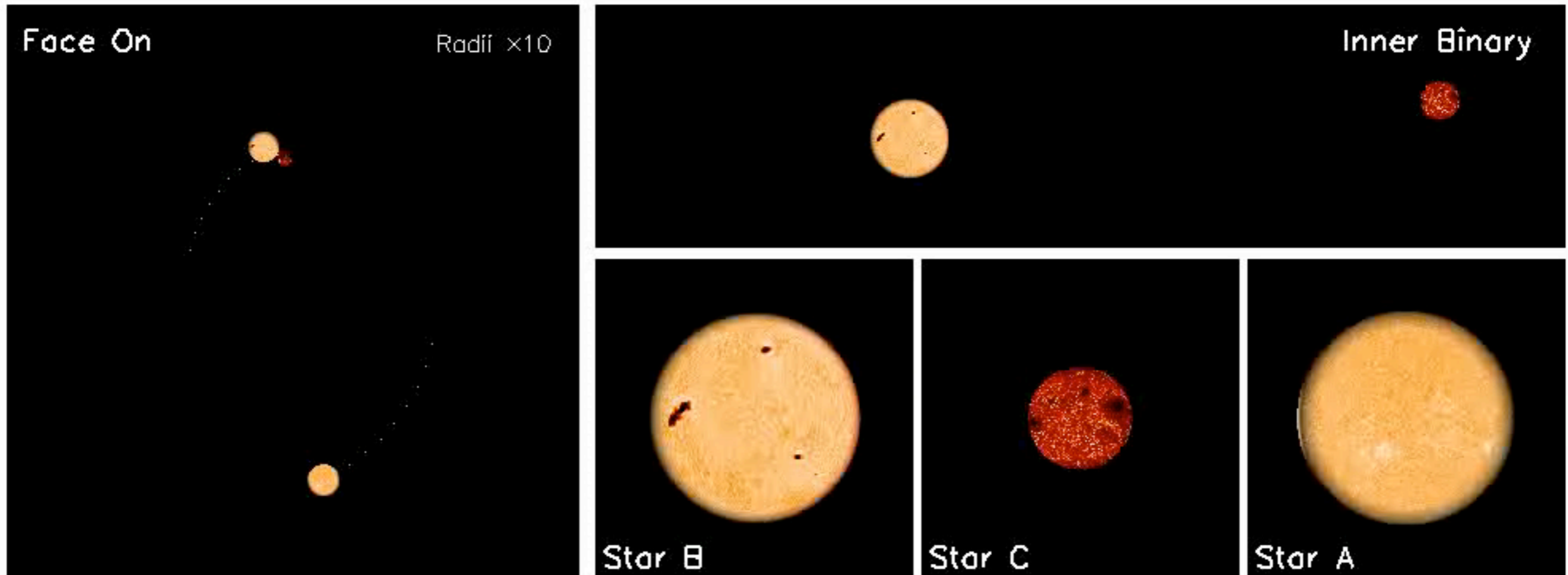


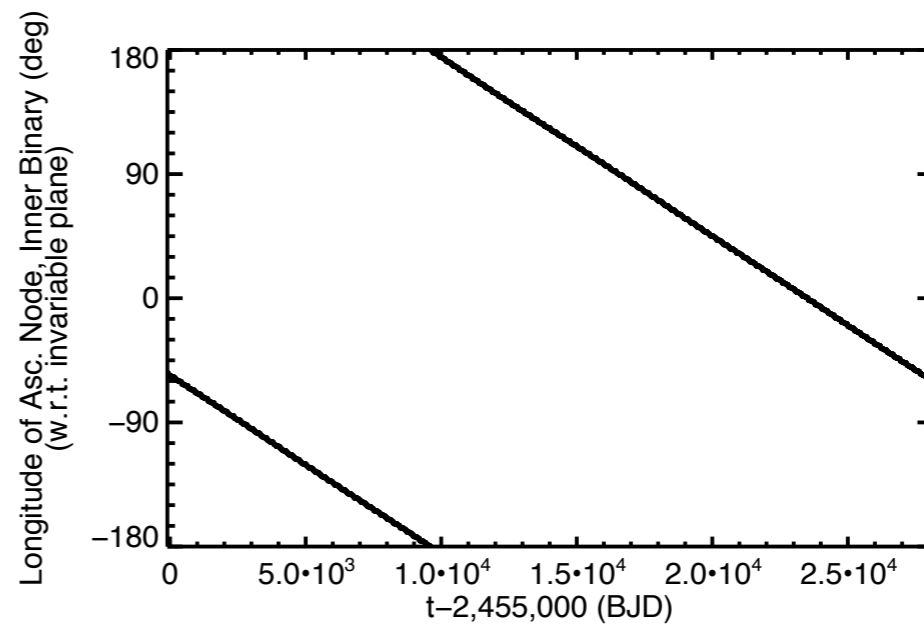
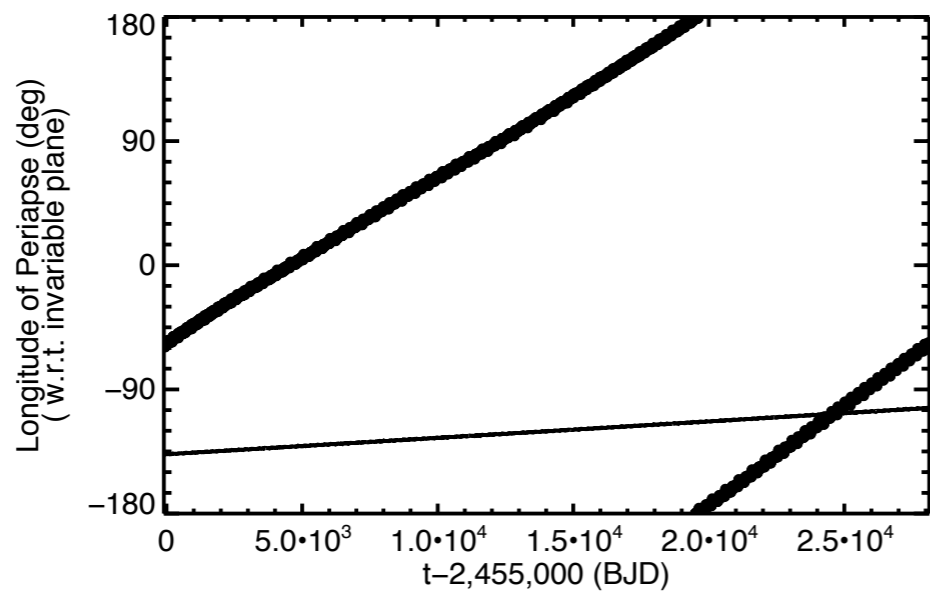
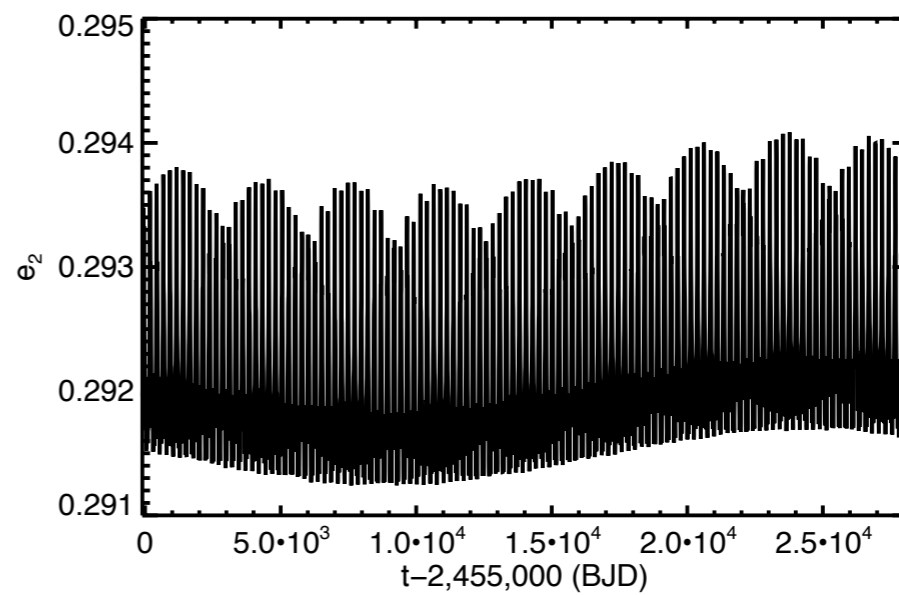
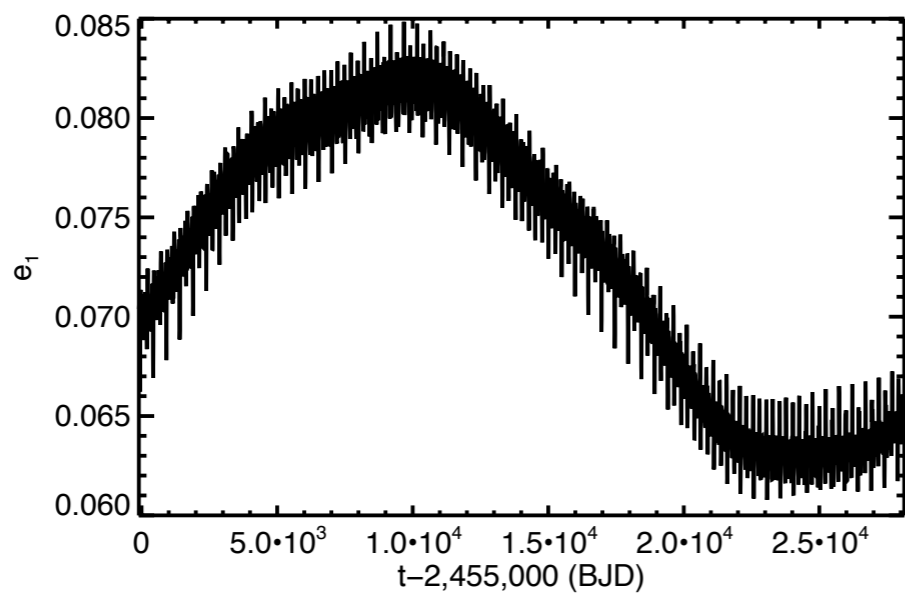
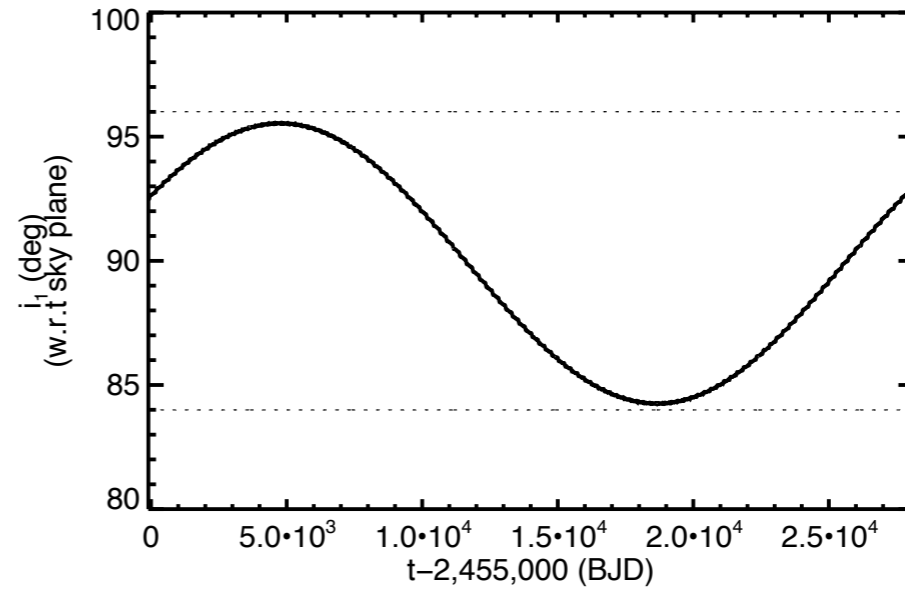
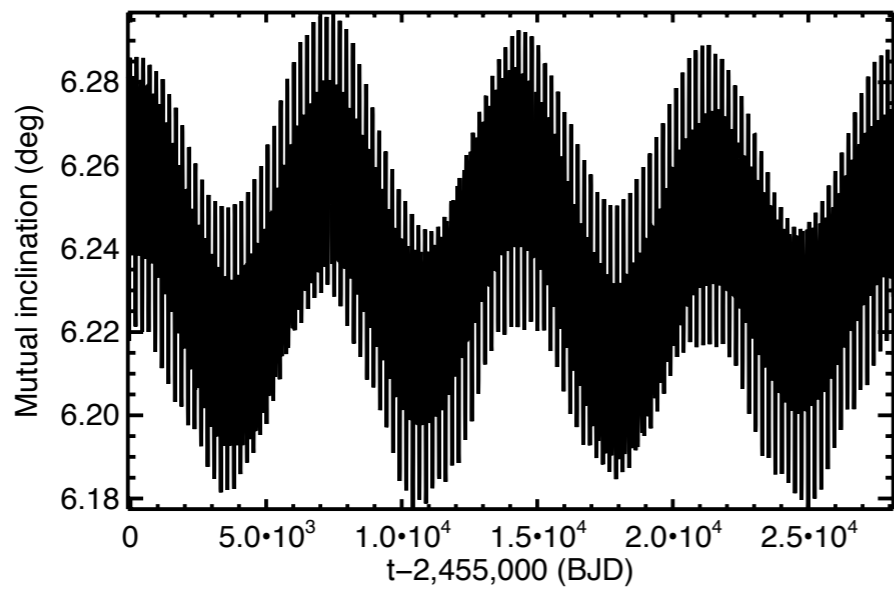


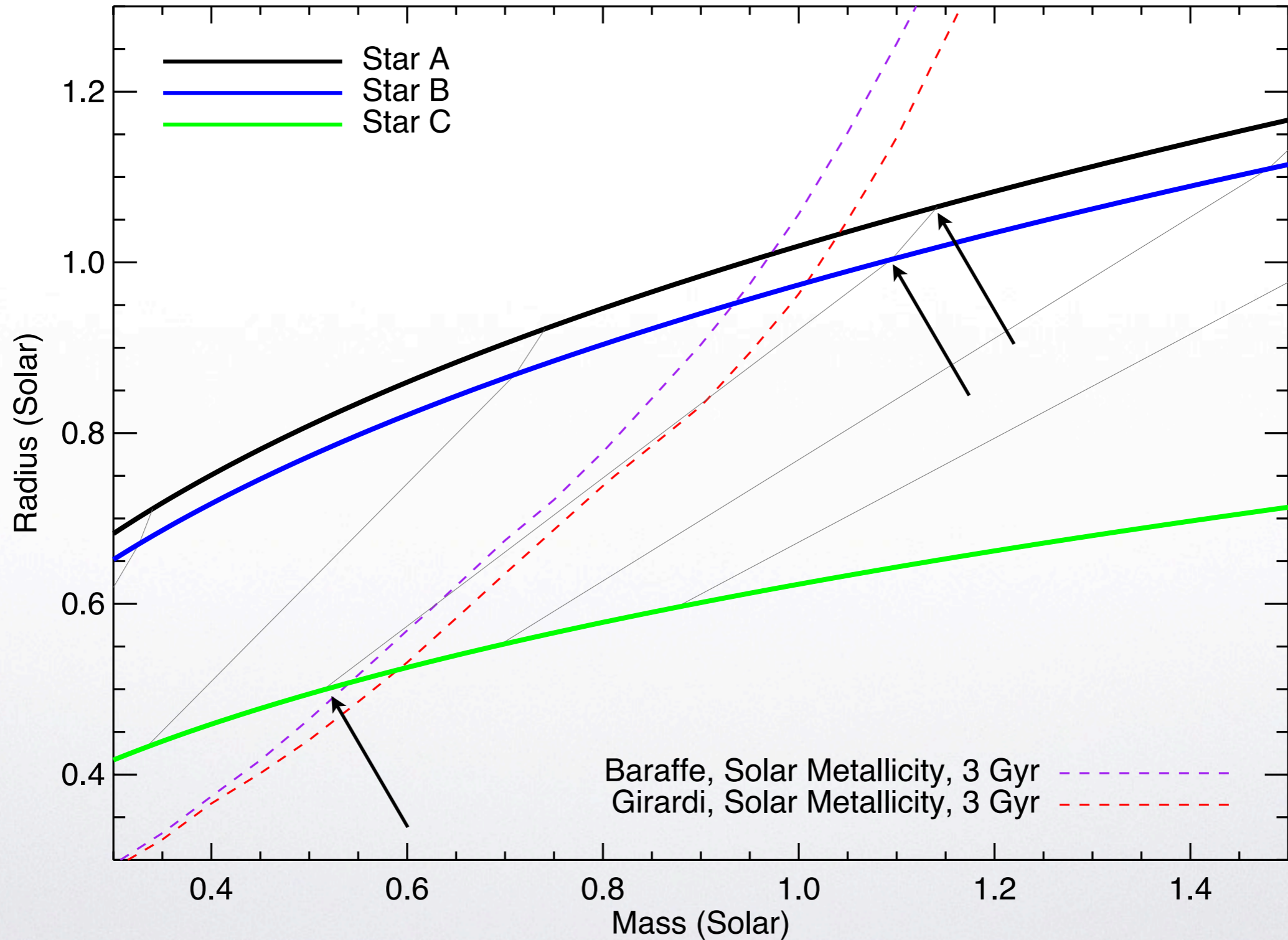
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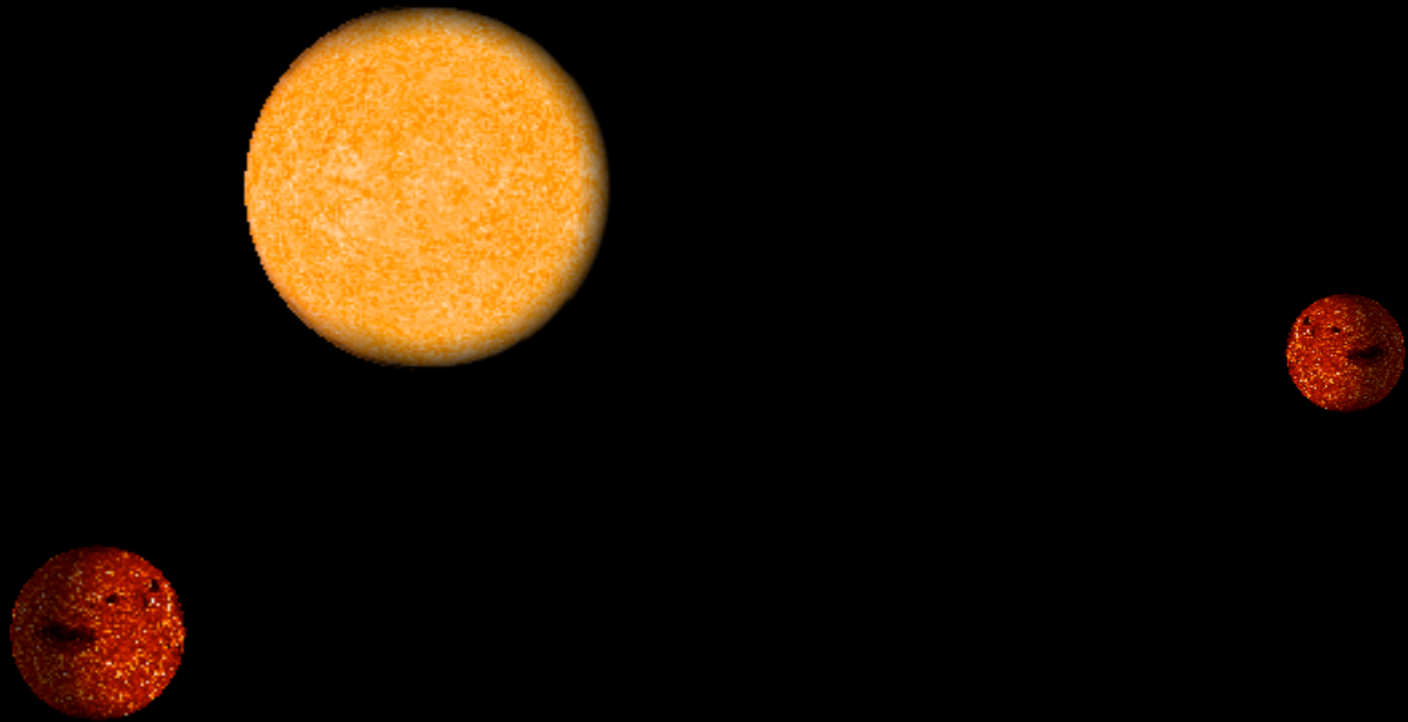


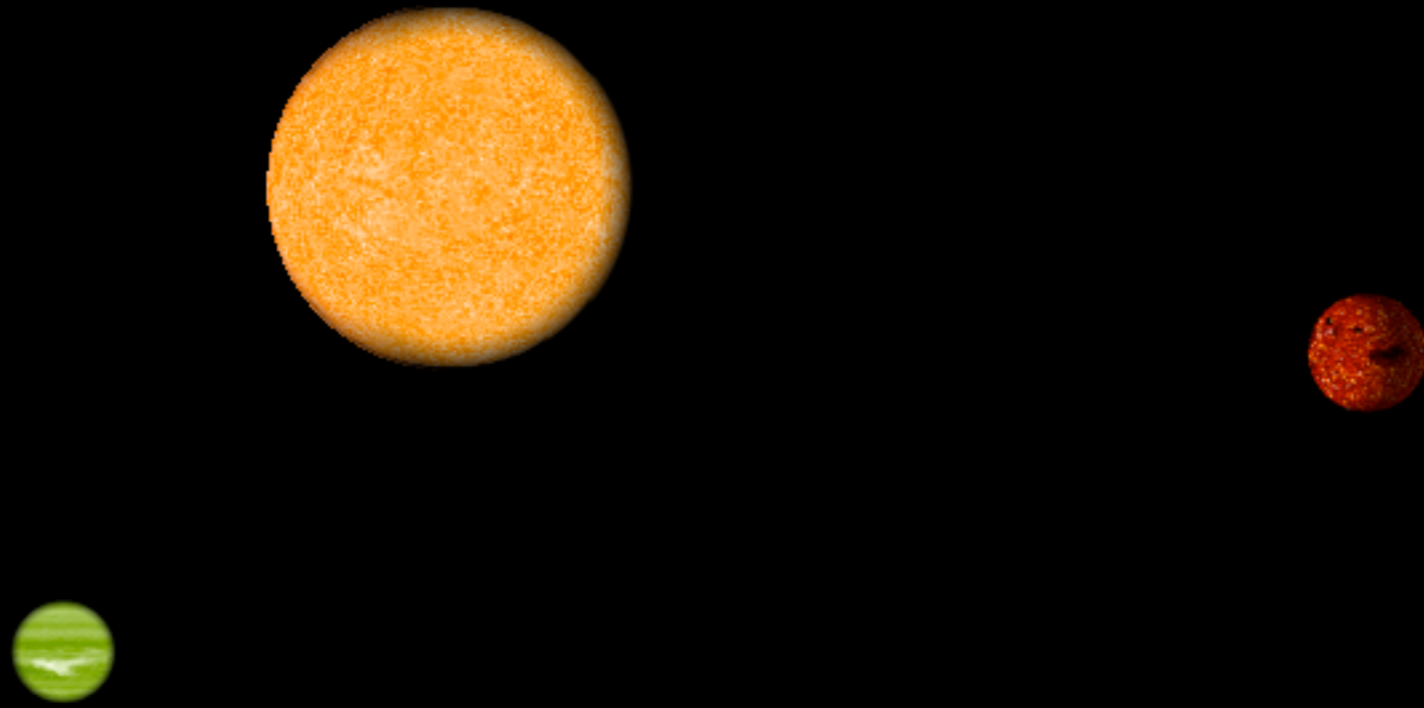
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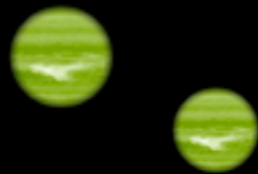




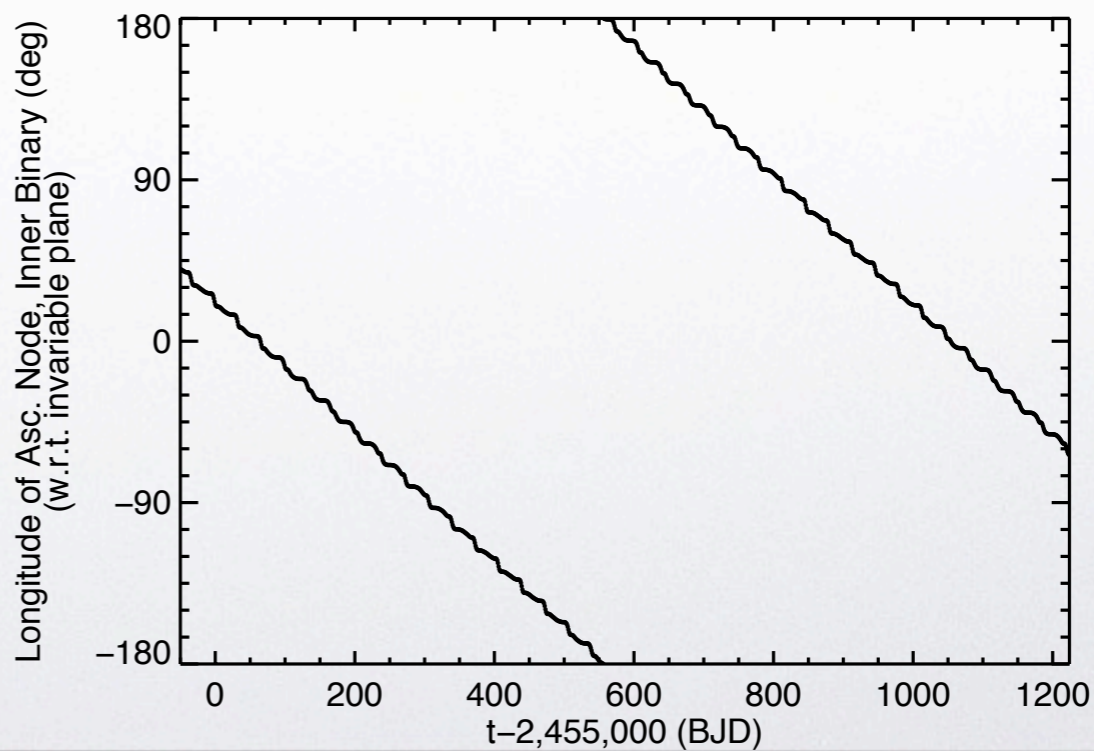
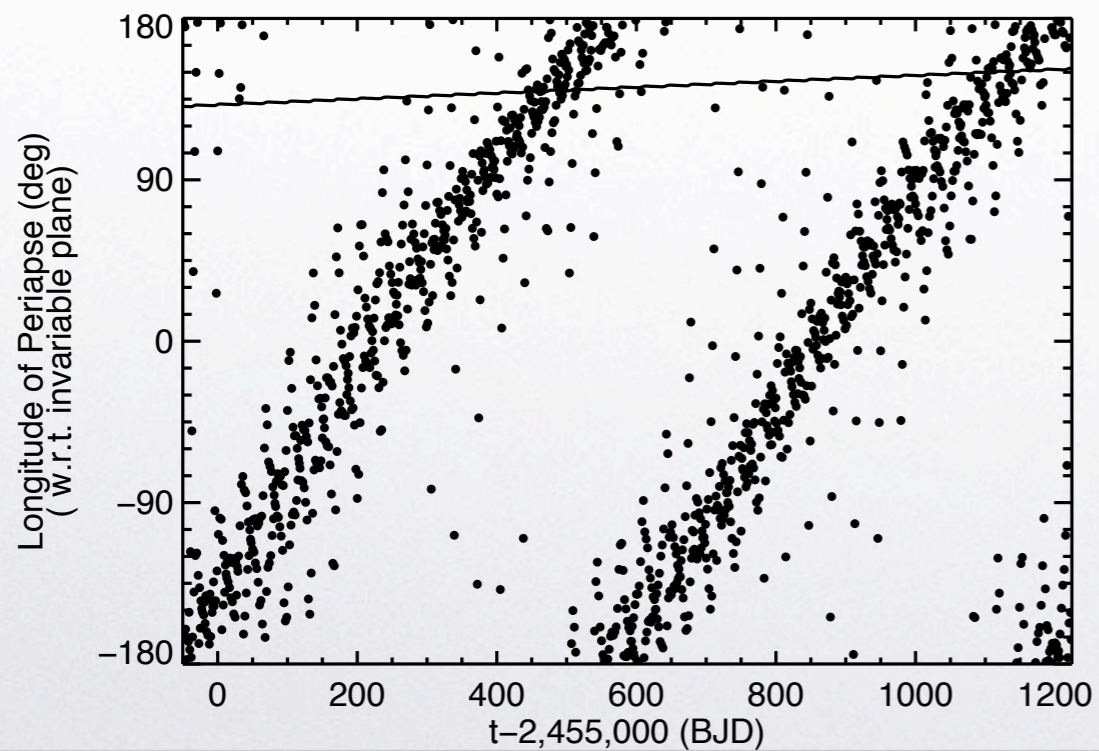
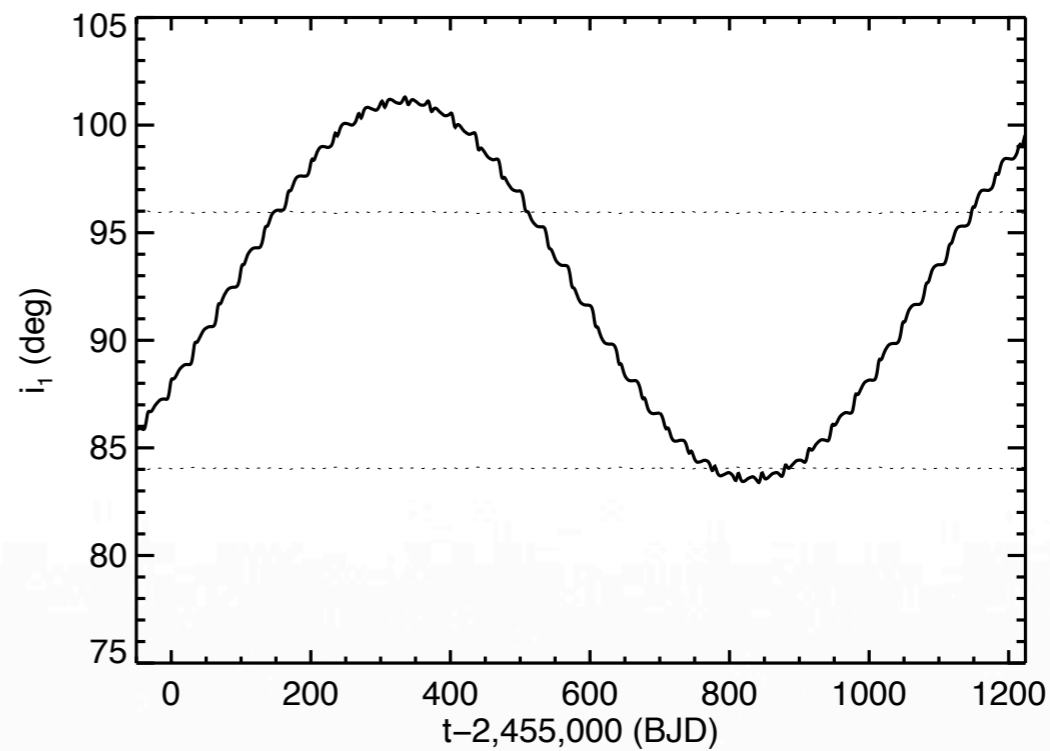
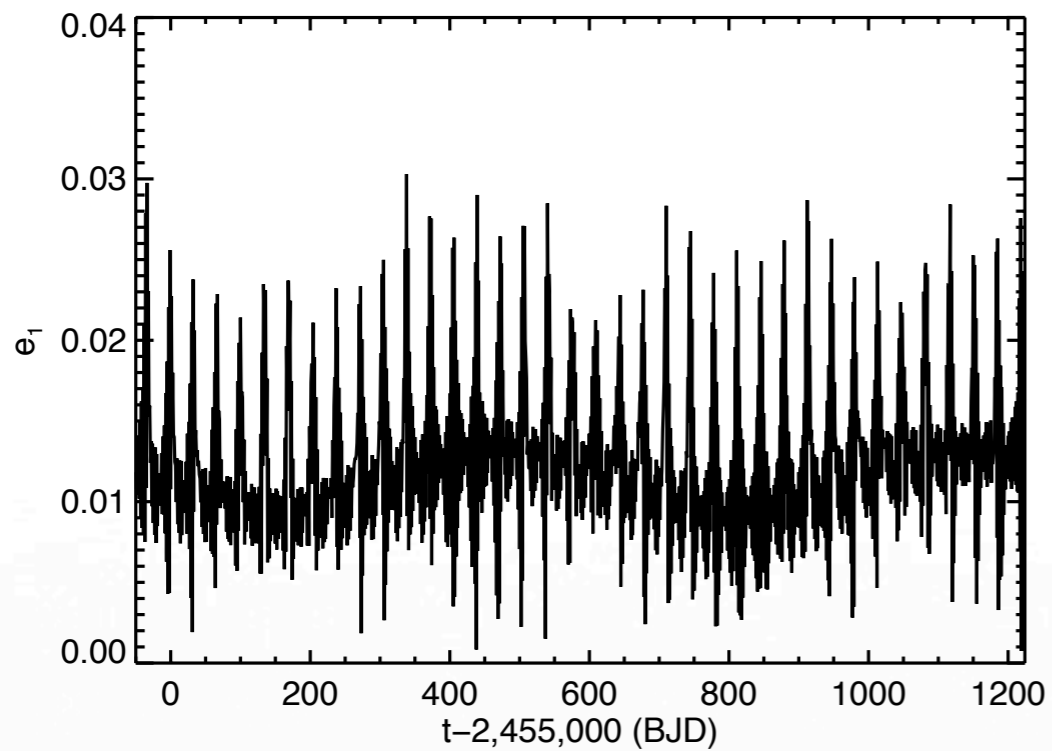


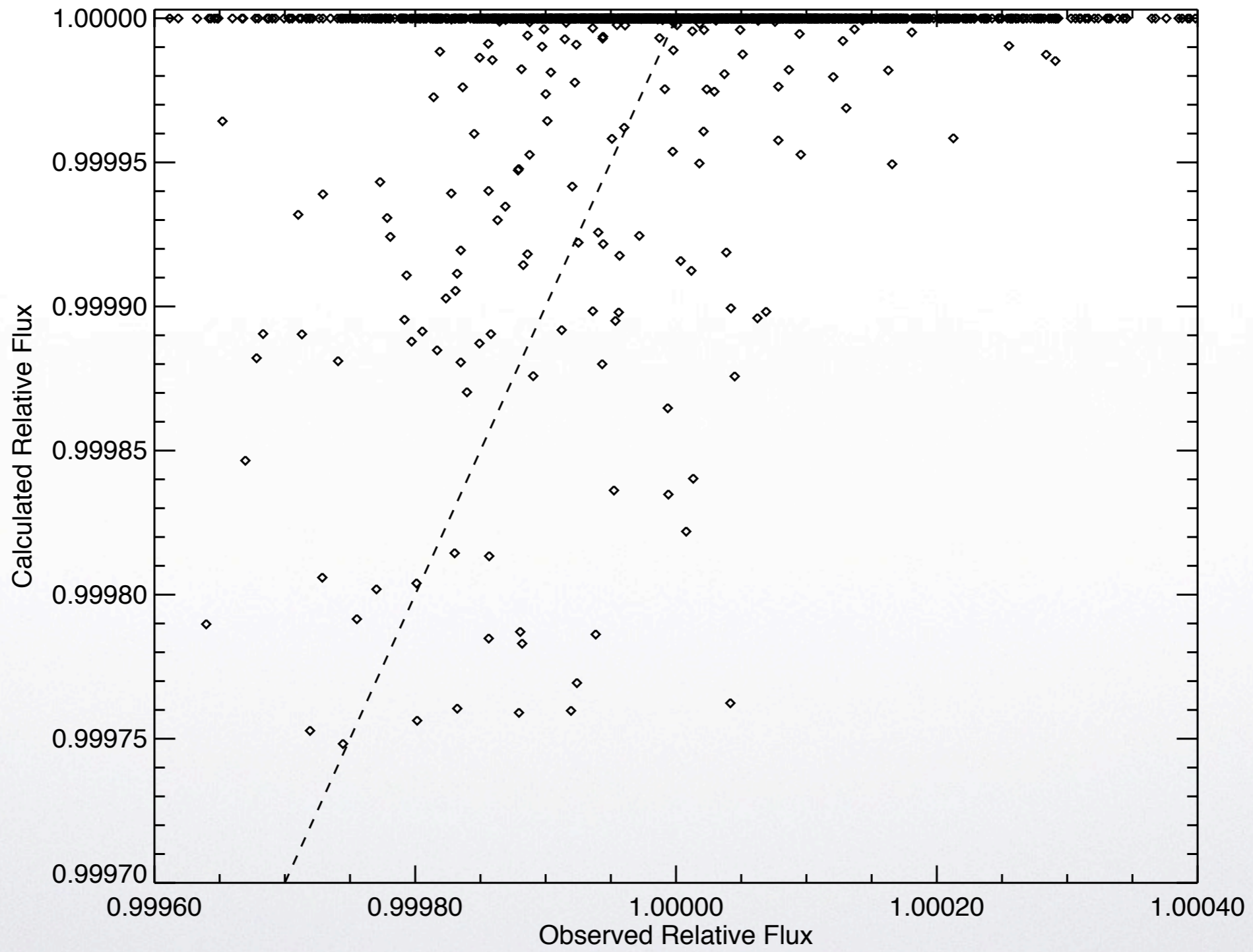


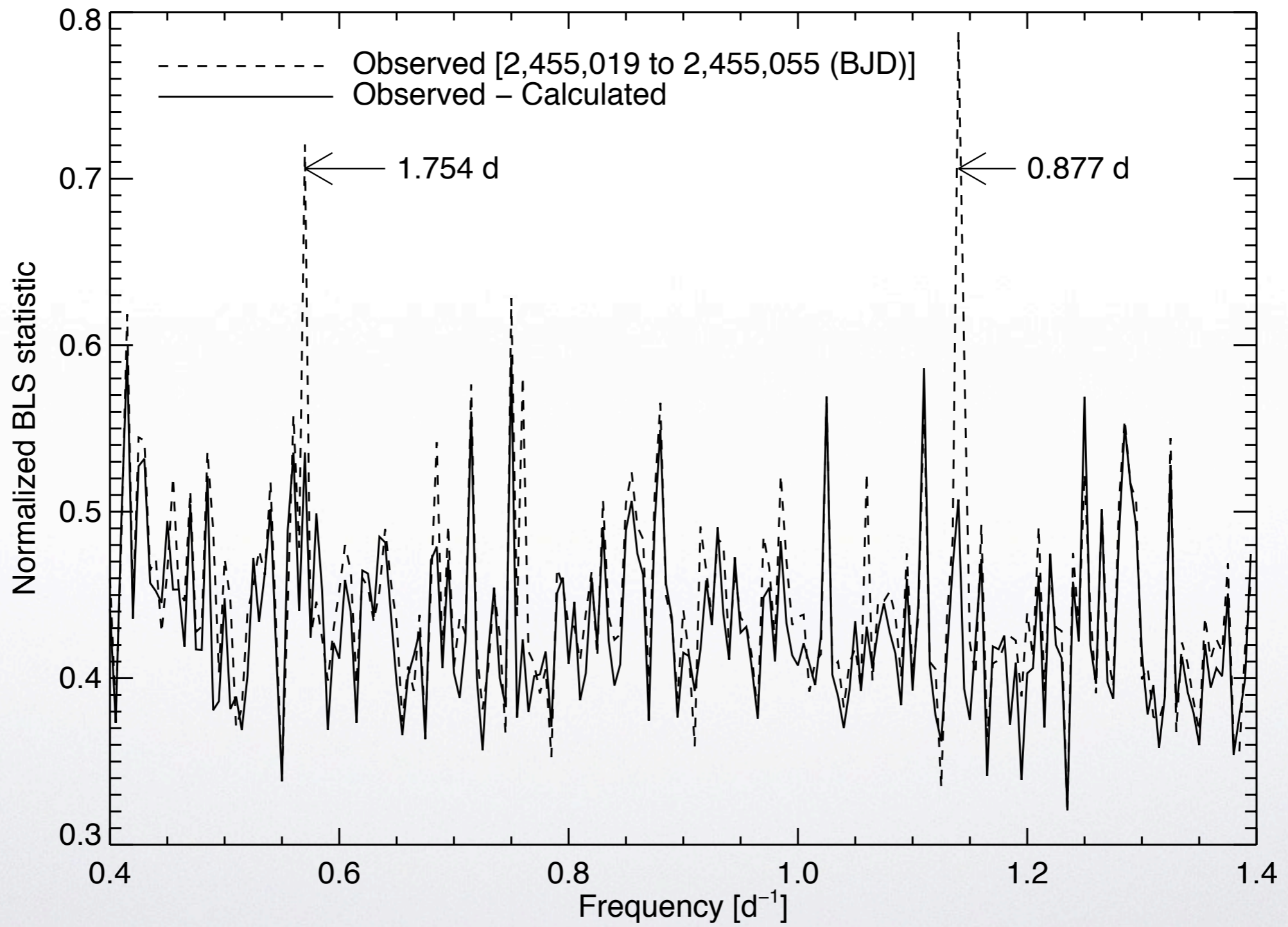


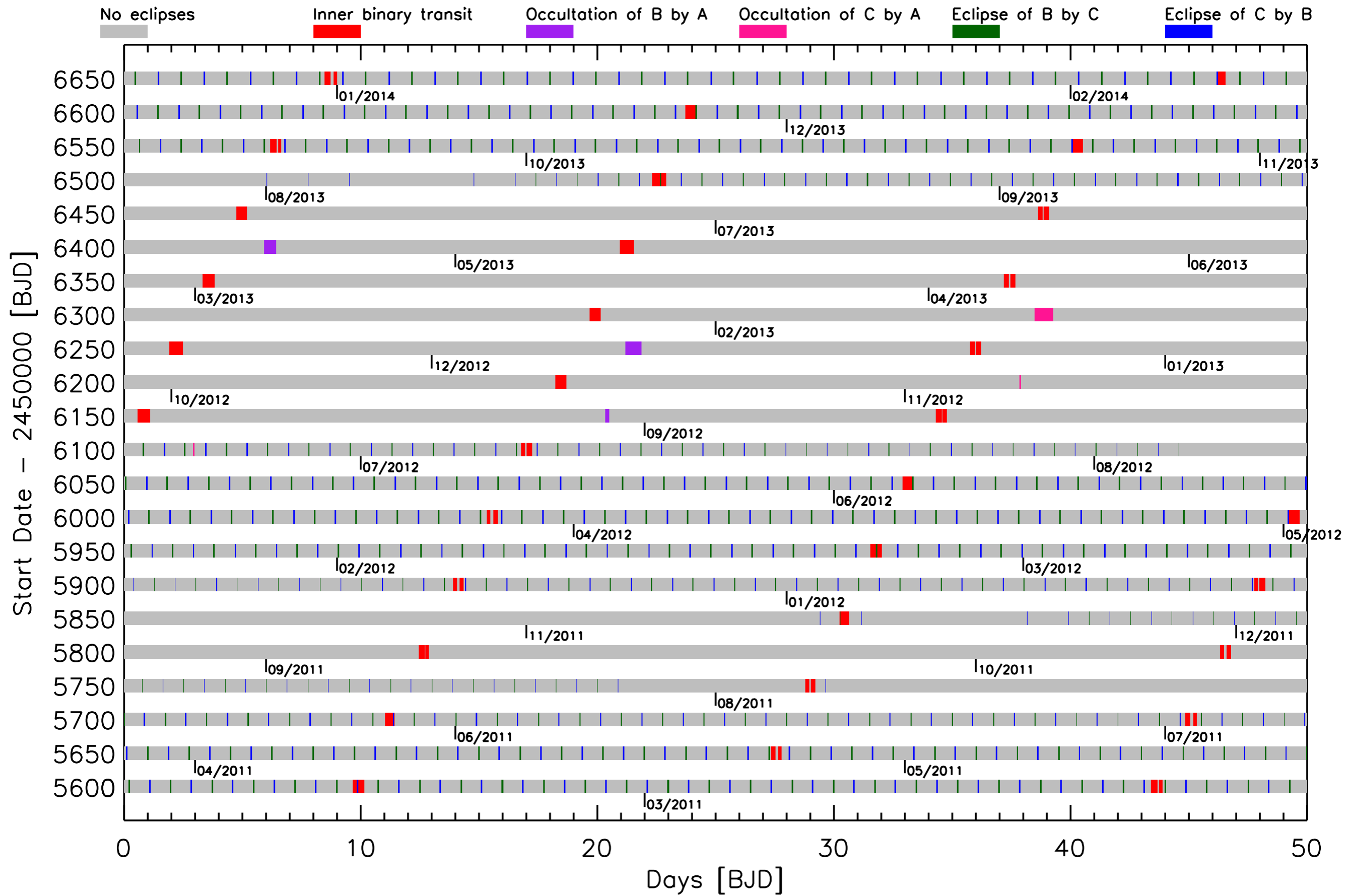


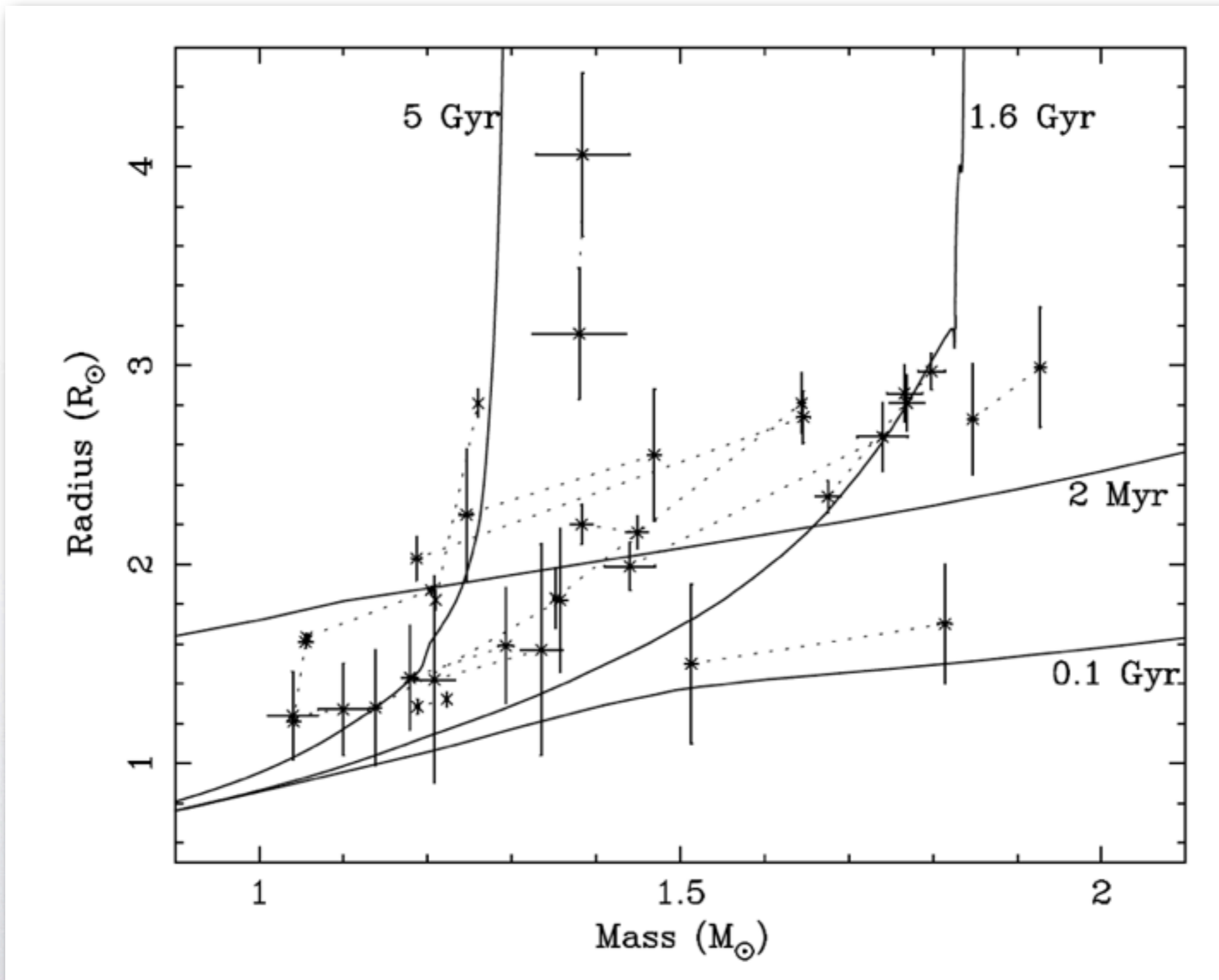












Helminiak, Konacki, Ratajczak, Muterspaugh (2009)

Kepler Eclipsing Binary Catalog

Revision: 1.96

Date: 2011-06-15

IMPORTANT NOTICE: This is a second revision of the Eclipsing Binary catalog; it follows up the first paper in the series, [Prsa et al. \(2011\), AJ 141, 83](#). It includes Q0, Q1 and Q2 data. The results are *preliminary* and may change before the paper is accepted for publication in the *Astronomical Journal*. The pre-print of the paper may be downloaded here: [Slawson et al. \(2011\), submitted](#).

IN PROGRESS: Catalog-wide manual detrending is being performed. The updates are made to this page in real time. The official catalog (V2.0) will have all data detrended.

The table fields are: Kepler Input Catalog (KIC) identifier; morphology type -- detached (D), semi-detached (SD), overcontact (OC), ellipsoidal (ELV) and uncertain (?); barycentric ephemerides (BJD_0 , P_0); Kepler magnitude (Kmag); principal parameters (temperature ratio T_2/T_1 , sum of fractional radii q_1+q_2 , orthogonalized eccentricity $e \sin \omega$, $e \cos \omega$, mass ratio q , fillout factor FF and $\sin i$; the last column contains links to three figures: raw light curve (raw), detrended light curve (dtr), and polyfitted phase curve (fit). Do not trust parameters if the polyfit curve looks bad!

You can access the initial version of the catalog (V1.0) [here](#).

The table below is sortable. Click on the column header to sort by that column.

KIC:	TYPE:	BJD_0	P_0	Kmag	T_2/T_1	q_1+q_2	q	$e \sin \omega$	$e \cos \omega$	FF	$\sin i$	Figures
01026032.00	D	54966.773843	8.460438	14.813	0.85956	0.12451	N/A	0.05515	0.01308	N/A	0.99687	raw dtr fit
01026957.00	D	54956.011753	21.762784	12.559	0.49053	0.18848	N/A	0.06237	0.07830	N/A	0.98538	raw dtr fit
01433962.00	D	54965.325203	1.592691	15.470	0.78423	0.11622	N/A	0.12883	0.07820	N/A	0.99716	raw dtr fit
01571511.00	D	54954.506187	14.021624	13.424	0.82928	0.13522	N/A	0.10259	0.02367	N/A	0.99416	raw dtr fit



Eclipsing Binaries

