

# Bloated Hot Jupiters:

## What can tides do?

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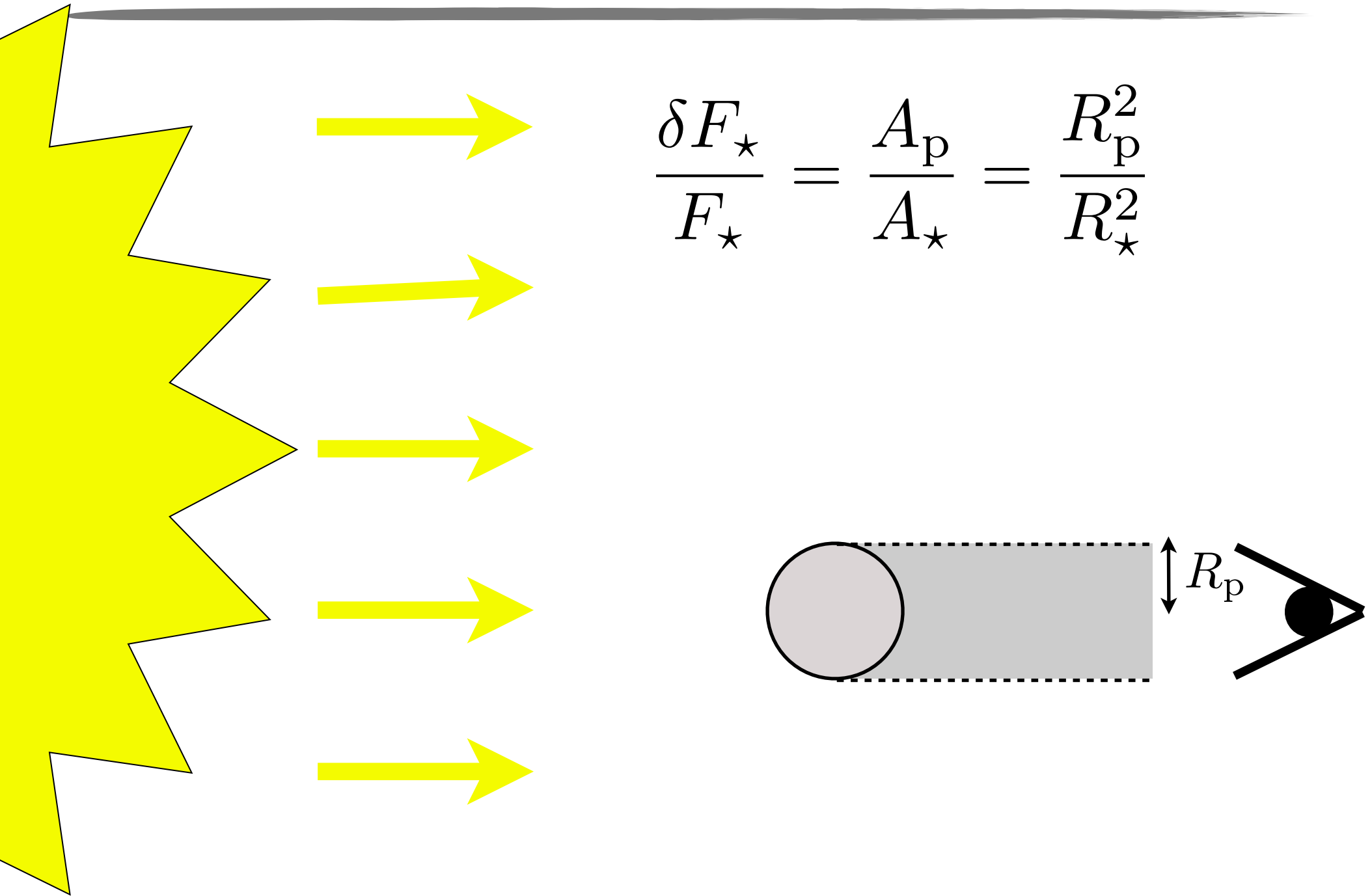
- Tidal distortion: The **true** radius of transiting planets
- Tidal friction: An efficient bloating mechanism?

Jérémy Leconte

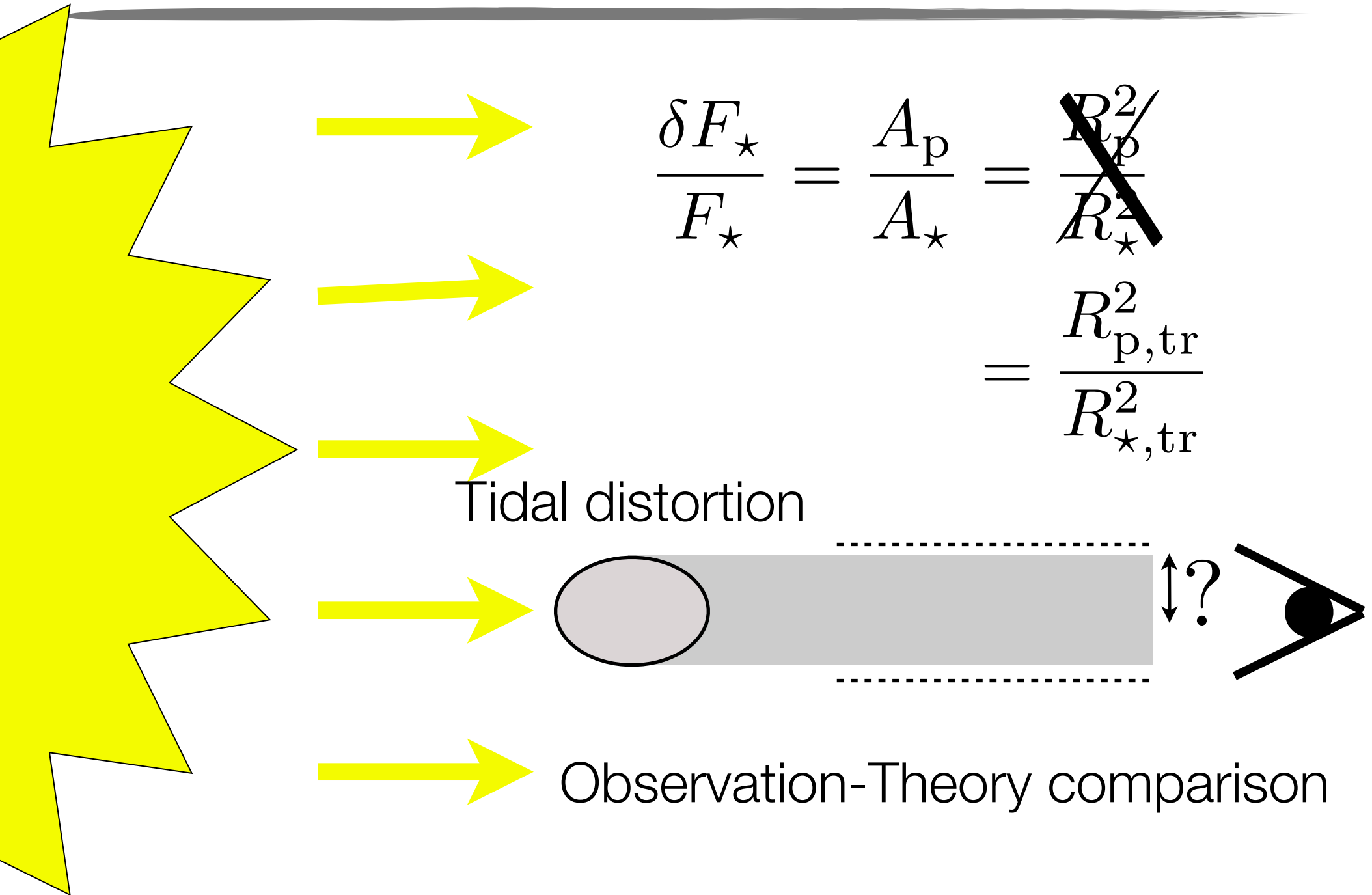
G. Chabrier, D. Lai, I. Baraffe, B. Levrard



# Effect of tidal distortion on transit measurements



# Effect of tidal distortion on transit measurements



# Analytical computation of the true radius

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Total energy

$$E = U + U' + W + W' + T + W_{\text{int}}$$

Equilibrium set of equation

$$\left\{ \frac{\partial E}{\partial x_i} \Big|_{M, J, \dots} = 0 \right\}_{x_i = r_*, \text{shape}}$$

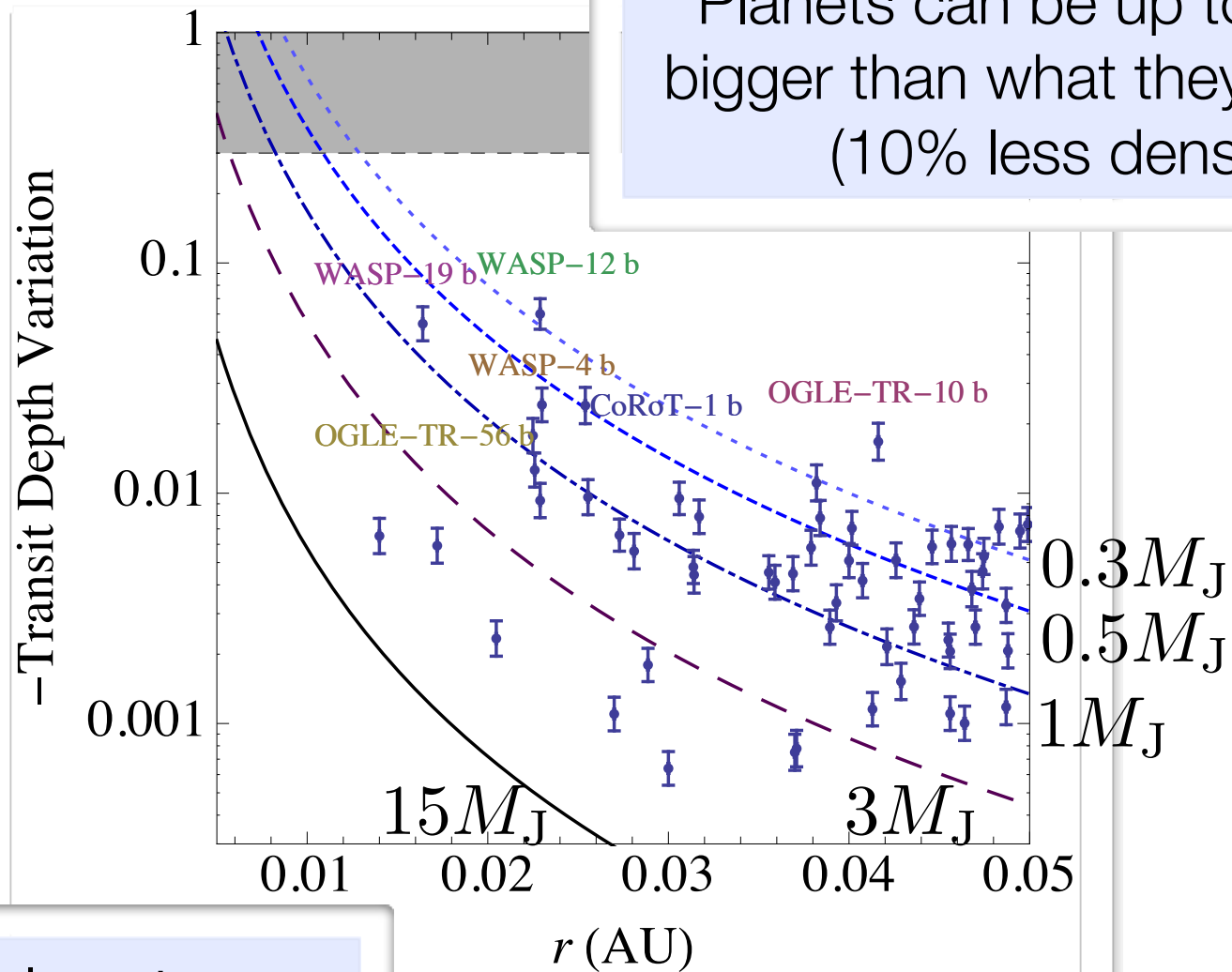
Linear regime: tides+synchronous rotation

$$\frac{R_p - R_{\text{mes}}}{R_p} = (\alpha_{\text{rot}} + \alpha_{\text{tid}}) \frac{M_\star}{M_p} \left( \frac{\bar{R}_p}{r_\star} \right)^3 > 0$$

*Lai et al. (ApJ 1994), Leconte et al. (A&A 2011)*

# A negative bias in the radius determination

Planets can be up to 3-4% bigger than what they appear  
(10% less dense)



Bloated planets are  
even more bloated!

*Leconte et al. (A&A 2011)*

Can tidal heating explain bloated planets?

Conclusion

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We don't know much  
about tidal Dissipation!!!

Can tidal heating explain bloated planets?

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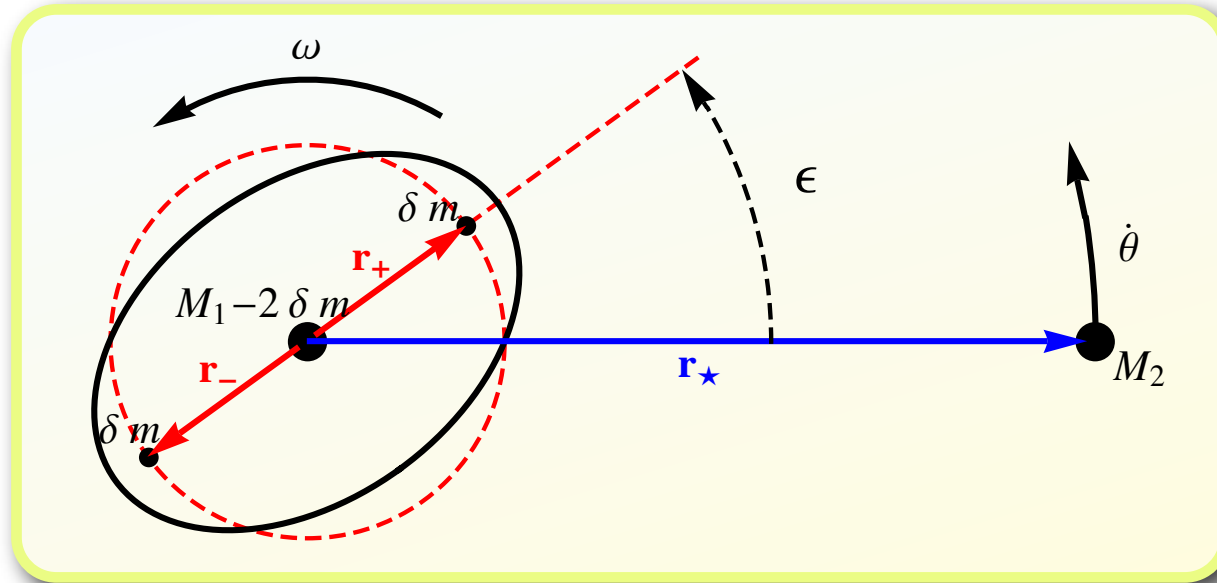
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We don't know much  
about tidal Dissipation!!!

One thing we do know is  
what an eccentric  
keplerian orbit is.



# One main theory / Two main parametrizations



What is the frequency dependence of  $\epsilon$ ?

**Constant phase lag**

$$\epsilon = 1/Q$$

- Need perturbative developments:

➔ Limited to low eccentricity and inclinations

**Constant time lag**

$$\epsilon = 2(\omega - \dot{\theta})\Delta t$$

- Linear:

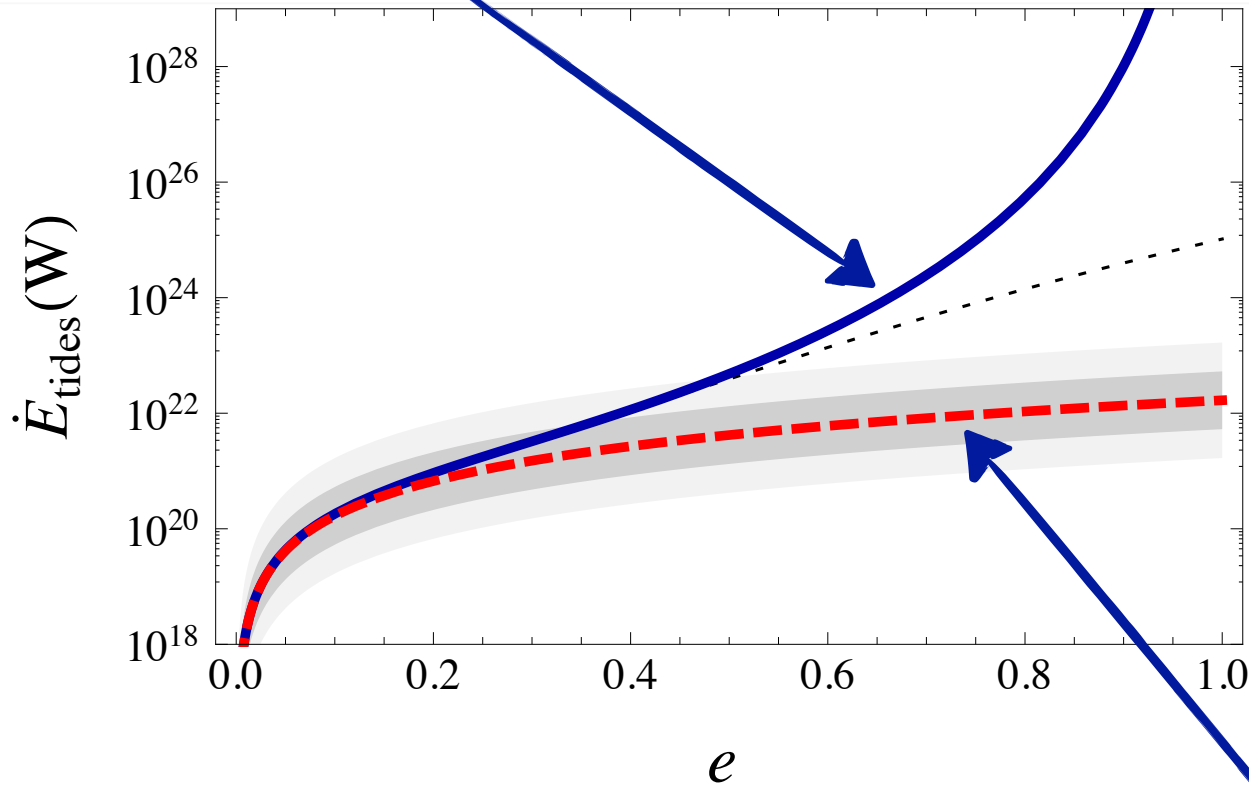
➔ Not limited in eccentricity and inclination

# Quasi circular model underestimates tidal heating

$$\dot{E}_{\text{tides}} = 2K_p \left[ N_a(e) - \frac{N^2(e)}{\Omega(e)} \right]$$

## Constant Time lag:

*Levrard et al. (A&A, 2007)*  
*Wisdom (Icarus, 2008)*  
*Leconte et al. (A&A, 2010)*



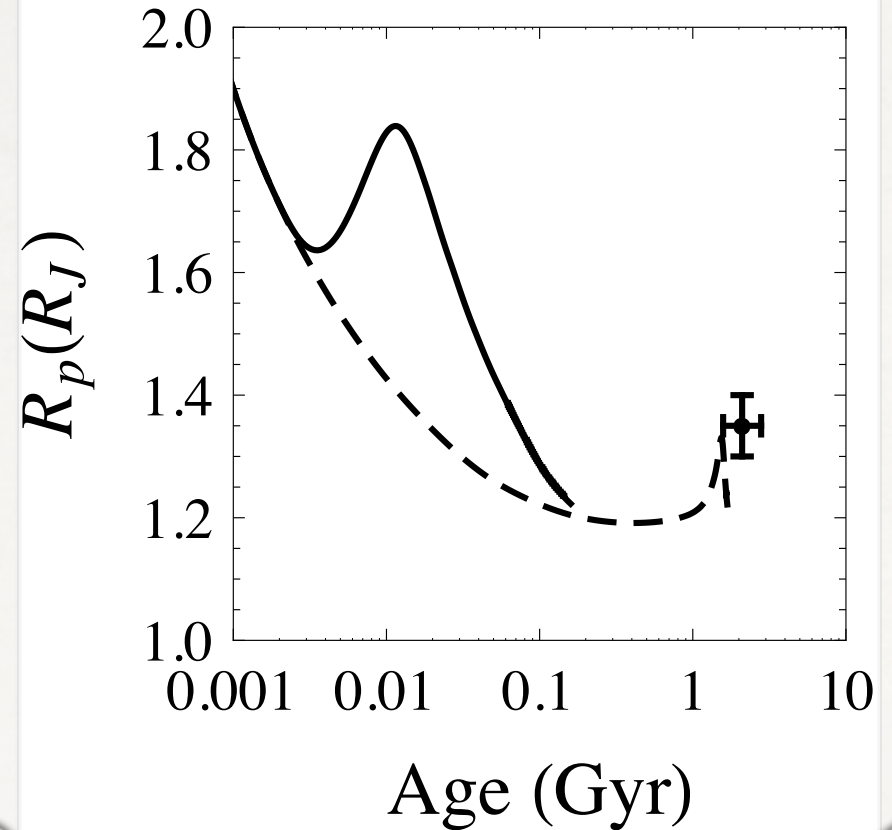
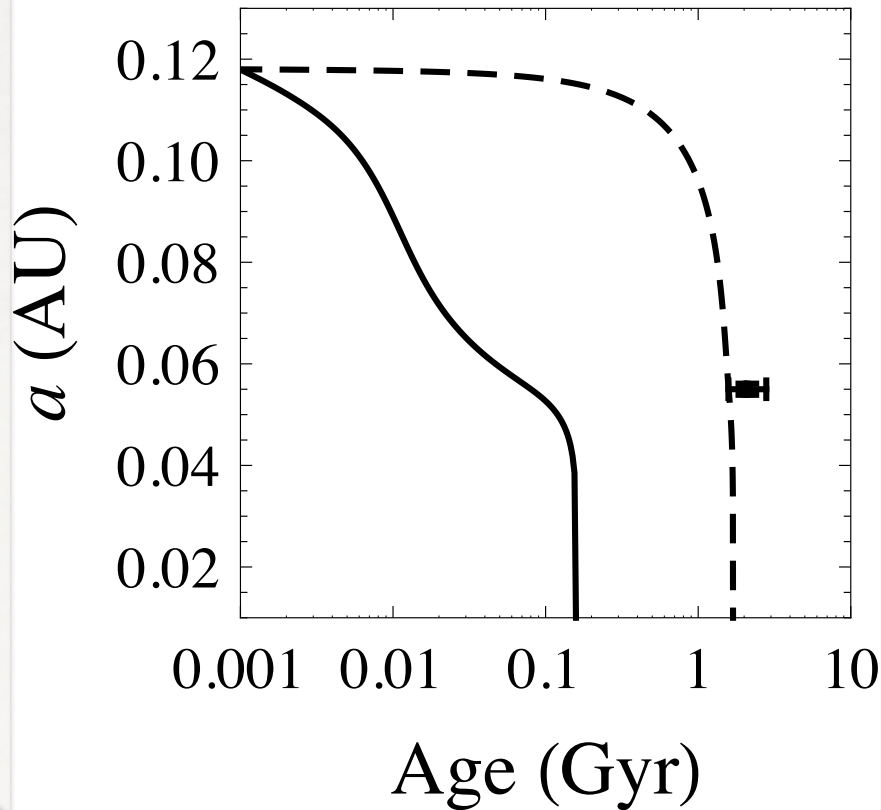
$e^2$  approx  
underestimates  
tidal heating by  
orders of  
magnitude!

## Constant Phase Lag

*Jackson et al. (Apj, 2008)*  
*Miller et al. (Apj, 2009)*  
*Ibgui et al. (Apj, 2009)*

$$\dot{E}_{\text{tides}} = 7K_p e^2$$

# Comparison with the $e^2$ model

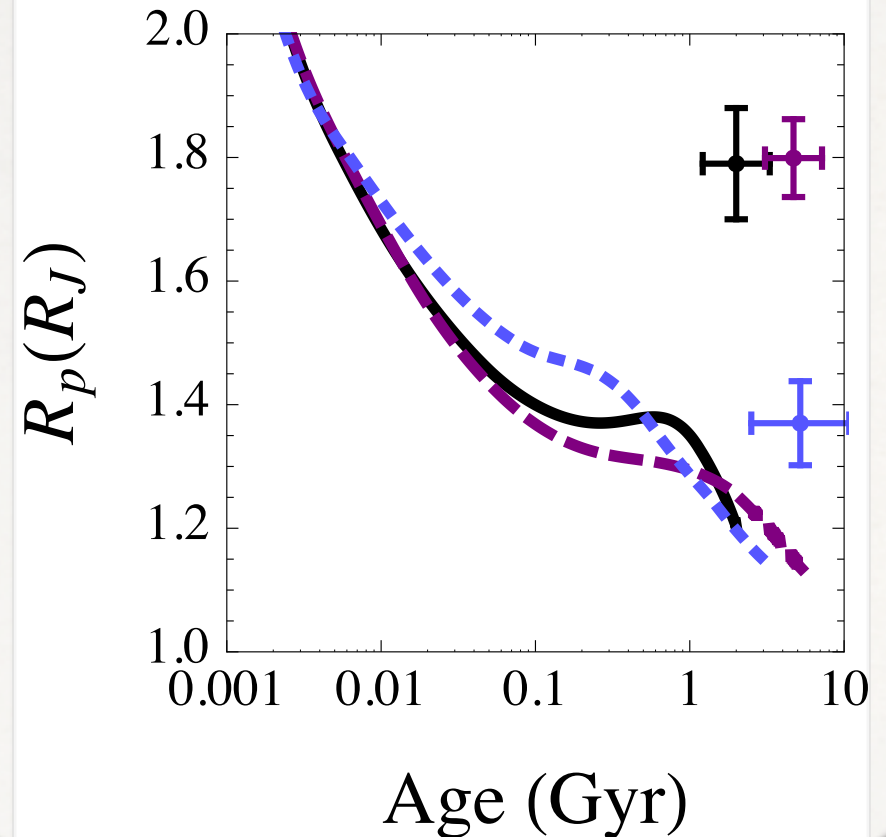
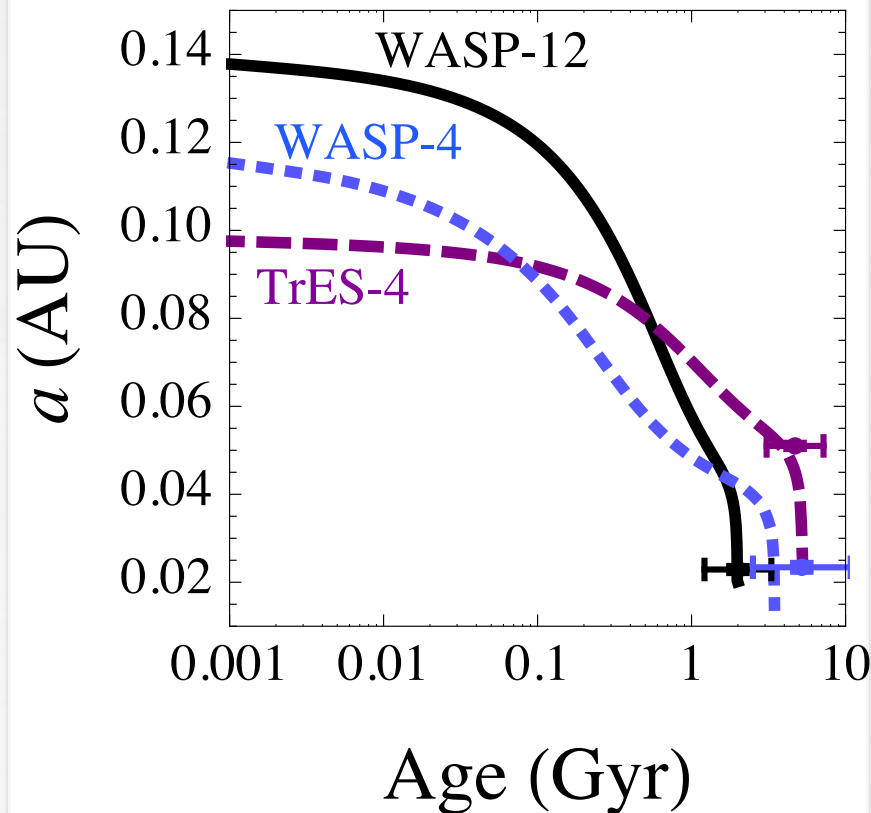


————— *Full Equations*

.....  *$e^2$  model*

With the full equations, tidal dissipation occurs **much earlier**

# Most bloated planets: Tidal dissipation arises too early



Circularization occurs **too early** to heat the planet at a **late** epoch

*Leconte et al. (A&A, 2010)*

# Conclusion

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## ★ Tidal distortion

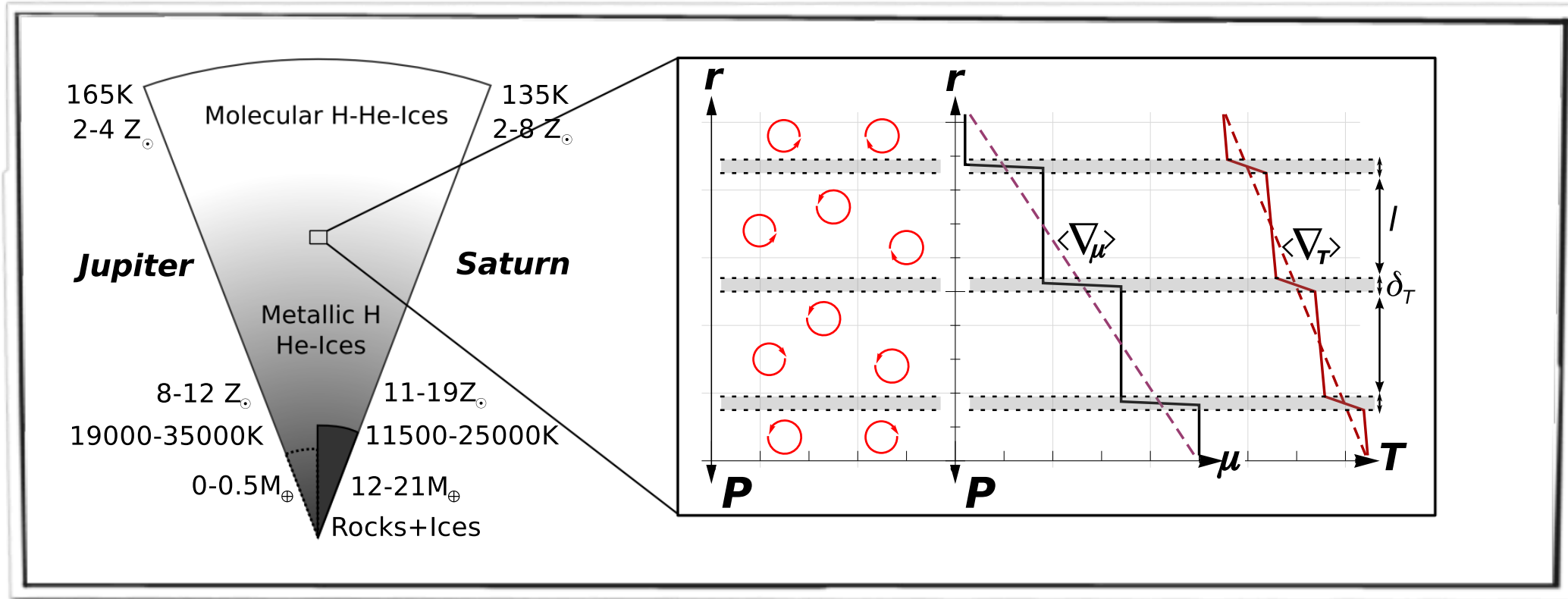
- Bias in the transit data (up to 5-10% in transit depth)
  - ➔ Can be corrected analytically
- Planets are **bigger** than what they appear

## ★ Tidal Heating

- eccentric orbits must be treated properly:
  - ➔ Complete formula or high order calculations needed
  - ➔ High orders are **not** mere corrections
- Not sufficient to explain most bloated exoplanets (for bodily tides in the 2 body problem), but has a significant contribution

# Another possible bloating mechanism:

## Double diffusive convection

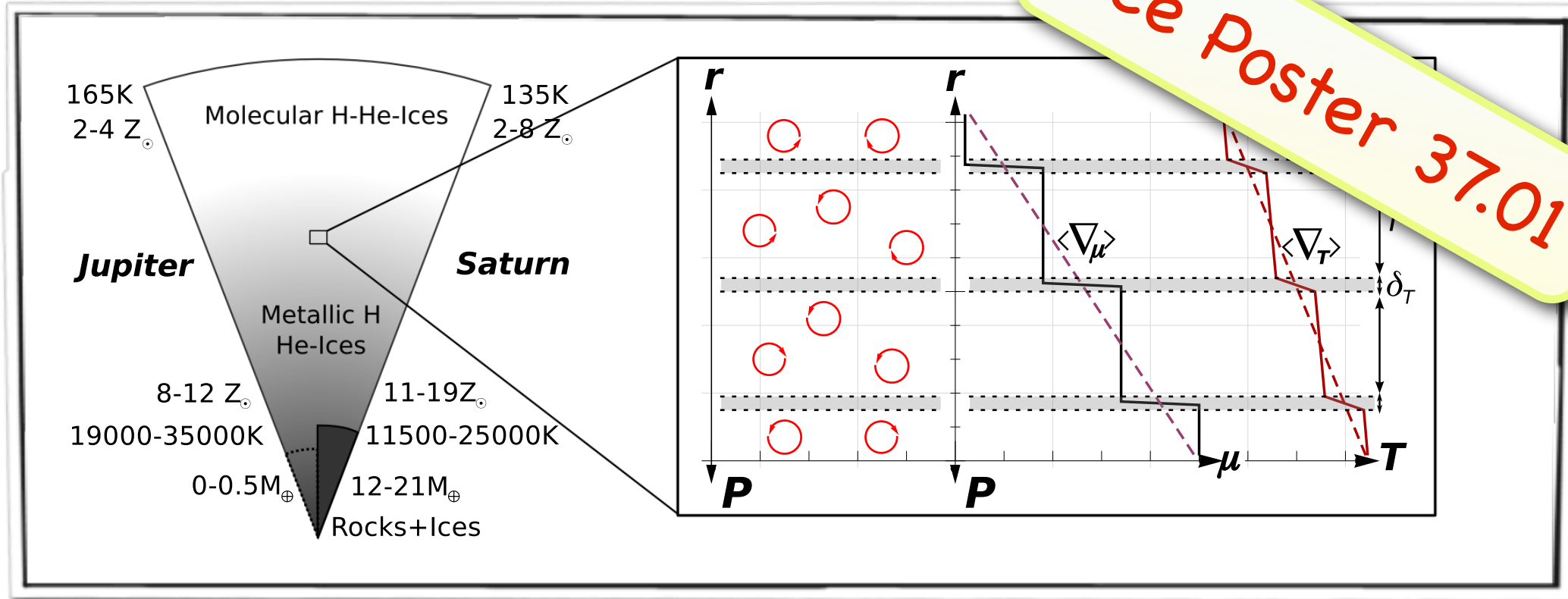


- Double diffusive convection impedes energy transport
- *Possible absence of core in Jupiter!*

*Leconte & Chabrier (Submitted)*

Another possible bloating mechanism:

Double diffusive convection



See poster 37.01

- Double diffusive convection impedes energy transport
- *Possible absence of core in Jupiter!*

*Leconte & Chabrier (Submitted)*

# Quasi circular model underestimates tidal heating

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$$\dot{E}_{\text{tides}} = 2K_p \left[ N_a(e) - \frac{N^2(e)}{\Omega(e)} \right]$$

*Hut (A&A, 1981)*

*Levrard et al. (A&A, 2007)*

*Wisdom (Icarus, 2008)*

*Leconte et al. (A&A, 2010)*

*Hansen (Apj, 2010)*

$$\frac{\dot{E}_{\text{tides}}}{7K_p e^2} = 1 + \frac{54}{7}e^2 + \frac{1133}{28}e^4 + \frac{31845}{224}e^6 + \frac{381909}{896}e^8 + O(e^{10})$$

*Jackson et al. (Apj, 2008)*

*Miller et al. (Apj, 2009)*

*Ibgui et al. (Apj, 2009)*

$$\dot{E}_{\text{tides}} = 7K_p e^2$$



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$$\dot{E}_{\text{tides}} = 2K_p \left[ N_a(e) - \frac{N^2(e)}{\Omega(e)} \right]$$

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Does not come from a particular model. Due to the strong dependence to the orbital distance ( $r^{-6}$ )

*Jackson et al. (Apj, 2008)*

*Miller et al. (Apj, 2009)*

*Ibgui et al. (Apj, 2009)*

$$\dot{E}_{\text{tides}} = 7K_p e^2$$